

Estimation of clinical dose distributions for breast and lung cancer radiotherapy treatments

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Cover illustration: Illustration of the fields in a stereotactic lung treatment (left) and loco-regional breast treatment (right), prepared by Emma Hedin in the Eclipse treatment planning system (Varian Medical Systems). Clinically used plans applied on phantoms representing simplified human torsos.

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ABSTRACT

The overall aim of this thesis was to investigate the uncertainties in the dose distribution determined at the treatment planning stage. The work has been based on the main hypothesis that the way of determining dose at the stage of treatment planning can be improved to such an extent that it affects the risk-benefit assessment. Photon beam treatments of breast and lung cancer were considered, i.e. treatments that are delivered to a region of the body that includes lung tissue. Density inhomogeneities are a challenge for the clinical dose calculation algorithms (DCAs). Another challenge for the loco-regional breast cancer treatments are the adjacent fields where the jaw positioning uncertainty may influence the uniformity of the dose distribution.

Different clinical DCAs were compared regarding their ability to calculate dose to lung (organ at risk). The differences were quantified in terms of normal tissue complication probabilities (NTCP) in Paper I. This study showed that the uncertainties in clinical DCAs can be of the same magnitude as the uncertainties of published NTCP model parameters. Adjusted NTCP model parameters were retrieved to avoid introduction of this additional uncertainty. The performance of clinical DCAs regarding calculation of target dose for the case of stereotactic (small fields) lung cancer treatments was compared to Monte Carlo (MC) calculations in Paper II. The principle-based DCA Acuros XB (Varian, Eclipse) was found to comply better with MC than the pencil-beam based analytical anisotropic algorithm (AAA) included in the study. The clinical impact of the transition from the AAA to Acuros XB was discussed. In paper III and IV breast cancer treatments were studied. The impact of jaw positioning uncertainty on the dose distribution in the case of adjacent fields was investigated in paper III. The effect on lung tissue was small whereas hotspots were found in soft tissue with unknown risks for plexus brachialis. In paper IV the performance of different clinical dose calculation algorithms in lung tissue with low density due to the breathing adaptive technique of deep inspiration breath hold (DIBH) was investigated. The clinical impact of the transition from AAA to Acuros XB was discussed. Acuros XB was compared to MC for the lowest lung density identified and the reliability of the Acuros XB calculation was confirmed. The clinical impact of the transition from AAA to Acuros XB was quantified for dose planning criteria based on different lung DVH parameters.

Keywords: External radiation therapy, breast cancer, lung cancer, clinical dose calculation algorithms, Monte Carlo, NTCP, dose planning criteria

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POPULÄRVETENSKAPLIG SAMMANFATTNING PÅ SVENSKA

Strålterapi ges som behandling vid flera olika cancerdiagnoser. Behandlingarna utformas för att maximera sannolikheten för tumörkontroll och samtidigt minimera risken för biverkningar i normalvävnaden. Det är en balansgång mellan risk-nytta som baseras på vetenskapliga studier och klinisk erfarenhet av hur mycket stråldos som olika tumörer kräver samt hur mycket stråldos som olika organ tål. Stråldosen beräknas av en dator när behandlingen planeras. Risk-nytta bedömningen görs utifrån denna beräknade fördelning av stråldosen i patienten. För att kunna göra en korrekt bedömning krävs korrekt beräknade dosfördelningar. I denna avhandling studeras hur osäkerheterna ser ut i de beräknade dosfördelningarna för bröst- och lungcancerbehandlingar. De olika kliniska beräkningsmetoderna jämförs med en referensmetod som innebär mycket noggrann och tidskrävande simulering av strålningens väg genom patienten. Denna referensmetod kallas Monte Carlo-simulering. Dessutom utreds hur dosfördelningen påverkas av osäkerheten i positionering av de rörliga delarna i strålbehandlingsmaskinen. I vissa typer av bröstcancerbehandlingar byggs dosfördelningen upp av två direkt anslutande strålfält. Om dessa fält överlappar eller är separerade på grund av att en viss inställning av fältets storlek inte efterlevs i verkligheten skulle potentiellt en överdosering eller underdosering kunna ske i skarven.

Generellt visar resultaten att det finns osäkerheter i de beräknade dosfördelningarna som är kliniskt relevanta. Den kliniska erfarenheten och de vetenskapliga studierna baseras mest på dosfördelningar beräknade med tidiga mindre exakta kliniska beräkningsmetoder. I utredningarna om beräkningsmetoderna visades att risk-nytta bedömningar baserade på mer nyligen introducerade kliniska beräkningsmetoder är potentiellt mer korrekta men att justeringar bör göras av kriterierna som används vid planeringen av behandlingen så att inte risk-nytta balansen oavsiktligt ändras. I studien om närliggande fält och risken för att de överlappar eller är separerade framkom att effekten på lungvävnad var liten men att det i fettvävnad och muskelvävnad kan kvantifieras en överdosering, vilken kan medföra risker för nerver i området.

LIST OF PAPERS

This thesis is based on the following studies, referred to in the text by their Roman numerals.

- I. Hedin, E. and Bäck, A. *Influence of different dose calculation algorithms on the estimate of NTCP for lung complications*. Journal of applied clinical medical physics 2013; 14(5):127–139.
- II. Hedin, E., Chakarova, R. and Bäck, A. *From AAA to Acuros XB for lung cancer SBRT*. Submitted
- III. Hedin, E., Bäck, A. and Chakarova, R. *Jaw position uncertainty and adjacent fields in breast cancer radiotherapy*. Journal of applied clinical medical physics 2015; 16(6):240-251
- IV. Hedin, E., Bäck, A. and Chakarova, R. *From AAA to Acuros XB for breast cancer treatment planning: Implications for dose to lung tissue*. Submitted

Appendix

In the appendix a report concerning the development of the Monte Carlo model is presented.

Hedin, E., Bäck, A., Swanpalmer, J. and Chakarova, R. *Monte Carlo simulation of linear accelerator Varian Clinac iX* Report MFT-RADFYS 2010:01

RELATED PUBLICATIONS

During my time as a PhD student I have contributed to two other published studies.

Chakarova, R., Müntzing, K., Krantz, M., Hedin, E., and Hertzman, S. *Monte Carlo optimization of total body irradiation in a phantom and patient geometry*. Physics in Medicine and Biology 2013; 58(8):2461-9.,

Spang, F J., Rosenberg, I., Hedin, E. and Royle, G. *Photon small-field measurements with a CMOS active pixel sensor*. Physics in Medicine and Biology 2015; 60(11):4383-98.

Preliminary results have been presented as follows

The effect of a change of dose calculation algorithm on NTCP for radiation induced pneumonitis – A comparative study.

Emma Hedin, Roumiana Chakarova, Anna Bäck.

Poster at European Society for Radiotherapy & Oncology 29th conference (ESTRO29). 2010, Barcelona, Spain.

Monte Carlo simulation of loco regional radiation treatment of breast cancer: A case study.

Emma Hedin, Roumiana Chakarova, Anna Bäck

Poster at European Society for Radiotherapy & Oncology 31st conference (ESTRO31). 2012, Barcelona, Spain.

Monte Carlo simulation of wedge fields: Implementing backscatter correction.

Emma Hedin and Roumiana Chakarova

Oral presentation at SWE-RAYSS annual workshop. 2014, Malmö, Sweden.

Lung-DVHs from different algorithms

Emma Hedin, Anna Bäck and Roumiana Chakarova

Oral presentation at 3rd Öresund Workshop on Radiotherapy. 2015, Helsingborg, Sweden.

From AAA to Acuros XB for lung SBRT

Emma Hedin, Roumiana Chakarova and Anna Bäck

Oral presentation at 4th Öresund Workshop on Radiotherapy. 2016, Helsingborg, Sweden.

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ABBREVIATIONS

3D / 4D	Three/Four Dimensional
AAA	Analytical Anisotropic Algorithm (DCA in Eclipse TPS)
AE	Energy level above which secondary electrons are tracked individually (secondary electrons with energy less than this value are included in the CH)
AP	Energy level above which secondary photons (bremsstrahlung) are tracked individually (bremsstrahlung photons with energy less than this are included in the CH)
AXB	Acuros XB (DCA in Eclipse TPS)
BSCF	Backscatter Correction factor
CC	Collapsed Cone (DCA in Oncentra TPS)
CH	Condensed History
CT	Computed Tomography
CTV	Clinical Target Volume
DCA	Dose Calculation Algorithm
DIBH	Deep Inspiration Breath Hold
DVH	Dose Volume Histogram
ECUT	Energy level below which the electron track is terminated and all energy is deposited locally.
EDW	Enhanced Dynamic Wedge
EUD	Equivalent Uniform Dose
FB	Free Breathing
GTV	Gross Tumor Volume
ITV	Internal Target Volume
LBTE	Linear Boltzmann Transport Equation
LGL	Loco-regional breast cancer treatment including supraclavicular lymph nodes
LKB	Lyman-Kutcher-Burman
MC	Monte Carlo

MLC	Multi Leaf Collimator
MLD	Mean Lung Dose
MU	Monitor Unit (A certain amount of charge as measured by the monitor chamber)
NTCP	Normal Tissue Complication Probability
PB	Pencil Beam (DCA in Oncentra TPS)
PBC	Pencil Beam Convolution (DCA in Eclipse TPS)
PCUT	Energy level below which the photon track is terminated and all energy is deposited locally.
PTV	Planning Target Volume
RS	Relative-Seriality
SBRT	Stereotactic Body Radiation Therapy
STT	Segmented Treatment Table
Tang	Tangential breast cancer treatment
TPS	Treatment Planning System
V_{20Gy}	Parameter from the DVH. “The volume receiving the dose 20Gy or more”. The chosen dose level varies.
$D_{98\%}$	Parameter from the DVH. “98% of the volume receives this dose or more”. The chosen volume varies.

1 INTRODUCTION

External radiation therapy is a commonly used treatment modality to treat cancer either as a stand-alone treatment or in combination with surgery and/or chemotherapy. Radiation dose in external radiation therapy is given to such a level that the cancer cells are likely to be killed (high cure rate) but the function of the normal tissue surrounding the cancer cells is likely to be maintained (low risk for complication). This risk-benefit balance is assessed at the treatment planning stage and impacts the design of the treatment plan. Today the risk-benefit balance of a treatment is most often optimized based on the physical dose distribution calculated in the treatment planning system (TPS), i.e. the delivered dose distribution is estimated as equal to the dose as calculated in the TPS. Unfortunately, the planned dose differ from the delivered dose distribution for several reasons. This project focuses on uncertainties in the calculation of dose at the planning stage that will affect the risk-benefit balance assessment, i.e. differences that stem from approximations in the computer algorithms for dose calculation and from technical tolerances of the positioning of beam limiting collimators of the treatment machine.

There are other factors, not considered in this thesis, that may cause differences between planned and delivered dose, for example, difficulties in reproducing the patient geometry/position during planning and irradiation. The differences emerge due to for example setup errors, breathing motions and tumor shrinkage. Strategies to reduce those differences are, for example, breathing adaptive techniques such as deep inspiration breath hold (DIBH) during irradiation, on-board imaging to monitor tumor/patient position and different patient fixation techniques. Nevertheless, since the current way of calculating the risk-benefit balance is based on the optimum dose distribution as shown in the TPS, the assessment of the risk-benefit balance made at the treatment planning stage is unaffected by above mentioned factors.

In the clinical work flow the dose at the planning stage is calculated with dose calculation algorithms (DCAs) in a TPS. In this thesis photon beam treatments are considered. The DCAs include different methods for how to calculate dose in the patient geometry. Today, this calculation is based on a CT scan or magnetic resonance imaging scan of the patient. In this work CT scans are considered. The calculation has to be relatively fast since the calculation is performed several times per patient by the treatment planning staff while trying to find a dose distribution that fulfills the treatment planning criteria. Since the introduction of computer based dose calculations there has been a continuous evolution of DCAs. The standard pencil beam convolution DCAs include pre-

calculated pencil beam kernels and do not model changes in lateral electron transport due to inhomogeneities. The DCA evolution then went via more sophisticated algorithms with improved modelling of lateral electron scatter. The most recent type of algorithm does not include pre-calculated scatter kernels but are instead principle based algorithms using the principle of simulating the radiation transport by tracking each individual particle or by numerically solving the Linear Boltzmann Transport Equation (LBTE).

In this project breast and lung cancer treatments are investigated. Tangential breast cancer treatments (Tang) with tangential fields covering the breast tissue are studied as well as loco-regional breast cancer treatments (LGL) including not only tangential fields but also anterior/posterior fields covering regional (supraclavicular) lymph nodes. The lung cancer treatments studied are conventional three-dimensional (3D) conformal treatments and stereotactic body radiation therapy (SBRT) treatments. All those cancer treatments have in common that they are delivered to a region of the body that includes lung tissue. In other words, the tissue inhomogeneity is large in the CT scans that the dose calculation is based on. For dose calculations in areas including lung tissue, the approximations in the clinical DCAs may result in inaccurate dose distributions [1], i.e. the dose is not accurately calculated in or near the lung tissue. Hence, for both breast and lung cancer treatments, the dose to lung as a risk organ is difficult to accurately assess as well as the dose to the target volume, i.e. the volume required to have a certain dose coverage. For the breast cancer treatments the target is in the vicinity of lung tissue and for the lung cancer treatments the target may even consist partly of lung tissue. Another challenge for the LGL case is the adjacent fields. The LGL plans investigated in this work are constructed such that the anterior/posterior fields and the tangential fields are matched in isocenter where there is no field divergence. The matching of fields is a challenge since there are uncertainties in the jaw positioning due to technical tolerances of the treatment machine. In the case of adjacent fields the jaw positioning uncertainty becomes an issue since overlapping fields may result in inadequate increase of dose and a gap between fields in a region where homogeneous target dose is desired may result in underdosage of target. Both the target coverage and dose to healthy tissue may therefore be inaccurately estimated at the planning stage. In this work those two factors, i.e. i) approximations in clinical DCAs and ii) impact of technical tolerances on adjacent fields, are investigated regarding how they affect the accuracy of dose calculation at the stage of treatment planning.

To make the work clinically relevant the inaccuracies in dose distributions are quantified in terms of changes in the dose volume histograms (DVHs) generally and also in terms of the dose volume histogram parameters

commonly used in dose planning criteria, e.g. the target volume receiving at least 100% of prescribed dose or the lung volume receiving more than 40% of prescribed dose. In one of the studies in this work the differences in dose distributions was quantified by differences in Normal Tissue Complication Probability (NTCP) values for lung tissue.

As mentioned above, basing the risk-benefit balance assessment on the plain physical dose rather than on an estimated biological effect in tissue is common practice. One reason is that the uncertainties in the estimation of biological effect are large. However, the transition from physical dose based evaluation to evaluation based on estimates of biological effect has the potential of improving clinical outcome since the biological effect is more correlated to treatment outcome as compared to the plain physical dose. Ideally the relationship between the delivered dose distribution and the risk for complication would be known for each specific patient. As of today this is not the case. The difficulties in determining the relationship between dose distribution and probability of complication is an effect of many factors and phenomena. For example, the average dose response curve must be modelled for a certain population since the radiation sensitivity for each individual patient is not known. The epidemiological studies therefore require large data sets to reduce the statistical uncertainty to an acceptable level. Furthermore, the determination of the delivered dose distribution, which is linked to the response, is not trivial. The delivered dose distribution and the planned dose distribution differ for several reasons as discussed above. In this work NTCP models and published model parameters are used without any consideration of their accuracy. However, the results of how the NTCP estimate is affected by choice of algorithm also indicate how the uncertainties in the DCAs introduce uncertainties in the NTCP modelling.

More accurate calculation of the dose distribution in or near lung tissue will be of importance for both breast and lung cancer treatments. For conventional lung cancer treatments lung toxicity in some cases limit how high dose that can be delivered to the target. Therefore, a more accurate assessment of lung dose is important to avoid delivering less dose than actually possible. Furthermore, with a more reliable calculation the safety margins can be reduced. For lung SBRT the dose is prescribed to a target partly consisting of lung tissue. Using DCAs with approximate inhomogeneity corrections potentially results in differences between prescribed/planned and delivered dose to target. The breast cancer treatments are delivered to a large group of patients with a long expected survival and in general in good health. This group will benefit from more accurate calculation of lung dose and lung tissue NTCP estimates since

this enables a reduction of the lung dose which can lead to a better quality of life.

When evaluating clinical dose calculation algorithms the commonly used reference method in the medical physics community is the Monte Carlo (MC) method. Also in this work MC calculations are used for comparison to find and quantify the weaknesses of the clinical DCAs. In general the MC calculations involve simulation of individual particles transport through the accelerator and the patient. To distinguish between the clinical MC algorithms that involve approximations to reduce calculation times the non-approximate MC method is sometimes referred to as ‘full MC’. The full MC simulation is used as reference method in this work. This method involves simulation of primary particle transport through the treatment accelerator head for each field used and then subsequent simulation of the particle transport within the patient/phantom. The absolute dose calibration is based on measured data for the calibration geometry. The MC method has the potential of being very accurate. However, the accuracy depends on the input. For example, the representation of the geometry of the accelerator head must be appropriate. When measured and simulated data are found to comply for a number of fields applied on a homogenous water phantom it is assumed that the systematic error in simulated dose for any other geometry is small compared to the systematic errors in the clinical DCAs. On the other hand, the MC method due to its nature gives dose distributions with statistical noise. This must be recognized and sufficient simulation time must be allowed to reduce the statistical noise so that it does not have an impact on the result.

2 AIM

The studies in the current work are based on the main hypothesis that the way of determining delivered dose at the stage of treatment planning can be improved to such an extent that it affects the estimated risk of complication and/or the appropriate treatment planning criteria.

2.1 Paper I

The objective of this work is to determine how to change the NTCP model parameters for lung complications derived for a simple correction-based pencil beam dose calculation algorithm in order to make them valid for other dose calculation algorithms. The studied dose calculation algorithms are Pencil Beam (PB) and Collapsed Cone (CC) both in Oncentra v4.0 TPS (Nucletron/Elekta) as well as Pencil Beam Convolution (PBC) and Analytical Anisotropic Algorithm (AAA) both in Eclipse v8.9 TPS (Varian Medical Systems). This work includes three types of treatments — tangential and locoregional breast treatment and conventional (no SBRT) lung treatment — to study how the results are affected by the type of treatment. The effect on NTCP of changing dose calculation algorithm is presented in relation to the reported uncertainties in the original model parameters.

2.2 Paper II

The aim of this study is to quantify the individual differences between target coverage calculated with two different DCAs and full MC respectively, for SBRT lung treatment plans. The DCAs included in the study are AAA and Acuros XB (AXB) in Eclipse v11.0.31 (Varian Medical Systems). SBRT plans originally planned with AAA will be recalculated with AXB and MC and a subgroup of plans presenting the largest differences between AAA and AXB will be replanned with AXB to analyze the effect of changing from AAA to AXB based treatment planning for SBRT lung treatments. The second aim is to search for patient/plan characteristics that characterize the subgroup of plans presenting larger differences between AAA and AXB. The overall goal is to present complementary data needed for an attentive transition from AAA to AXB for SBRT treatment planning.

2.3 Paper III

The objective of this work is to study the influence of the uncertainties in the jaw position on the dose distribution in the patient geometry of a LGL (including regional/supraclavicular lymph nodes) breast cancer treatment which involves adjacent fields. Furthermore, it is investigated how a treatment planning protocol including field overlap of 1 mm affects the situation. This case study will contribute to the understanding of the benefits and disadvantages of using 1 mm overlap and if there is a need for further optimization of such a treatment protocol. The MC method is used to obtain the dose distributions. It is a reference method for validation of clinical dose calculations in the presence of heterogeneities, in the penumbra and in the buildup region and allows for a 3D dose evaluation including the use of DVH parameters currently used to specify dose planning criteria. The effect of ± 1 mm uncertainty in the jaw positioning is investigated by the two extreme situations of gap and overlap of the adjacent fields that may happen in the reality. In particular, these extremes are 2 mm gap or overlap in the case of a planning protocol without gap or overlap, as well as 1mm gap and 3mm overlap in the case of a planning protocol with 1 mm overlap (used in our hospital for all loco-regional breast cancer treatments).

2.4 Paper IV

The overall goal of this study is to present data needed for the transition from AAA to AXB by investigation of the differences in lung dose between AAA, AXB and MC in free breathing (FB) CT-scans and DIBH (low lung density) CT-scans, for both tangential and loco-regional (including regional/supraclavicular lymph nodes) breast cancer treatment plans. The aim is to describe the impact of lung density on the differences between AAA and AXB by calculating two treatment plans per patient – one on FB CT scan and one on DIBH CT scan. By evaluating the lung density in DIBH CT scans for a large population the results are generalized. Furthermore, two cases of low lung density are identified in this large population and calculated with AAA, AXB as well as with full MC.

3 THEORETICAL BACKGROUND

3.1 Monte Carlo simulation with EGSnrc research code

In the MC method the transportation of each particle in a radiation field is simulated by sampling from probability distributions determining for example type of interaction. With MC as reference dose calculation method the calculation uncertainties due to model approximations are assumed to be small compared to when TPS dose calculation algorithms are used. However, to calculate a dose distribution with MC a model of the accelerator must be accurately tuned by comparing MC calculated data with experimental data in water phantom. Using the MC model for calculation of dose distributions in patient geometry also requires an accurate representation of the patient geometry with reliable tissue segmentation based on the CT image.

To ensure an accurate MC calculation there are also some basic underlying information that must be accurate, including elemental material composition, random number generators and probability distributions. In this implementation of the MC method those factors are not assumed to be an issue for the accuracy of the calculation.

There are different general MC transport codes. In this section the transport of photons and electrons in EGSnrc will be briefly outlined. The general procedure for photon MC simulation utilized in EGSnrc can be divided into four steps (summary by Frederic Tessier presented on the IAEA course on the EGSnrc code package, Trieste 2011. The details can be found in EGSnrc documentation ‘PIRS-701’[2]).

1. Decide **how far** to go until next interaction
2. Transport on a **straight line** to the interaction site taking into account geometry constraints.
3. Select which **interaction** takes place
4. Change **energy and direction** according to the corresponding differential cross section.

When it comes to simulation of electron transport the approach is different. Slowing down an electron results in many more interactions with surrounding matter. Each interaction event therefore cannot be simulated separately due to limitations in computer power. One solution to this is called ‘condensed history’ (CH) technique and was developed by Berger et al. [3]. This technique

is implemented in EGSnrc. In this technique all events where the energy loss is smaller than a given value is ‘condensed’ and represented by one larger electron step. The CH technique requires several algorithms and quantities to accurately take all interactions into account. For example the concept of restricted stopping power. The restricted stopping power is the total stopping power excluding all events creating secondary particles with energy above the energy level at which secondary particles are allowed. A secondary particle is either an electron that is knocked out in an interaction event or a bremsstrahlung photon. For electrons knocked out in an interaction event this energy level is specified by the parameter AE and for bremsstrahlung photons the corresponding parameter is AP. Details about restricted stopping power and other essentials in the CH technique as implemented in EGSnrc can be found in EGSnrc user’s manual PIRS-701 [2].

The user must also select the energy below which a particles track is terminated and all energy is deposited locally. The parameter that sets this is called ECUT for electrons and PCUT for photons.

The MC simulation of a treatment accelerator starts with electrons incident on the target slab at the top of the accelerator head. Once the treatment head geometry is defined according to specifications from the vendor the process of adjusting the basic parameters for the model can start, i.e. the parameters describing the characteristics of the electrons incident on the target slab. The process is schematically described in Figure 1. It starts with a parameter guess and then the particles exiting the accelerator head are collected collected in BEAMnrc information about particle type, location, energy and direction is stored in a ‘phase space’ file. The phase space is used as input in the next step where dose is calculated in water phantom in DOSXYZnrc. Measured data and simulated data are subsequently compared. The process is repeated until the differences between measured data and simulated data are within acceptance for all field sizes analyzed.

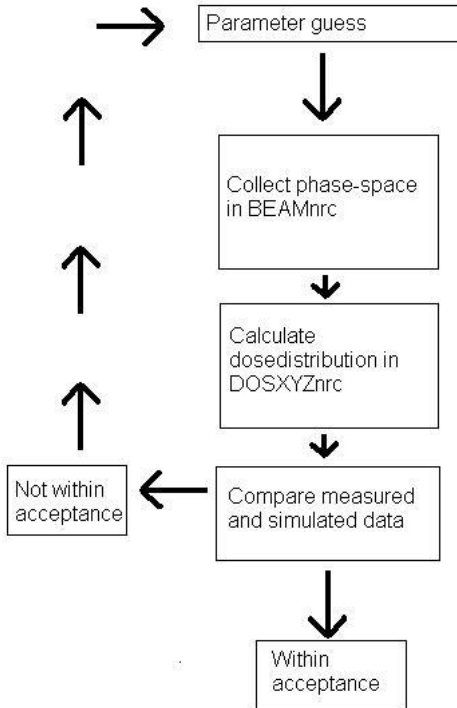


Figure 1. Schematic picture of the work of adjusting the basic parameters in the MC model of the treatment accelerator head.

3.1.1 Simulation of dynamic wedge

To be able to deliver a desired dose distribution the accelerator head has components that shapes the fields in a specific treatment. The collimator ‘jaws’ roughly limits the beam to the appropriate field size and the multi leaf collimator (MLC) refines the shape of the field. Both are modelled in the MC method. Furthermore, the treatments considered in this work sometimes includes a dynamic wedge. For a field that includes a dynamic wedge one of the jaws defining the field size in the y-direction is moving (closing the field) during irradiation.

The MC method involves different techniques of sampling from probability distributions using random numbers. To prepare for the work of simulating dynamic wedges and the elaboration on backscatter (see section 4.3.4) the sampling technique used for simulation of dynamic wedges in EGSnrc is discussed briefly here.

Wedge fields are generated by the DYNJAWS[4, 5] code option following Varian Enhanced Dynamic Wedge (EDW) implementation. The dynamic movement of the upper jaws is controlled by the so-called segmented treatment tables, STT. Each STT contains information on the jaw position versus dose delivery information at different instances of the EDW field in form of cumulative weighting of monitor units (MU). A single STT, (the one for 60° wedge), is used to generate all the other STTs for various field sizes and wedge angles.

By using this position probability sampling the movement of the jaw is simulated to be continuous (more realistic) as opposed to the step and shoot approximation.

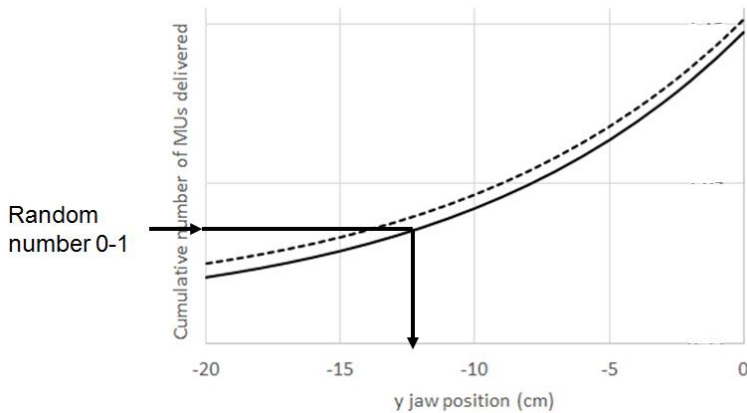


Figure 2. Sampling from the cumulative probability distribution of a STT. Transformation method! The dotted line is backscatter corrected, this is discussed in Section 4.3.3

Why sampling from the cumulative probability distribution function is correct can be intuitively understood. The random numbers are homogeneously distributed between 0 and 1. We want a mapping that transforms this homogeneously distributed variable to values of jaw position. The cumulative probability distribution function is constructed such that when a random number, say 0.45, is chosen on the y-axis (see Figure 2 above) this means that 45% of the random numbers are going to be below this value (since they are homogeneously distributed) and also that 45% of the jaw position values are going to be smaller than this value (according to the definition of the cumulative probability distribution function). The jaw position values between -20 and -15 in Figure 2 above will be more seldom chosen than jaw position values between -5 and 0 since in the latter interval the STT curve is steeper. The intervals can be made arbitrarily small and the reasoning is still valid.

3.1.2 Impact of statistical noise on DVH

Due to its nature the MC calculated dose distribution is fluctuating with statistical noise. When the true dose distribution of a certain structure is homogenous with all voxels in this structure receiving the same dose, then the MC calculated dose distribution will have voxels appearing to receive both smaller and larger dose than the true value. The impact of statistical noise in the dose distribution on the DVH can be intuitively understood when this homogeneous dose distribution is considered. The true DVH (cumulative) will then consist of a horizontal line up until the dose value that all voxels receive where the DVH abruptly decreases to zero. For the MC calculated dose distributions some of the voxels receive smaller dose values than the true value. Therefore, the MC calculated DVH curve will start to descend before the true abrupt decrease of the DVH. Furthermore, the DVH will not decrease all the way down to zero after the true dose value since some voxels are calculated to receive a higher dose than the true value. So, the noise of the MC calculation will cause the DVH to be flattened out, see an illustration of this in Figure 3. The larger statistical uncertainties in the dose distributions the larger the effect will be on the DVH. The dose distribution discussed so far is similar to that of a target structure – similar dose to all voxels of the structure. For a risk organ the dose distribution is much more inhomogeneous and the DVH will be different. The same principle of how statistical noise (in the dose distribution) affects the DVH of course also applies to the risk organs. However, for the risk organs one also has to consider the situation of voxels with dose values close to zero. A fairly large volume may receive low dose but in a noisy dose distribution with few interactions only a fraction of this volume may be ‘detected’. Additionally, voxels with large relative statistical uncertainty (small dose values and large statistical uncertainty) are commonly zeroed.

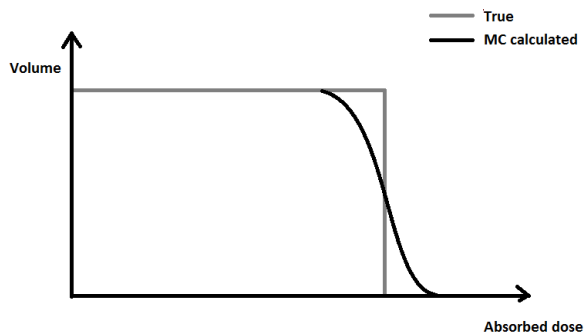


Figure 3. Illustration of how a true DVH is distorted by statistical noise in the MC calculation.

3.2 Clinical dose calculation algorithms

In this work the clinical DCAs are used as ‘finished products’. There is no attempt to suggest improvements or to explain the behavior of the algorithms at any deeper knowledge level. Nevertheless, some basic information about the algorithms has been helpful in formulation of research questions and is also helpful in the discussion of the results.

The algorithms used are the Pencil Beam (PB) and Collapsed Cone (CC) algorithms from Oncentra Masterplan TPS (Nucletron/Elekta) as well as Pencil Beam Convolution (PBC) with modified Batho inhomogeneity correction, Analytical Anisotropic Algorithm (AAA) and Acuros XB (AXB) from Eclipse TPS (Varian Medical Systems). Different versions of the algorithms has been used corresponding to the most recent version implemented at the hospital at the time for the study.

The two standard pencil beam algorithms PB and PBC have different approaches to for examples how to determine the pencil beam scatter kernels. PB uses Monte Carlo calculated kernels whereas PBC uses a method based only on the measured data described in [6]. How the scatter kernels are adjusted in case of inhomogeneity in the patient/phantom are also different according to the user manuals. They have that in common that the inhomogeneity correction is only based on the density along the fan line, i.e. the inhomogeneity correction does not include a correction of the lateral electron scatter[1]. The DCA evolution then went via more sophisticated algorithms such as AAA and CC. AAA include inhomogeneity correction of the scatter kernels in multiple lateral directions (normal to the beam direction) [7], i.e. not only in the beam direction which is the case in PB and PBC. CC is based on point kernels[8] rather than pencil beam kernels that PB, PBC and AAA are based on. The most recent type of algorithm used in this study is AXB. AXB does not include pre-calculated scatter kernels but is instead principle based. AXB numerically solves the Linear Boltzmann Transport Equation (LBTE)[9].

3.3 Uncertainties in jaw positioning

A method for determining the uncertainties in jaw positioning due to technical tolerances has been developed earlier in our hospital [10]. It is based on EPID (electronic portal imaging device) images of adjacent fields that are analyzed for a particular gantry angle. Jaw positional uncertainty of up to 1 mm has been detected for the Varian Clinac iX accelerators in our hospital and sometimes systematic shifts that holds during an entire patient course.

4 MATERIAL AND METHODS

4.1 NTCP models

The normal tissue complication probability (NTCP) is used to evaluate the risk for complication after radiotherapy. The NTCP value is calculated for a specific end-point. For example, the end-points for lung tissue is commonly different grades of pneumonitis.

Two NTCP models are used to calculate NTCP in this work. They are described below. The lung DVHs are corrected for fractionation effects according to the linear-quadratic model (LQ-model) using $\alpha/\beta = 3$ Gy and dose per fraction = 2 Gy. This is made to match the way the original model parameters are retrieved.

4.1.1 LKB-model

NTCP is calculated using the Lyman-Kutcher-Burman model (LKB-model) [11, 12] with the DVH reduced to EUD following Niemiero et al.[13] and model parameters [D50, m, n]. The formula used for NTCP calculation according to the LKB-model is described in Equation 1 and the formula for calculating EUD for the NTCP model is described in Equation 2

$$NTCP_{LKB} = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^t e^{-\frac{x^2}{2}} dx, \quad (1)$$

$$\text{where } t = \frac{EUD - D_{50}}{mD_{50}}$$

$$\text{and } EUD = \left(\sum_i v_i D_i^{1/n} \right)^n. \quad (2)$$

4.1.2 RS-model

NTCP is also calculated using the Relative Seriality (RS)[14] model with the model parameters [D50, γ , s]. The formula used for NTCP calculation according to the RS-model is described in Equation 3, notation following Rancati et al. [15] V_i is the fractional volume receiving the dose D_i .

$$NTCP_{RS} = \left[1 - \prod_{i=1}^M (1 - P(D_i)^s)^{V_i} \right]^{1/s}, \quad (3)$$

where M is the number of subvolumes (number of dose bins in the DVH), and $P(D_i) = 2^{-\exp(e\gamma(1-D_i/D_{50}))}$.

For the LKB-model a reduction of the DVH to EUD is performed as a step in calculating NTCP (see eq 2). To be able to plot NTCP values against a single dose value, EUD is calculated also for the RS-model. For the RS-model EUD is calculated from the NTCP value as the uniform dose that would yield the same NTCP (see eq 4).

$$EUD_{RS} = D_{50} * \frac{(1 - \log(-\log(NTCP)))}{\log(2) * e\gamma} \quad (4)$$

4.1.3 NTCP-model parameters from clinical studies

Model parameters were taken from four different studies [16-19]. The studies are summarized in Table 1.

Table 1. Summary of the NTCP model parameter sets used.

		Lung volume	MLD ^a Range (Gy)	Endpoint	Used on treatment type
<i>Seppenwoolde et al.</i>	LKB RS	paired paired	~2-35	RP ^c ≥ grade 2 SWOG ^d	Lung, LGL, Tang
<i>Gagliardi et al.</i>	RS	ipsilateral	unknown	RP ^c clinical	LGL, Tang
<i>Rancati et al.</i>	LKB	ipsilateral	2.5-18	RP ^c ≥ grade 1 modified CTC- NCIC ^e	LGL, Tang
	RS	ipsilateral			
De Jaeger et al. ^b	LKB	paired	~2-25	RP ^c ≥ grade 2 SWOG ^d	Lung

^a Paired lungs

^b Parameters for the octree/edge algorithm with equivalent-pathlength inhomogeneity-correction

^c Radiation Pneumonitis

^d SouthWest Oncology Group toxicity criteria

^e Common Toxicity Criteria modified by the National Cancer Institute of Canada

4.1.4 Method for adjusting model parameters

The method used for adjusting model parameters for a different DCA than the one used in the clinical study determining the model parameters is described in detail in [20]. This method was implemented by the author of this thesis in a MATLAB program. The concept of the method and the assumptions made are briefly described here, following the notation in [20].

All parameters studied were retrieved for a standard pencil beam algorithm. The aim was to find adjusted NTCP model parameters that in conjunction with a given dose calculation algorithm would yield the same NTCP value that the original parameters yield in conjunction with the standard pencil beam algorithm. The tissue-describing parameters n and s were kept constant, while D_{50} and m/γ were adjusted. The original model parameter set is denoted \mathbf{H}_0 and the parameter set to be used in conjunction with the new algorithms is denoted \mathbf{H} . The original NTCP value for the i :th patient is denoted $P_{NTCP}(i, \mathbf{H}_0)$, this is calculated based on the standard pencil beam algorithm. The NTCP value calculated based on the new algorithm is denoted $C_{NTCP}(i, \mathbf{H})$. For a certain parameter set \mathbf{H}_{min} the difference between P_{NTCP} and C_{NTCP} is minimized. \mathbf{H}_{min} was found with a least-squares fitting procedure. The $P_{NTCP}(i, \mathbf{H}_0)$ and $C_{NTCP}(i, \mathbf{H})$ were transformed by applying a logarithm twice:

$$\tilde{P}_{NTCP}(i, \mathbf{H}_0) = \log(-\log(P_{NTCP}))$$

$$\tilde{C}_{NTCP}(i, \mathbf{H}) = \log(-\log(C_{NTCP}))$$

The objective function to be minimized was as follows (the objective function is denoted $\chi^2(\mathbf{H})$ due to assumptions in the estimation of standard deviations of adjusted parameters):

$$\chi^2(\mathbf{H}) = \sum_{i=1}^N \frac{[\tilde{P}_{NTCP}(i, \mathbf{H}_0) - \tilde{C}_{NTCP}(i, \mathbf{H})]^2}{\tilde{\sigma}_i^2}$$

where N is number of patients and $\tilde{\sigma}_i$ are the theoretical standard deviations of the distribution of the difference $\tilde{P}_{NTCP}(i, \mathbf{H}_0) - \tilde{C}_{NTCP}(i, \mathbf{H})$.

During the fitting process $\tilde{\sigma}_i^2$ was set to unity. After the fit the standard deviations of the adjusted parameters were estimated from the residuals of the fit. The details of the equations can be found in [20]. The assumptions were:

- $\tilde{\sigma}_i^2$ was assumed to be the same for each data point/patient
- the difference $\tilde{P}_{NTCP} - \tilde{C}_{NTCP}$ was assumed to be normally distributed. Normal probability plots were used to check normality.
- The standard deviations of the parameter D50 was determined by keeping m/γ constant at the value from the least-squares fit and vice versa.

4.2 Treatment planning

The treatments in this study are all constructed according to current clinical practice. Since only 3D conformal treatments are included in this work the only time a beam limiting device is moving during irradiation is when dynamic wedges are used. All plans are originally planned in the Eclipse TPS (Varian medical systems) where the currently used dynamic wedges are called enhanced dynamic wedge (EDW).

4.2.1 Conventional lung treatments

The exact field angles for the lung cases vary from case to case. They are based on three beam directions — anterior, posterior, and from the ipsilateral side. All lung plans use a photon energy of 6 MV for all fields. The beam directions are optimized to restrict the dose to the spinal cord, the contralateral lung, and the heart. Additional beams from the contralateral side are added if needed. EDWs are used if needed. The prescribed dose is 35x2 Gy to the planning target volume (PTV). PTV is defined as the clinical target volume (CTV) with approximately 1 cm margin (depending on organ motion). CTV is defined as the gross tumor volume (GTV) with 1 cm margin (or smaller if bone or air is confining the volume).

4.2.2 Stereotactic lung treatments

The treatment planning is done with 5-7 static coplanar or non-coplanar beams. If a satisfactory dose distribution is obtained with a coplanar technique, this is preferred to non-coplanar techniques. The beams are spread in the largest possible angle. Opposed/overlapping beams on the skin is avoided. EDWs are used if needed. Prescribed dose is 3x15 Gy minimum dose to the PTV, centrally in PTV the dose can be up to 22 Gy per fraction. The PTV is defined as the clinical target volume (CTV = the solid tumor and diffuse growth at its borders) with a margin of 5 mm in transversal plane and 10 mm in the longitudinal direction. In case of large tumor movement the margin is extended to include all tumor positions by delineating CTV in all phases of a four-dimensional (4D) CT (many 3D CT sets are obtained, each corresponding to a

particular breathing phase). An internal target volume (ITV) is then defined which encompasses all the CTVs from the different 4D CT phases and PTV is constructed by adding a margin to ITV. The stereotactic treatment is only given to small tumors with maximal tumor diameter of 6 cm.

4.2.3 Tangential breast cancer treatments

The Tang plans include two main tangential 6MV photon beams toward the breast. Additional small field segments of 6 or 15MV are sometimes used from either direction to increase target-dose homogeneity. EDWs are used if needed, but EDWs are not allowed if the treatment is delivered during DIBH. The prescribed dose is 50 Gy. 95% of CTV should receive the prescribed dose and the minimum dose to PTV must be larger than 93% (46.5 Gy). CTV consists of the remaining breast tissue and PTV is defined as CTV with 5-10 mm margin. PTV is also defined by the anatomy, for example the skin and lung confines the extension of PTV.

4.2.4 Loco-regional breast cancer treatments

The LGL plans include 4-8 fields. Four main fields consisting of two tangential fields towards the breast and additional two photon beams toward the axilla region (anterior and posterior beams). Both 6 and 15 MV are used. The beam arrangement is illustrated on the front cover (right figure). EDWs are used if needed, but EDWs are not allowed if the treatment is delivered with gating. The prescribed dose is 50 Gy, 95% of CTV should receive the prescribed dose and the minimum dose to PTV must be larger than 93% (46.5Gy). CTV consists of the remaining breast tissue. PTV is defined to include CTV with 5-10 mm margin as well as the supraclavicular lymph nodes. PTV is also defined by the anatomy, for example the skin and lung confines the extension of PTV.

4.3 Verification and implementation of the Monte Carlo model

The EGSnrc research code is in this work used by simulating the accelerator head in BEAMnrc and then by simulating the transport of radiation in phantom and in the patient geometry in DOSXYZnrc.

The virtual accelerator is defined by assorting certain modules predefined in BEAMnrc. The modules, materials and dimensions are specified to resemble the real accelerator as described in technical specifications released for simulation purposes. A sketch of the 6 MV accelerator head simulated in this work is shown in Figure 4.

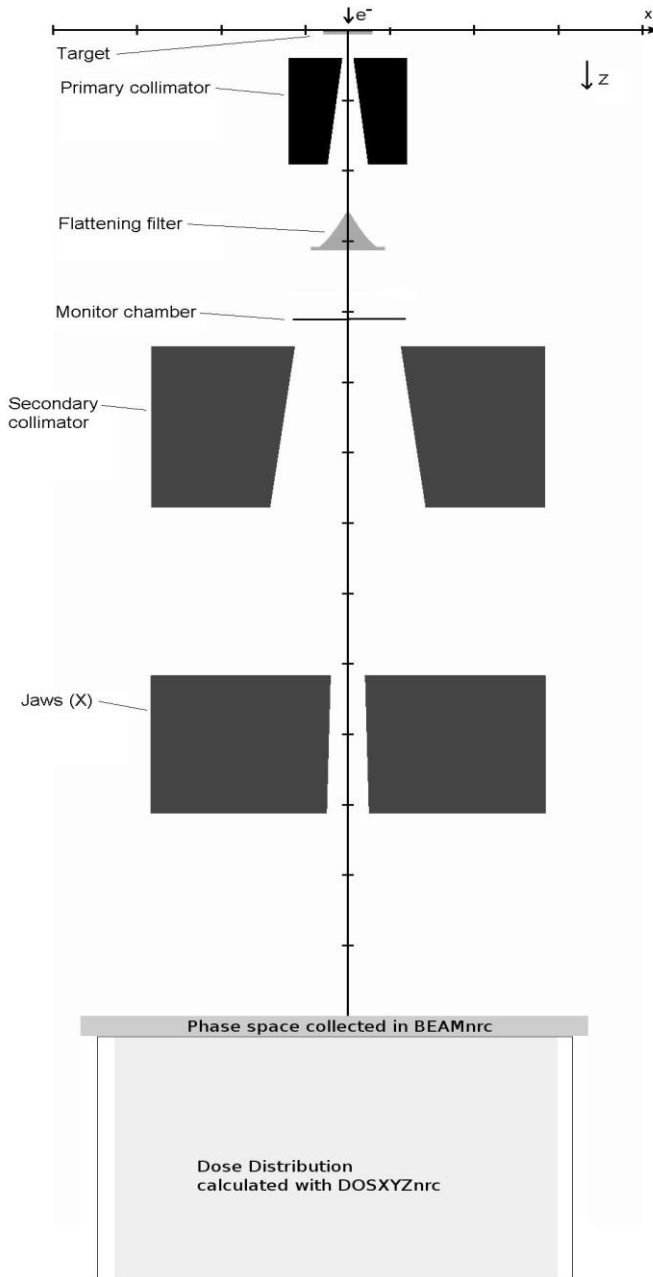


Figure 4. Sketch of the virtual accelerator defined in BEAMnrc.

Both 6MV and 15MV photon fields are calculated. This requires two separate MC models – one for the 6MV and one for the 15MV accelerator head. The work of adjusting basic parameters for the 6MV accelerator head was made by the author of this thesis and is reported in Appendix A (Report MFT-Radfys 2010:01). The Monte Carlo method was validated against measured data in water phantom (profiles, depth dose curves and output factors) for an extensive variety of field sizes (2x2 cm² – 40x40 cm²). Model parameters for the 15 MV accelerator head were adopted from [21, 22]. Additional work of validating the model (6 and 15 MV) for mlc and wedge fields was made in paper III. Both symmetric (not shown in Paper III) and asymmetric wedge fields were validated against measurements. The mlc model was designed according to technical specifications from the vendor and verified for static mlc fields (not shown in Paper III). The measurements were conducted with an ion chamber array (IC Profiler, Sun Nuclear Corporation).

Prior to using the MC model for a specific treatment type, example fields with characteristics corresponding to the treatment type are applied on a water phantom and calculated with the MC model and compared to measurement and/or the clinical DCA. This is made to elucidate the accuracy of the model in homogeneous geometry. The water phantom depth dose curve of a small field of a stereotactic lung treatment as calculated by MC and clinical DCAs as well as measured with a pin-point ionization chamber is shown in Figure 5. The difference between the methods in dose maximum is up to 1.6 %. The water phantom lateral profile for a double asymmetric rectangular field including wedge (15 degrees) is shown in Figure 6, the MC calculation is compared to a relative measurement with ion chamber array (IC Profiler, Sun Nuclear Corporation, 251 ion chambers with 2.9 mm width and 5 mm spacing) as well as absolute measurement with ionization chamber CC13 (IBA Dosimetry, Germany).

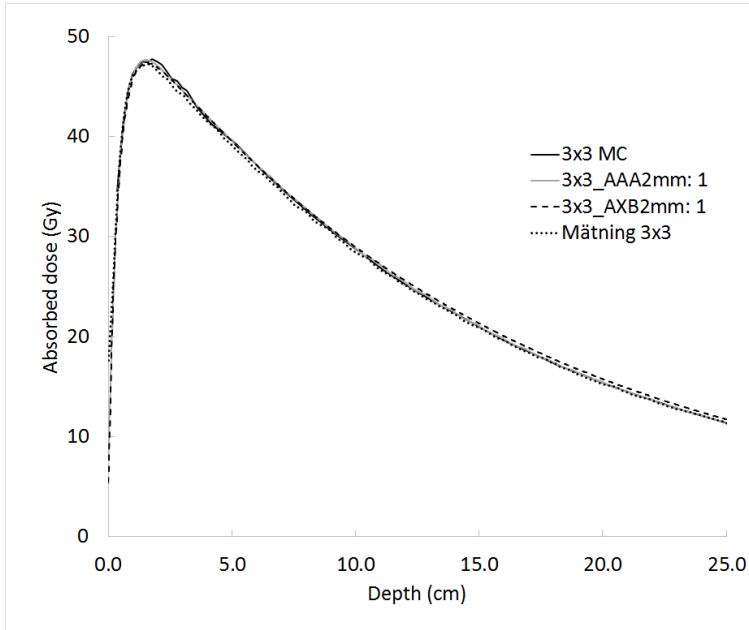


Figure 5. Water phantom depth dose curve of 3x3 cm³ field. Calculated with MC model, AAA and AXB as well as measured with pin-point ionization chamber.

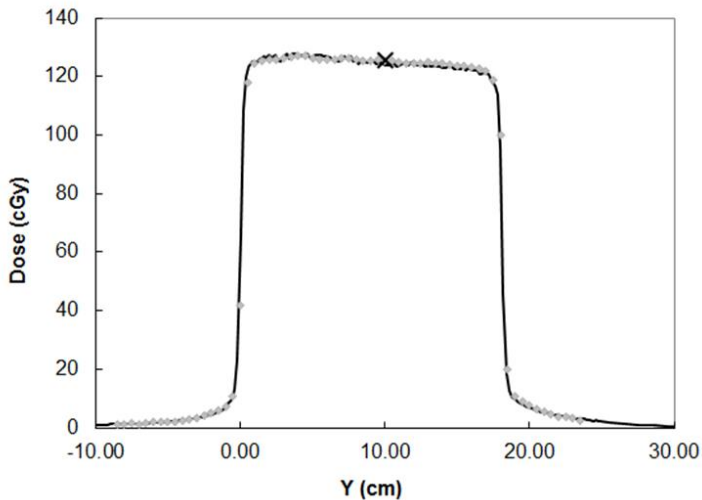


Figure 6. Water phantom lateral profile for tangential field in LGL breast treatment. 15 degree wedge, double asymmetric. MC calculation (solid black line) compared with ion chamber array measurement (grey dots) which is a relative measurement normalized to the absolute ion chamber measurement (cross).

The model transport parameters used during calculation of clinical treatment plans are shown in Figure 7-8.

```

=====
                        Electron/Photon transport parameter
=====

Photon cross sections                sl
Compton cross sections              default
Photon transport cutoff(MeV)        0.1000E-01
Pair angular sampling               KM
Pair cross sections                 BH
Triplet production                  Off
Bound Compton scattering            ON
Radiative Compton corrections       Off
Rayleigh scattering                 Off
Atomic relaxattions                 Off
Photoelectron angular sampling      ON

Electron transport cutoff(MeV)      0.7000
Bremsstrahlung cross sections       NIST
Bremsstrahlung angular sampling     KM
Spin effects                         On
Electron Impact Ionization         Off
Maxium electron step in cm (SMAX)   5.000
Maximum fractional energy loss/step (ESTEPE) 0.2500
Maximum 1st elastic moment/step (XIMAX) 0.5000
Boundary crossing algorithm         EXACT
Skin-depth for boundary crossing (MFP) 3.000
Electron-step algorithm             PRESTA-II

```

Figure 7. *EGSnrc* transport parameters used in the *BEAMnrc* simulations.

```

=====
                        Electron/Photon transport parameter
=====

Photon cross sections                xcom
Compton cross sections              default
Photon transport cutoff(MeV)        0.1000E-01
Pair angular sampling               KM
Pair cross sections                 BH
Triplet production                  Off
Bound Compton scattering            ON
Radiative Compton corrections       Off
Rayleigh scattering                 Off
Atomic relaxattions                 ON
Photoelectron angular sampling      ON

Electron transport cutoff(MeV)      0.5210
Bremsstrahlung cross sections       NIST
Bremsstrahlung angular sampling     KM
Spin effects                         On
Electron Impact Ionization         tk
Maxium electron step in cm (SMAX)   0.1000E+11
Maximum fractional energy loss/step (ESTEPE) 0.0400
Maximum 1st elastic moment/step (XIMAX) 0.5000
Boundary crossing algorithm         EXACT
Skin-depth for boundary crossing (MFP) 3.000
Electron-step algorithm             PRESTA-II

```

Figure 8. *EGSnrc* transport parameters used in the *DOSXYZnrc* simulations.

For the BEAMnrc simulations (phase space collection) AE was chosen to be 0.700MeV with ECUT=AE and AP was chosen to be 0.01MeV with PCUT=AP. For the DOSXYZnrc simulations (dose calculation) AE was chosen to be 0.521 MeV with ECUT=AE and AP was chosen to be 0.01 MeV with PCUT=AP. This is following the recommendations for therapy beam dose calculations in the BEAMnrc user's manual [4] and is coherent with or more detailed than other published similar work [23-26].

The settings above implies that electrons in the phantom/patient are followed down to total energy of 0.521MeV. According to recommendations in BEAMnrc user's manual [4] "ECUT should be chosen so that the electron's range at ECUT is less than about 1/3 of the smallest dimension in a dose scoring region". To follow this recommendation the density in the CT image or the voxel dimensions of the calculation must be kept above certain values. For example for the MC model to accurately simulate the dose distribution in air (0.001205g/cm^3) the smallest voxel dimension allowed is 7 mm. For a 2 mm voxel dimension (common clinical dose grid) the lowest density accurately simulated is 0.0038 g/cm^3 (using the CSDA range for water).

Probability distributions for the chosen AE and AP are constructed in the PEGS software included in the EGSnrc code package. Nine tissue types are defined, namely; air, lung, adipose, muscle skeletal and five bone tissues obtained by interpolation of bone mass density and composition between spongiosa skeletal and cortical bone. The elemental composition of the materials included are calculated according to the formalism in [27] and [28].

4.3.1 Absolute dose calibration

The formalism for conversion of the MC dose in Gy per primary history to the dose in Gy for a certain number of monitor units MU (denoted further in the text as absolute dose) is based on simulations of the calibration geometry and corrections for the effect of backscattered radiation to the monitor chamber, as described in [29]. The accelerators in our hospital are calibrated in water at 10 cm depth at source-to-surface distance (SSD) 90 cm for a $10\text{ cm} \times 10\text{ cm}$ field. The MC model is solely used to report dose to medium, no conversion to dose to water is made.

This empirical approach for absolute calibration is commonly used in the context of Monte Carlo calculation of radiation therapy beams. The relative dose (normalized to number of primary particles) from the MC simulations is related to the relative dose in the calibration point. Furthermore, the number of MUs for each field is related to the number of MUs per Gy in the calibration

point. However, the MUs are measured with the monitor chamber that is placed above the jaws and therefore a small fraction of the signal from the monitor chamber is from radiation that has interacted in the jaws and are backscattered towards the monitor chamber. The amount of backscattered radiation to the monitor chamber varies with field size since the larger fields the smaller parts of the jaws are in the field. The monitor chamber response is not modelled in the MC simulation and therefore the backscatter must be corrected for without knowing the actual amount of charge in the monitor chamber produced by backscattered radiation. For small fields the charge representing one MU is reached faster than expected. This means in turn that 1 MU is not ‘worth’ as much dose below the accelerator head as expected. The ratio between the measured absolute dose and the simulated absolute dose (not backscatter corrected) for this small field size gives us a clue about how the number of MUs for a given field should be adjusted to correspond to the number of MUs measured with a monitor chamber not subject to backscattered radiation at all, i.e. the number of MUs suitable for input to the MC model. The backscatter correction is further discussed below.

4.3.2 Backscatter correction

A backscatter correction factor (BSCF) is used that relates the amount of backscattered dose to the monitor chamber for a certain field to the calibration field size. A linear dependence is considered between the backscattered dose to the monitor chamber and the field size as suggested by Verhaegen et al.[30] It is assumed that the effect of the components located below the upper Y jaw, namely the lower X jaw and the MLC, is negligible. This assumption is consistent with the results reported on the dominating effect of the upper Y jaw on the backscatter compared to that of the lower X jaw.[30, 31] The BSCF is therefore only dependent on the field length in the Y direction (FSy) and is given by:

$$BSCF(FSy) = \frac{a+b*10}{a+b*FSy} \quad (1)$$

New parameter values of a and b in Equation 1, specific for our accelerators, are obtained, namely, $a = 1.034$ (1.028) and $b = -0.00085$ (-0.00070) for 6 (15) MV, respectively. The field sizes included in this optimization procedure are 4x4 cm, 20x20 cm and 40x40 cm symmetrical square fields, as well as 4x20 cm and 20x4 cm symmetrical rectangular fields. The process of retrieving the parameters including minimizing the difference between simulated and measured output factors.

This method of correcting for backscatter is experimental and is not based on any simulation of the monitor chamber. As shown in Figure 9 after backscatter correction the difference between measured and simulated output factors is less than 1% for the 6MV accelerator head model and less than 0.5% for the 15 MV accelerator head, for the investigated field sizes.

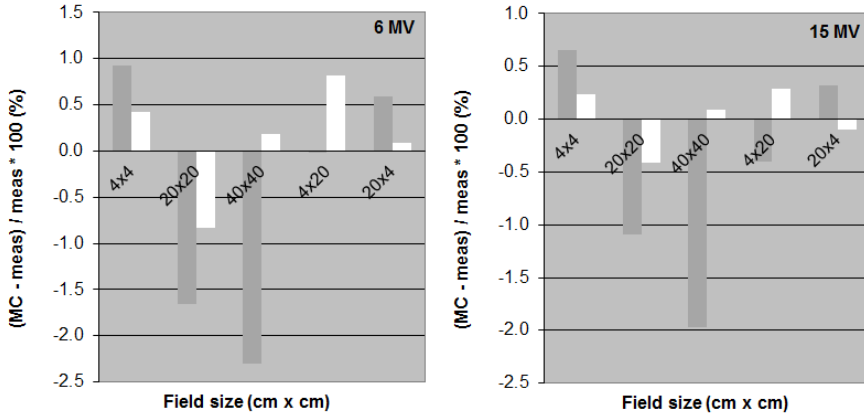


Figure 9. Differences between MC-calculated and measured output factors for both non-corrected MC-calculated values (gray) and backscatter corrected MC-calculated values (white).

4.3.3 Backscatter correction for fields with wedge

For wedges, the backscatter correction is applied on the differential segmented treatment table; $STT_{diff,i} = STT_i - STT_{i-1}$, where i is an index indicating the row of the STT. To facilitate the writing in Equation 2, it is defined that $STT_0 = 0$. The row-index, i , varies from 1 to maximum number of rows in the STT. Each row of the backscatter corrected STT, STT_{bscorr} , is thereby given by:

$$STT_{bscorr,i} = \sum_1^i ((STT_i - STT_{i-1}) * BSCF(FSy_i)) \quad (2)$$

In this way, the backscatter effect is taken into account when simulating the jaw movement. The backscatter corrected STT is normalized to the number of cumulative monitor units, delivered at the last position of the jaw, before it is used in the EGSnrc/BEAMnrc for producing a phase space. The number of MUs of a wedged field is in the treatment plan equal to the cumulative number of MUs delivered at the last position of the jaw. Therefore, a backscatter correction factor, (denoted global in the text), is needed also for wedged fields - so that the total number of MUs can be corrected in a similar way as for to

the non-wedge fields. This global backscatter correction factor used for wedge fields in the conversion of the MC dose to absolute dose is obtained by the ratio between the cumulative number of MUs for backscatter corrected and non-corrected STT, respectively. A backscatter corrected STT is compared to the original STT in Figure 2 in Section 3.1.1.

4.3.4 Study-specific settings

The MC model is used in three out of four papers to recalculate treatment plans originally planned with one of the clinical DCAs. During recalculation the same number of monitor units, MLC/collimator positions, EDWs and beam arrangement are used as in the original plan. The number of histories required in the MC calculations to achieve acceptable statistical noise was determined by test calculations for each treatment type. The number of histories was increased until there was no visual effect on the DVH.

Paper II

In this study the MC calculation was made with dose scoring in cubical voxels with 2 mm sides. The results are compared to the AXB algorithm. In the AXB algorithm materials are mixed when the mass density is in a certain interval, i.e. the border between for instance lung/adipose tissues is not sharp but in a given mass density interval both lung and adipose tissue are present. For MC simulations a distinct border between different tissue types is used. To match the AXB calculations as good as possible, this border was chosen at the mean of the mass density interval used for mixed materials in AXB. The 3D dose distributions are analyzed in CERR (Matlab based computational environment for radiotherapy research).

Paper III

In this paper the MC model is used to investigate jaw misalignment of up to a few millimeters. Therefore, the resolution is improved compared to normal clinical dose grids and the MC calculation is made with dose scoring in cubical voxels with 1.5 mm sides. Nine tissues are defined in the tissue segmentation process, similar to how it is done in Paper II. However, the MC results are not explicitly compared to a clinical DCA in this study why the tissue types are not chosen according to the tissue segmentation table from AXB (as in Paper II and IV). Instead, the density intervals for each material are somewhat arbitrarily chosen, but they are defined to match with the tissue inserts used during CT calibration. The densities are also compared to the material density of each tissue type as reported in ICRU Report 44 [32]. The 3D dose distributions are imported as DICOM dose files via Vega library[33] in the Eclipse v. 11.0 (Varian Medical Systems) TPS for viewing and DVH analysis.

Paper IV

In this paper the MC calculations were made with dose scoring in voxels with dimension of 2 mm in the transversal plane and 3 mm between CT-slices. In this study breast treatment plans are applied on patient CT scans with low lung density due to DIBH gating technique. For the two low-density cases identified, the amount of voxels with density less than 0.0041 g/cm^3 in the lung tissue was quantified. Below this density the 2 mm voxel dimension is too small for the chosen ECUT as recommended by Walters et al. [4]. The tissue segmentation is in this study identical to Paper II since MC is compared to AXB. The 3D dose distributions are analyzed in CERR (Matlab based computational environment for radiotherapy research).

4.4 Dose calculation with clinical dose calculation algorithms

The configuration of the DCAs are identical to the clinical implementation.

The physical material table used for all AXB calculations are presented in Table 2.

Table 2. Physical material table used in the AXB calculations

Material name	Minimum Density (g/cm^3)	Maxium Density (g/cm^3)
Air	0.0000	0.0204
Lung	0.0110	0.6242
Adipose	0.5539	1.0010
Muscle	0.9693	1.0931
Cartilage	1.0556	1.6000
Bone	1.1000	3.000

4.4.1 Study-specific settings

Paper I

In paper I the studied dose calculation algorithms are Pencil Beam (PB) and Collapsed Cone (CC) both in Oncentra v4.0 TPS (Nucletron/Elekta) as well as Pencil Beam Convolution (PBC) with modified Batho inhomogeneity correction and Analytical Anisotropic Algorithm (AAA) both in Eclipse v8.9 TPS (Varian Medical Systems). The calculation grid is 2.5 mm with a 5 mm slice separation of the CT series. The plans are originally calculated with PBC. The plans are recalculated with AAA and also exported to Oncentra where they are recalculated with PB and CC. The MUs obtained in the PBC calculation are used in all recalculations.

Paper II

The original treatment plans were planned based on AAA in Eclipse (version 11.0.31, Varian Medical Systems). All plans were recalculated with AXB (Eclipse, version 11.0.31). The same number of MUs, MLC/collimator positions, EDWs and beam arrangement were used for the recalculated treatment plans. A clinically realistic dose grid of 2 mm was used for all dose calculations, including 2 mm slice separation of the CT series.

Paper III

Test calculations are performed with the dose calculation algorithm currently used at our hospital for this type of treatment, namely the analytical anisotropic algorithm (AAA) version 10.0.28 implemented in Eclipse (Varian Medical Systems). A dose grid of 1.5 mm is used since the investigated issue involves misalignment of jaws of a few millimeters.

Paper IV

All treatment plans were originally planned with AAA and they were recalculated with AXB using the same number of MUs, MLC/collimator positions, EDWs and beam arrangement. A clinically realistic dose grid of 2 mm in the transversal plane and 3 mm between CT-slices were used for all dose calculations. Throughout the study AAA and AXB version 13.6.23 was used.

4.5 Study designs

Paper I

10 tangential breast (Tang), 10 loco-regional breast (LGL) and 10 lung cancer treatment plans are included in the study (see detailed description of the types of treatments in section 3.3). The plans are originally calculated with PBC in Eclipse. The plans are recalculated with AAA and also exported to Oncentra where they are recalculated with PB and CC. The MUs obtained in the PBC calculation are used in all recalculations. Lung DVHs are compiled in their respective TPS and used to estimate NTCP. GTV is subtracted from the lung DVH in the case of lung cancer. The DVHs are retrieved for paired lungs and in the case of breast cancer treatment also for the ipsilateral lung.

The mean lung dose (MLD), NTCP and equivalent uniform dose (EUD) are calculated for all DVHs and for all four calculation algorithms. NTCP is calculated using the LKB-model[11, 12] with the DVH reduces to EUD, following Niemerko[13] and the relative seriality (RS) model[14]. The model parameters derived for a correction-based pencil beam dose calculation algorithm are taken from four different publications describing studies that consider different grades of pneumonitis.

The original parameters were assumed to be valid for PB. The impact of choice of DCA on the NTCP values is illustrated by plotting the reference NTCP value against its different EUDs as calculated by the different DCAs. Furthermore, new NTCP model parameters for PBC, AAA, and CC were derived following the method suggested by Brink et al. [20], this method is discussed in section 3.2.1. The impact of choice of DCA on the NTCP is also compared to the statistical uncertainties in the model parameters as reported from the clinical trials.

Paper II

20 SBRT lung treatments (detailed description of the treatment type in section 3.3) are included in the study. The original treatment plans were based on AAA and were recalculated with AXB as well as with full MC. The MUs obtained in the AAA calculation were used in all recalculations.

The dose calculation methods were compared for all treatment plans by visual analysis of total DVHs for GTV and PTV and the differences were quantified by $D_{5\%}$, $D_{50\%}$ and $D_{98\%}$. $PTV-V_{100\%}$ was also retrieved to investigate the feasibility of a 100% isodose prescription to PTV.

For each case the patient/plan characteristics listed below were recorded. Those plan/patient characteristics were recorded to investigate if they can be used to predict the change in calculated target dose coverage when changing dose calculation method from AAA to AXB.

- GTV volume
- PTV volume
- Volume of lung tissue part of PTV
- Distance from GTV edge to nearest lung edge
- Average of lung density in three points two centimeters from PTV
- Proportion of PTV edge in lung.

For the plans with largest change in PTV- $V_{100\%}$, when the plan was recalculated with AXB, a re-planning was made based on AXB's dose calculation. During re-planning with AXB, PTV- $V_{100\%}$ was kept within 0.5% of the value of the original AAA plan. The treatment planning criteria for this treatment type are described in section 3.3, for the re-planned cases additional parameters were recorder apart from what is determined in the treatment planning criteria, namely mean dose to GTV and volume encompassed by the 100% isodose.

Paper III

In this paper one LGL breast treatment is considered. Dose distributions are obtained for the following five cases of junction between the cranial fields and the tangential fields: 2 and 1 mm gap, perfect match, as well as 2 and 3 mm overlap.

DVH parameters are evaluated for PTV, Body and Body minus PTV. $V_{105\%}$, $V_{110\%}$ and $V_{120\%}$ are chosen to illustrate the increased volumes of hot-spots, both inside and outside of PTV. $V_{95\%}$ for PTV and Body minus PTV is used to described the potential lack of coverage in case of gap between fields as well as to describe the increased volume of normal tissue receiving the same dose level as target in case of field overlap. Furthermore, $D_{98\%}$ and $D_{2\%}$ (near minimum and near maximum dose according to ICRU report 83[34]) and mean dose to PTV is monitored. The increased dose in the junction region in case of overlap is further quantified by the maximum width in the craniocaudal direction of the volume covered by 110% isodose. Since the jaw position uncertainty is only a few millimeters this measure becomes important to be able to discuss the results considering variation in the setup for the different treatment fractions.

Paper IV

14 patients with two parallel treatment plans each – one on FB and one on DIBH CT-scans were included in the first part of the study. 5 of those has undergone LGL breast treatment and 9 had undergone tangential treatment. The densities of the DIBH scans for the 14 patients were compared to the corresponding densities measured in the underlying CT-scans for all breast cancer patients treated with DIBH technique during one year. This large population consisted of 157 patients. In this larger group, the Tang case and the LGL case with the lowest lung density were identified and included in the study. Those two additional patients had only one CT-scan, i.e. DIBH. By collecting the patient material for the study as described above it is seen that low lung-densities are investigated. Furthermore, knowledge of the general density distribution of the studied patient type is useful. This enables generalization of the results from the studied group of patients to the treatment type as a whole.

All treatment plans were originally planned with AAA and recalculated with AXB. The two low lung density cases were also recalculated with MC. The MUs obtained for the AAA plans were used in all recalculations. The performance in lung tissue of the different dose calculation methods were compared for all treatment plans by analysis of ipsilateral lung DVH parameters $V_{5\text{Gy}}$, $V_{10\text{Gy}}$, $V_{20\text{Gy}}$ and $V_{40\text{Gy}}$. The change in parameters due to a change in DCA from AAA to AXB was plotted against lung density to study the impact of lung density on the differences of calculated dose to lung tissue between the algorithms.

The lung density was measured for all patients so that for each CT-scan the lung density was determined as the average lung density in a two dimensional region of interest (ROI) in transversal plane (x/y-plan in the Eclipse coordinate system). The ROI was placed within the 15% isodose line and the size was at least $2 \times 2 \text{ cm}^2$. A detailed description of the location of the planes where the lung density was measured can be found in Paper IV. The lung density used to study the impact of lung density on differences between AAA and AXB was measured in the isocenter plane in both the LGL and the Tang plans.

5 RESULTS

Paper I

The estimated dose distribution and the corresponding DVH both change when the treatment plans are recalculated with a different dose calculation algorithm. A change from PBC to AAA causes an average relative decrease in MLD (1 SD) of 5% ($\pm 2\%$), 4% ($\pm 2\%$), and 4% ($\pm 4\%$) for the Lung, LGL, and Tang plans, respectively. The corresponding results for a PB-to-CC change are 8% ($\pm 2\%$), 9% ($\pm 1\%$), and 10% ($\pm 3\%$). The maximum absolute difference between NTCP values (without adjusting the model parameters) for the two types of algorithms is seen for LGL plans with a 6% (10%) difference for Eclipse (Oncentra). The absolute difference naturally increases for NTCP values closer to the steepest point of the NTCP curve.

Examples of how the NTCP curves are changed by a change of dose calculation algorithm from PB (reference) to PBC, AAA and CC are shown in Figure 10. PB-based NTCP values are plotted against the different values of EUD for the different dose calculation algorithms. Hence, the diagrams visualize what parameter shift that would be necessary to yield the same NTCP value from a PBC/AAA/CC-calculated DVH as for the reference PB-calculated DVH. Figure 10 b include all studied treatment plans. Figure 10 a and c include only breast plans since the NTCP model parameters were based on dose data for ipsilateral lung in these cases. The differences in NTCP values in the figures are due to differences in endpoint studied (notice the differences in y-scale in figure 10). It is clear that the absolute differences in NTCP values in the lower end of the curve are very small. Seppenwoolde et al.[16] and Rancati et al.[18] report model parameters both for the RS and LKB-model. The two models show analogous result, only one model is shown in Figure 10. The two Pencil Beam algorithms PB and PBC are similar while AAA and CC shows a larger change in NTCP value where CC shows the largest change (see Figure 10).

In Figure 10 the uncertainty of the original NTCP model parameters is also presented, the gray area symbolizes the confidence interval of the NTCP value for each EUD. In Figure 10 a-b the differences due to different algorithms are relatively small compared to the confidence interval while in Figure 10 c these differences are comparable in size to the confidence interval. The reported confidence intervals of NTCP model parameters differ between different studies. The smaller confidence interval in Figure 10 c can be due to that studies on a mild and more frequent endpoint [18] will have high prevalence

of the endpoint and could thereby result in small confidence intervals for the model parameters.

New algorithm-specific model parameters were derived and are presented in Paper I. D_{50} is shifted up to 4.5 Gy to make the PB parameters valid for PBC, AAA and CC.

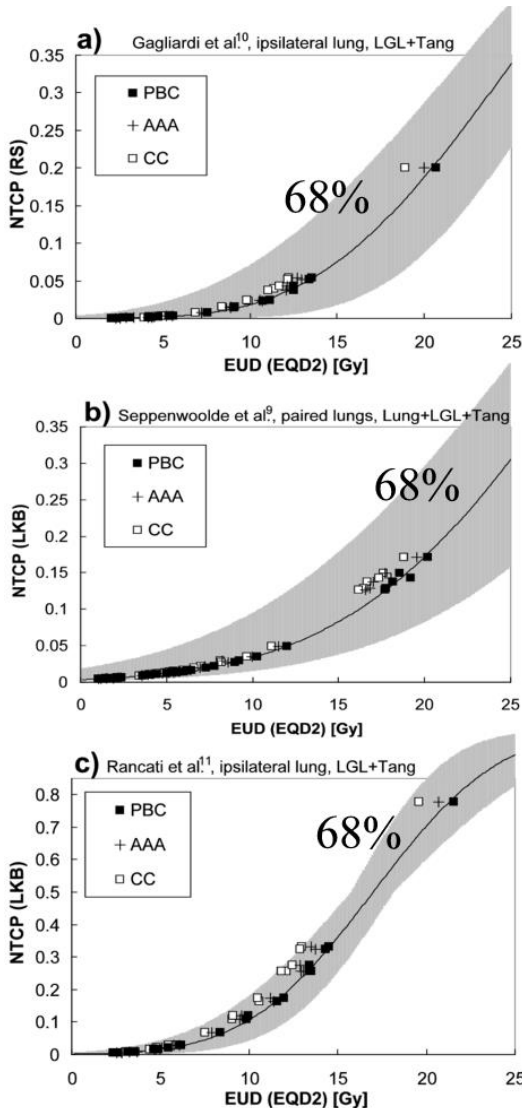


Figure 10. *NTCP values plotted against EUD for different algorithms. The line shows the NTCP curve for the PB calculation for the model parameter set investigated in each respective diagram. a) Parameters from Gagliardi et al.[17] (RS), ipsilateral lung, LGL+Tang plans. b) Parameters from Seppenwoolde et al.[16] (LKB), paired lungs Lung+LGL+Tang plans. c) Parameters from Rancati et al[18] (LKB), ipsilateral lung, LGL+Tang plans. Grey area represents confidence interval with level of confidence given in each diagram. Note that subfigure c) has a y-axis scale different from the others due to a much lower endpoint studied.*

Paper II

The DVHs for the 20 patients planned with AAA and recalculated with AXB (dose to water and dose to medium) and MC are shown for PTV in Figure 11. The two AXB calculations - dose to water and dose to medium are practically seen overlapping.

The DVHs illustrate how AAA overestimates target coverage compared to AXB. For PTV the $D_{98\%}/D_{50\%}$ value differ up to 10%/8% between AAA and AXB (AAA overestimating compared to AXB). When comparing AXB and MC $D_{98\%}$ is consistently overestimated with up to 6% by AXB compared to MC. The PTV- $V_{100\%}$ is consistently higher for AAA compared to AXB, the difference is up to 6%. The corresponding difference for an AXB-MC comparison are up to 7% for PTV- $V_{100\%}$ (AXB overestimating compared to MC).

For GTV (DVH not shown) the difference between $D_{98\%}$ calculated with AAA and AXB, respectively, is up to 7% overestimation by AAA compared to AXB, for $D_{50\%}/D_{5\%}$ the difference is $\pm 3\%/\pm 4\%$. MC and AXB predict similar $D_{98\%}/D_{50\%}/D_{5\%}$ for GTV, the difference is within $\pm 3\%/\pm 2\%/\pm 2.5\%$.

The five plans with largest differences in PTV- $V_{100\%}$ between AAA and AXB that were re-planned had the following plan numbers: 4, 13, 17, 18 and 20. Visual examination of the DVHs in Figure 11 reveals large differences between AAA and AXB for plan numbers 11, 12 and 14. This is seen as a shift of the DVH curve and is mainly expressed in the PTV- $D_{50\%}$ parameter. However, PTV- $V_{100\%}$ is related to the treatment planning criteria while PTV- $D_{50\%}$ is not, and therefore, strictly according to the treatment planning protocol, those plans are not largely affected by changing from AAA to AXB since the differences between the AAA and AXB DVHs are only present above 45 Gy (100%) in the DVH.

The re-planning caused a small change in mean dose to GTV and in the doses to risk organs. The volume encompassed by the 100% isodose and the 100% isodose volume ratios (AXB-replanned/AXB-recalculated) are presented in Table 3. The 100% isodose volume increased 7%-23% for the five replanned cases.

Table 3. The volume encompassed by the 100% isodose. Values for the recalculated and replanned AXB-cases shown. Ratio between 100% isodose volumes in the last column.

Plan ID	100% isodose volume (cm3)		Ratio
	AXB	AXBreplan	
04	30.61	36.51	1.19
13	87.01	96.8	1.11
17	54.48	66.75	1.23
18	85.71	94.06	1.10
20	13.37	14.36	1.07

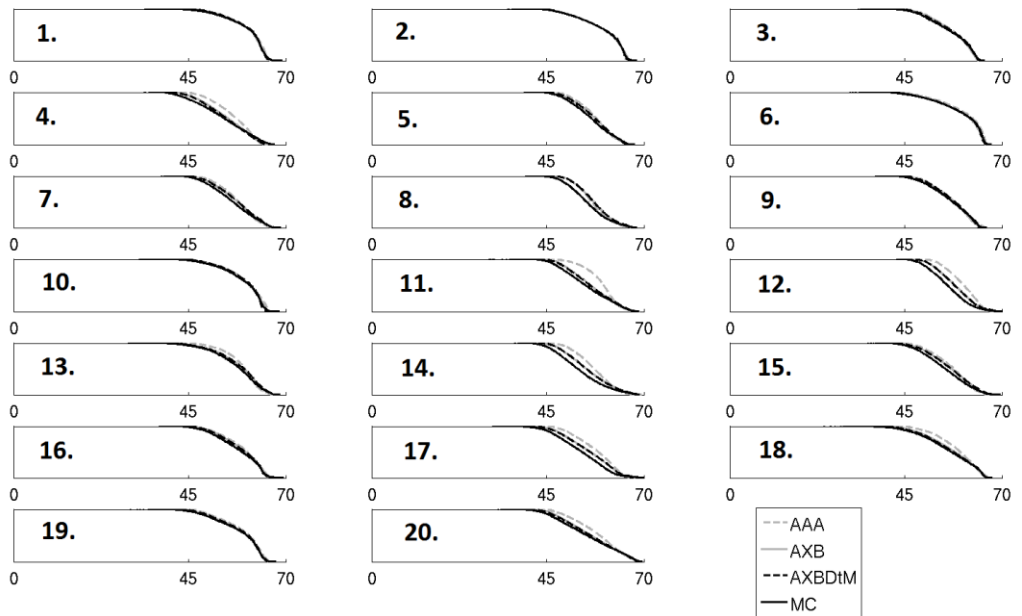


Figure 11. DVHs for PTV based on AAA, AXB (dose to water), AXBDtM (dose to medium) and MC calculations.

Paper III

Plan evaluation parameters for PTV, body, and PTV-body are listed in Table 4. PTV is 507.6 cm³. When gap is present, the largest concern is to evaluate possible cold spots in the target volume. The D_{98%} (near minimum dose) in the PTV is reduced from 91% for perfectly aligned fields to 88% and 85% for a 1 mm and 2 mm gap, respectively (see Table 4). The target coverage expressed as the PTV volume covered by the 95% isodose, V_{95%}, is reduced from 94% to 91% and 90% respectively for a 1 and 2 mm gap. Thus, for 95% isodose coverage there is not a large distinction between gaps of 1 or 2 mm. When overlap is present, the PTV volume covered by 105% and 110% isodoses is increased. A volume covered by 120% isodose appears as well. However, when comparing the two cases of overlap, the largest effect is seen for D_{2%} (near maximum dose). This is to be expected, since the effect of overlapping fields is restricted to a small part of the dose distribution.

When overlap is present, even the volume outside target (Body – PTV in Table 4) covered by 110% isodose increases, from 12 cm³ to 31 cm³ and 37 cm³ for 2 and 3 mm overlap. Also, a region of 15 cm³ confined by 120% isodose appears for 2 mm overlap and increases to 25 cm³ for 3 mm overlap. The region exposed by 110% dose or more does not include lung tissue, but other organs at risk, such as the plexus brachialis, may be present in this region.

To further quantify the increased dose in the junction region in the case of field overlaps, the maximum width in craniocaudal direction of the volume covered by 110% isodose is estimated. The values obtained are 1.5 cm and 2.1 cm for 2 mm overlap and 3 mm overlap, respectively. The width of the volume covered by 120% isodose is 0.4 cm and 0.6 cm for 2 mm and 3 mm overlap, respectively. 110% and 120% isodoses are not observed in the case of perfect alignment of jaws.

The changes in mean dose, V_{20Gy} and D_{2%} for the ipsilateral lung are small due to a large organ volume.

Table 4. Plan evaluation measures for PTV, body and body-PTV.

		Jaws 2 mm apart	Jaws 1 mm apart	Jaws perfectly aligned	Fields overlapping 2 mm	Fields overlapping 3 mm
<i>PTV</i>	$V_{95\%}$ (%)	90	91	94	95	95
	$V_{105\%}$ (%)	16	16	17	22	23
	$V_{110\%}$ (%)	0.2	0.3	0.4	3.0	4.0
	$V_{120\%}$ (%)	0.0	0.0	0.0	1.4	2.1
	$D_{2\%}$ (%)	108	108	109	113	121
	$D_{98\%}$ (%)	85	88	91	92	92
	D_{mean} (%)	101	101	101	102	103
<i>Body</i>	$V_{105\%}$ (cm ³)	207	216	224	268	283
	$V_{110\%}$ (cm ³)	13	13	15	47	59
	$V_{120\%}$ (cm ³)	0	0	0	15	25
<i>Body-PTV</i>	$V_{95\%}$ (cm ³)	503	510	526	547	558
	$V_{105\%}$ (cm ³)	126	129	133	153	164
	$V_{110\%}$ (cm ³)	11	11	12	31	37
	$V_{120\%}$ (cm ³)	0	0	0	5	14

Examples of interpretation: $V_{95\%}$ (%) = 90 means that 90% of the organ volume received 95% of the prescribed dose or more. $D_{2\%}$ (%) = 108 means that 2% of the organ volume received 108% of prescribed dose or more.

Paper IV

The differences between calculation methods in the values of V_{5Gy} , V_{10Gy} , V_{20Gy} and V_{40Gy} will be expressed in percentage points. The symbol % is used to indicate the unit (other common abbreviations are pp or p.p.).

The differences in the ipsilateral lung DVH parameters between AAA and AXB is illustrated in Figure 12. It is seen that none of the parameters V_{5Gy} , V_{10Gy} , V_{20Gy} and V_{40Gy} differ more than 3.1%. The smallest differences are seen for the parameter V_{20Gy} which differ less than 1% for all plans regardless of FB/DIBH or Tang/LGL. For the tangential treatment plans, decreased lung density in the DIBH CT-scan synchronize with larger differences between AAA and AXB for the DVH parameters V_{10Gy} , V_{20Gy} and V_{40Gy} as compared to the differences between AAA and AXB for the FB CT-scans. For the LGL plans the same trend is not visible.

The lung densities in the DIBH CT scans for the patient group with both FB and DIBH CT scans included in this study are distributed between medium to high density according to the density evaluation of a larger population (157 plans). The comparison of the densities of the larger and smaller group is shown in Figure 13.

The DVHs for the two low lung-density cases calculated with AAA, AXB and MC is shown in Figure 14. For those cases the differences in lung DVH parameters between AAA and AXB is larger than for the group of 14 patients included in the first part of the study. The largest differences are seen for V_{10Gy} and V_{40Gy} . For the LGL case AAA calculated 5% higher (lower) value of V_{10Gy} (V_{40Gy}) compared to AXB. For the tangential case AAA calculated 4% higher (lower) value of V_{10Gy} (V_{40Gy}) compared to AXB.

In Figure 14 it is seen that AXB comply substantially better with MC than AAA does. The compliance of the AXB and MC calculations is reassuring. The two methods both estimate a non-flat DVH and the difference between AXB and MC is less than 1% for all DVH parameters except $V_{5\%}$.

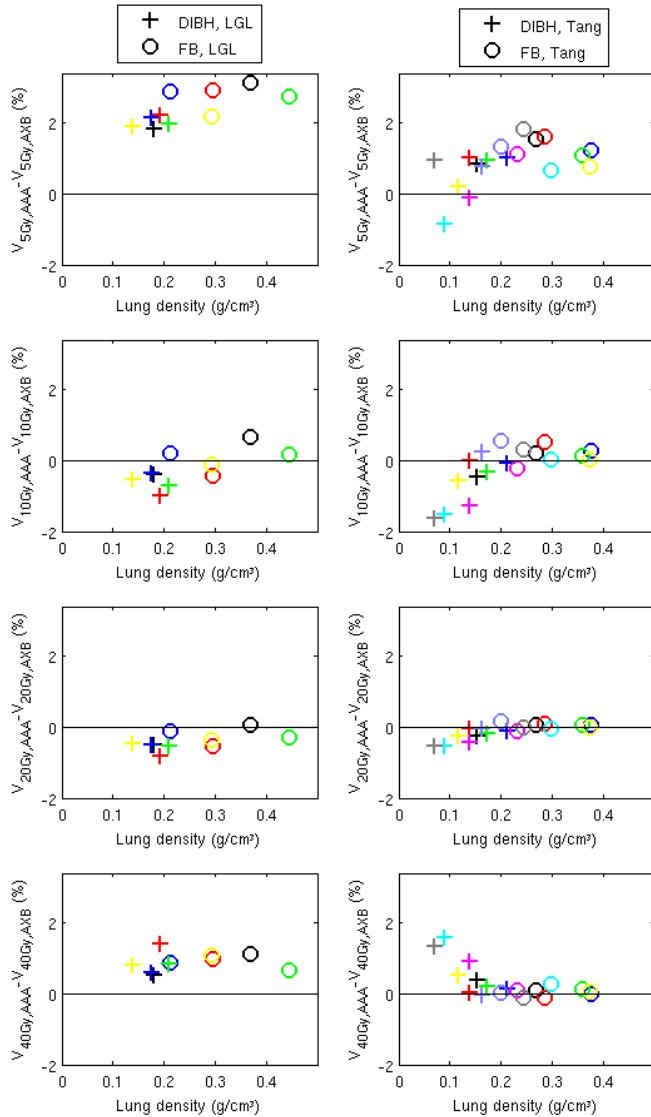


Figure 12. Difference between $V_{5Gy}/V_{10Gy}/V_{20Gy}/V_{40Gy}$ for ipsilateral lung calculated with AAA and AXB. Left: 5 FB (O) and 5 DIBH (+) loco-regional treatment plans. Right: 9 FB (O) and 9 DIBH (+) tangential (right) treatment plans. Each patient has a specific color indicating which O and + that belongs to that patient (each patient has two CT scans – one FB and one DIBH). Lung density in isocenter plane on the x-axis.

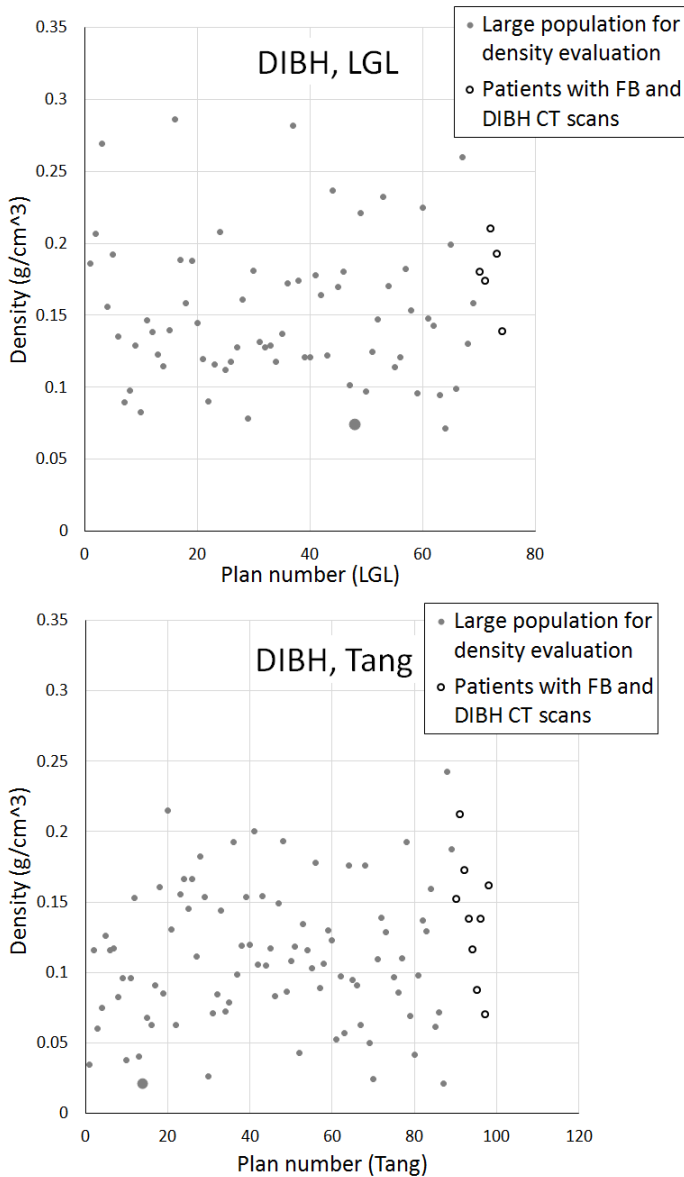


Figure 13. Lung density in isocenter plane for patients planned for LGL (left) and Tang (right) treatments that have treatment plans planned on DIBH CT scans. The DIBH CT scan lung density for the patients with both FB and DIBH scans are also shown for comparison. The larger dots (gray) symbolizes the plans chosen for AAA, AXB and MC comparisons.

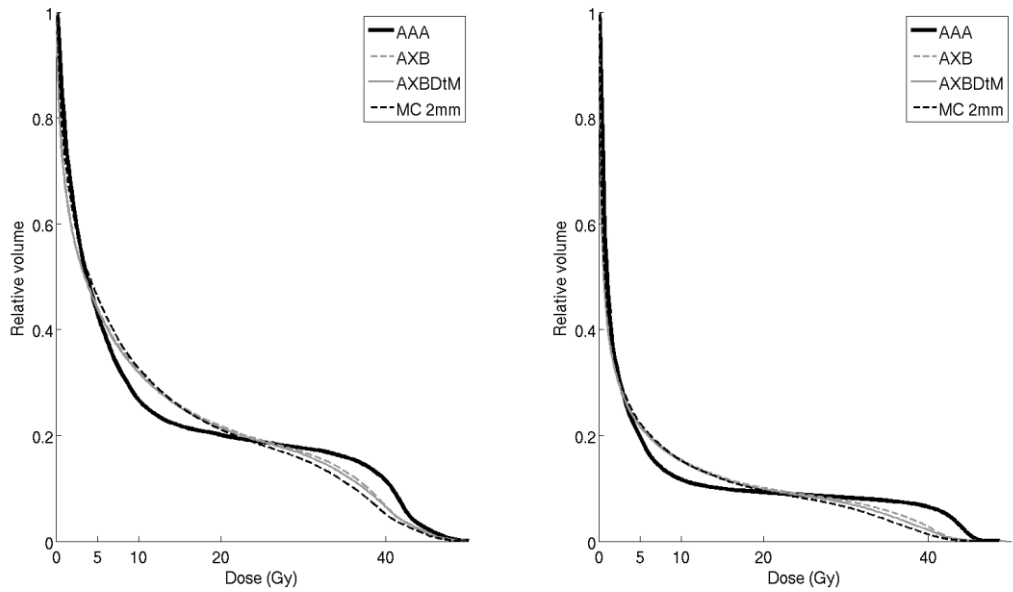


Figure 14. DVH for ipsilateral lung for a LGL (left) and a Tang (right) breast cancer treatment plan that were planned on the DIBH CT scan with the lowest lung densities observed. Dose calculated with AAA, AXB (dose to water), AXBDtM (dose to medium) and MC.

6 DISCUSSION

Reducing the uncertainties in the estimation of absorbed dose to the patient is a continuous work. The level of dose accuracy for megavoltage photon beams in external radiotherapy is discussed in AAPM Report no 85 [35]. The uncertainty at present (year 2004) is estimated to be 4.3 % (in terms of one standard deviation) when excluding dose calculation. When 2-3 % uncertainty in the dose calculation are factored into the total uncertainty the overall uncertainty is 4.7-5.2 %. A level of 5 % uncertainty is discussed as a desired and achievable level of accuracy for external radiation therapy [35]. However, it is recognized in [35] that this level of accuracy in the dose calculation is not achievable with many existing algorithms. It is for example discussed that some traditional dose calculation methods produce up to 10 % systematic errors in the dose in the thorax region when charged particle equilibrium is not assured. The results in this thesis are in line with this somewhat common knowledge. The difference between the standard pencil beam algorithms (PB and PBC) and algorithms that in an approximate way models change in lateral electron transport (AAA/CC) is illustrated in Paper I. The average decrease in MLD is up to 5% (10 %) when changing DCA in Eclipse (Oncentra).

LGL breast cancer treatments are considered in three out of four studies (Paper I, III and IV). This is a treatment with a complex beam geometry, i.e. adjacent fields. The LGL breast treatment is also giving a considerable lung dose to a group of patients with long expected survival. The risk for milder grades of lung tissue complication can be up to 80% as shown in Paper I. Therefore it is important to work with this type of treatment and continuously decrease the dose to lung tissue as well as to improve the accuracy of the estimation of risk for lung tissue complications. The case study on impact of jaw positioning uncertainty on the dose distribution for a LGL breast treatment (Paper III) was originally initiated to investigate if there was an effect on lung tissue. In Paper I it had been found that there was a difference in biological effect between different DCAs. To be able to conclude on the uncertainties of the estimation of dose at the planning stage it was desirable to investigate the adjacent fields. However, the effect on lung dose was small and difficult to assess and the effects on soft tissue were more apparent.

It is difficult to say how dependent the results of this thesis are on variations in the exact design of treatments for different treatment centers. It should especially be noted that the dose distributions of the SBRT lung treatments studied in this work are calculated on a 3D CT image set. The breathing motions are taken into account by constructing CTV (the solid tumor and

diffuse growth at its borders) for each phase of a 4D CT covering the entire breathing cycle. Then an internal target volume (ITV) is defined that encompasses all positions of CTV. The PTV is defined as ITV with 5-10 mm margin. PTV is required to be covered with a certain percentage of the prescribed dose for the treatment plan to be approved. There are other techniques for SBRT treatment planning that the results obtained in this work may not be valid for. For example some hospitals use the mean intensity projection of all 4D CT phases for dose calculation. Another approach is to use the mid ventilation scan. The 3D CT used for treatment planning in this work is a snap-shot of any phase of the breathing cycle.

Comparing clinical DCAs

The limitations of clinical DCAs in lung tissue is evaluated for the challenging clinical situations of small fields (lung SBRT) and low density lung tissue (LGL delivered with DIBH) in Paper II and IV. For the SBRT Lung treatments in Paper II AAA calculated an up to 10% higher $D_{98\%}$ for PTV compared to AXB. In Paper IV, for the cases of low lung density, the two investigated clinical DCAs calculate quite different lung DVHs. AAA underestimates the DVH for lower doses and overestimates the DVH for higher doses so that V_{10Gy} (V_{40Gy}) is underestimated (overestimated) by up to 5 percentage points. Since the value of V_{10Gy} and V_{40Gy} is around 10-20 % for the AAA calculation this means that the relative effect is large.

The results in Paper I can be used to discuss the differences between DCAs in terms of biological effect. The study showed that the difference between PB and CC was for some NTCP model parameters comparable in size to the uncertainty of the original parameters. The absolute difference in NTCP values was up to 10 percentage points. The suggested solution to this was to adjust the NTCP model parameters. NTCP model parameters could be successfully adjusted to be valid for other algorithms than the reference PB, i.e. the uncertainty from the mathematical adjustment of the parameters was small which indicates that the data points in Figure 10 are shifted to a new S-shaped dose-response curve.

The uncertainty of dose calculation in some clinical situations is much larger than the desired uncertainty of 2-3%. However, this is sometimes compensated by the treatment planning criteria. If all plans are calculated erroneously in a systematic way a treatment planning criterion can still be safe as long as it is adjusted to the erroneous dose level. This rationale was used for SBRT lung treatments [36] when both standard pencil beam algorithms (e.g. PB and PBC) and models that in an approximate way takes changes in lateral electron transport into account (e.g. CC and AAA) were employed clinically for this

treatment type. In the work cited, recommendation for SBRT lung treatments are presented. It was concluded that for treatment planning with CC/AAA-type of algorithms instead of standard pencil beam algorithms the 3x20Gy fractionation scheme had to be adjusted to 3x18Gy. A similar conclusion was made in a study comparing PBC and AAA for SBRT lung treatments [37]. This study resulted in a recommendation of lowering prescribed dose with 10% when changing DCA from PBC to AAA. In Paper II and IV the transition from AAA to the principle-based AXB is studied. For this transition, the variation among patients appears to be larger and without systematics, and the treatment planning criteria cannot be that easily translated to the new algorithm.

Comparing AXB and MC

AXB has been fundamentally investigated in several studies [9, 23, 24, 38-43] and been found to provide a valid and accurate alternative to Monte Carlo calculations. In Papers II and IV, the two accurate principle-based dose calculation methods, AXB and MC, are compared. They are based on the same measured data but otherwise independent.

The two methods cannot be expected to produce identical results. There are for example differences in the accelerator head modelling. However, considering the calculation of dose in the patient geometry, none of those methods is in principle less accurate than the other. Nevertheless, there are potentially differences between the methods also in the dose calculation due to different/inaccurate implementation regarding for example tissue interpretation or calculation parameters such as resolution of the AXB calculation and cut-off energy for the explicit tracking of parameters in the MC calculation.

Compared to AAA, AXB is indeed the clinical DCA presenting the ultimate compliance with the MC calculations in this work. Still, there are differences between AXB and MC. AXB calculated for example an up to 6% higher $D_{98\%}$ compared to MC for the SBRT lung treatments in Paper II. The differences between AXB and MC are also illustrated as a shift in PTV DVHs (Paper II). In Paper IV the differences between AXB and MC are seen in the high dose region of the lung DVHs.

One methodological consideration suitable in this context is the choice of ECUT and the voxel dimensions. According to the recommendations in the BEAMnrc user's manual [4] the range of the electrons at ECUT should be less than 1/3 of the smallest voxel dimension. This means that the lowest density accurately calculated with the MC method would be 0.0038 g/cm³ for 2 mm voxels. The lowest densities included in MC calculations are present in the

DIBH breast treatments in Paper IV (calculated with 2 mm smallest voxel dimension). In those two cases 8 % (Tang case) and 3 % (LGL case) of the voxels within the 15 % isodose have density below 0.0038 g/cm^3 . A less conservative choice of ECUT was used in for example [44]. The electron range at ECUT was in that study allowed to be half the smallest voxel dimension or smaller and the lowest allowed density for 2 mm voxels was therefore 0.0025 g/cm^3 . The number of voxels with density less than this are 6% (Tang case) and 2% (LGL case) for the two MC calculated cases of Paper IV. To investigate the impact of ECUT on the results was beyond the scope of this study and it is assumed that the choice of ECUT is safe also for the low density DIBH cases since the number of voxels below the allowed density is relatively small.

Another methodological issue to discuss when comparing the results of AXB and MC is the method for tissue segmentation. In the MC calculations sharp borders are used between tissue types defined by a certain density value. AXB on the other hand is mixing materials when the density is in an interval between two tissue types. It would be interesting to do the AXB calculations with the same tissue density borders as MC to see if the difference in tissue segmentation methods would affect the dose distributions.

Without further investigations, it is difficult to say which one of the two methods AXB and MC that is closest to the ‘true’ dose distributions. Nevertheless, the results from two calculation methods are in this work used to suggest in which interval the ‘true’ dose is likely to be.

7 CONCLUSIONS

This work indicates that

- The uncertainties in estimated dose at the treatment planning stage can be relevant for treatment outcome.
- The uncertainties in estimated dose at the treatment planning stage is sometimes larger than desired for the clinical situations investigated.

7.1 Paper-specific conclusions

Paper I

The error that can be introduced in NTCP estimates due to differences in dose calculation algorithms can be of the same magnitude as the confidence intervals of calculated NTCP values. The use of algorithm-specific NTCP model parameters can prevent the introduction of this additional uncertainty.

Paper II

Two accurate dose calculation methods (AXB and MC) were found to comply with similarly shaped PTV and GTV DVHs for the challenging situation of SBRT conventional 3D conformal lung treatment plans. A larger difference was generally found comparing AAA and AXB. The largest difference between AAA and AXB was found for the parameter PTV- $D_{98\%}$ and was up to 10% (AAA overestimating compared to AXB). The difference in the same parameter when comparing AXB and MC was found to be up to 6% (AXB overestimating compared to MC).

A change from AAA to AXB for treatment planning of SBRT lung treatments, without a change of treatment planning criteria, can increase the dose to the lung tissue close to the tumor due to an increase of the 100% isodose volume of up to 20% for some patients.

It was not possible to characterize the treatment plans with larger differences between AAA and AXB using the patient/plan characteristics studied, i.e. PTV volume, volume of lung tissue part of PTV, distance from GTV edge to nearest lung edge, average of lung density in three points two centimeters from PTV, proportion of PTV edge in lung tissue.

Paper III

A treatment planning protocol with 1 mm overlap does not considerably improve the coverage of PTV in the case of erroneous jaw positions causing gap between fields, but increases the overdosage in PTV and the dose to healthy tissue, in the case of overlapping fields, for the case investigated. Therefore, a treatment planning protocol including 1 mm field overlap can be questioned. Before recommendations are made further investigations are needed, which should consider, for example, decreased daily setup errors, hypofractionation, and negative side effects in healthy tissue.

Paper IV

For LGL, the difference between AAA and AXB in calculated lung dose was similar for FB and DIBH, whereas the difference increases with decreased lung density in DIBH for Tang treatments. For DIBH treatments the underlying CT-scans for a group of 157 patients show densities in the isocenter plane between 0.08 and 0.3 g/cm³ for LGL and between 0.02 and 0.25 g/cm³ for Tang treatments. For medium and high lung density, none of the studied lung DVH parameters differed more than approximately 3%. For the low density cases the difference can be up to 5%. The least affected lung DVH parameter was V20Gy which was affected less than 2% for all cases (FB/DIBH, LGL/Tang) and densities studied.

The AXB and MC predicted similar lung DVHs which is encouraging the use of AXB. The difference between AXB and MC was less than 1% for all DVH parameters studied except V5Gy that differed 3%.

To minimize changes in the treatment due to change of algorithm V_{20Gy} is a suitable parameter for controlling lung dose. V_{10Gy} is a less suitable choice, since in that case the algorithm change will result in a more conservative treatment plan regarding lung dose.

ACKNOWLEDGEMENT

Table 5. List of people that should be acknowledged

ID	Thank you...
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APPENDIX

Hedin, E., Bäck, A., Swanpalmer, J. and Chakarova, R. *Monte Carlo simulation of linear accelerator Varian Clinac iX* Report MFT-RADFYS 2010:01

MFT – RADFYS 2010:01

Monte Carlo simulation of linear accelerator Varian Clinac iX

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Abstract

This report presents methods and results from the development and verification of a Monte Carlo model of a Varian Clinac iX linear accelerator of nominal energy 6 MV.

Simulations are made by the BEAMnrc/EGSnrc Monte Carlo code package. Accelerator head components (target, primary collimator, flattening filter, monitor chamber, secondary collimator and jaws) are described in a simplified way according to the technical specifications supplied by Varian Medical Systems. The parameters adjusted in the model are related to the energy and the spatial distribution of the electrons incident on the target. It is assumed that the electrons are monoenergetic, normally incident on the target with Gaussian spatial distribution.

The process of parameter tuning and model verification involves two steps. The output from the accelerator head is simulated in one step and the corresponding dose distribution in water is calculated in a subsequent step. Simulated data are compared to measured data visually, quantitatively by directly comparing the data values and by statistical weighting of the differences in a χ^2/NDF analysis. The optimum model parameter set is found to be electron energy 5.7 MeV and focal spot width (FSW) 0.1 cm FWHM.

The model is verified by depth dose curves and profiles at different depths between 1.5 and 20 cm for field sizes ranging from $2 \times 2 \text{ cm}^2$ up to $40 \times 40 \text{ cm}^2$. Good agreement within 1% has been achieved between measured and simulated data for nearly all cases. Somewhat larger deviations are detected for profiles at the depth of dose maximum and for the depth dose distribution of $2 \times 2 \text{ cm}^2$ field.

The accelerator model has been reviewed by international experts and phase space data produced for particular geometries accepted in the IAEA Phase-space database for external beam radiotherapy (<http://www-nds.iaea.org/phsp/phsp.htmlx>). The model allows simulation of open fields and of wedge fields by applying step-and-shoot method. In a future work, 15 MV nominal energy will be considered and a MLC component will be included to simulate more complex field shapes.

Keywords: Monte Carlo methods, simulation, radiation therapy equipment, linear accelerator

Sammanfattning

Detta är en internrapport producerad i projektet ”Monte Carlo-baserad NTCP-utvärdering”. Rapporten sammanfattar arbetet med att utveckla en Monte Carlo-modell för en linjäraccelerator (Varian Clinac iX, nominell energi 6 MV) använd för extern strålterapi.

På avdelning för strålbehandling används rutinmässigt ett dosberäkningssystem. I dosberäkningssystemet planeras vilka fält och vilken dos som skall ges som behandling. Dosberäkningssystemet levereras med dosberäkningsalgoritmer som med hjälp av approximationer snabbt kan ge ett svar på hur dosfördelningen kommer att se ut. Arbetet med att förfinas algoritmer pågår kontinuerligt. Ett verktyg som kan användas för att bestämma dosens fördelning på ett mer sofistikerat sätt är Monte Carlo-simulering. En väl anpassad Monte Carlo-accelerator modell kan användas vidare för simulering av strålningens växelverkan i patientens vävnad och utvärdering av precisionen hos dosberäkningsalgoritmen. Speciellt anses Monte Carlo-simuleringar ge mer korrekt dos i komplicerade geometrier.

I den aktuella rapporten presenteras metod och resultat vid anpassning av parametrar i en Monte Carlo-modell baserad på EGSnrc transport-kod. Processen innefattar två steg, dels att simulera transporten av elektroner och fotoner genom acceleratorhuvudet samt samla in alla partiklar på ett visst avstånd under acceleratoren i en phasespace-fil och dels att simulera vad dosen blir i ett fantom (vattentank) under acceleratoren som träffas av alla partiklar ut phasespace-filen. Vid simulering av transporten av partiklarna genom acceleratoren används det för strålterapi avsedda gränssnittet BEAMnrc och vid simulering av dosen i fantom används DOSXYZnrc. Simuleringen av acceleratorhuvudet startar med en stråle elektroner som faller in mot targetet.

De parametrar som anpassas i Monte Carlo-modellen är två egenskaper hos de mot target infallande elektronerna: i) energi (de antas vara monoenergetiska) och ii) vidden på strålen (intensiteten antas vara Gaussiskt fördelad i rummet), som karakteriseras av FWHM. Olika parameterkombinationer testas och den mest optimala kombinationen väljs ut efter en trial-and-error procedur som slutar när överensstämmelsen mellan uppmätt och simulerad data är god nog. I detta arbete blev de slutgiltiga parametrarna 5.7 MeV i kombination med 0.1cm FWHM. Med dessa parametrar kända är det möjligt att simulera dosen i CT-baserade patientfantom.

Nyckelord: Monte Carlo, simulering, strålterapi, linjäraccelerator.

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List of abbreviations

- TPS – Treatment Planning System
- FWHM- Full Width at Half Maximum (i.e the width of the distribution where the distribution is half of its maximum value)
- FSW – Focal Spot Width (in this work characterized by FWHM of Gaussian distribution)
- DBS - The variance reduction technique Directional Bremsstrahlung Splitting
- SSD - Source Surface Distance
- NDF - Number of Degrees of Freedom
- OAF - Off Axis Factor
- SE - Standard Error (Standard deviation of a stochastic variable propagated through a given formula as an estimate of the error of a calculated value of a given physical quantity)
- MLC - Multi Leaf Collimator
- IMRT - Intensity Modulated Radiation Therapy

1 Introduction

Radiation therapy by photons is one of the most effective techniques for cancer treatment. Ionising radiation is used to destroy tumour cells by damaging their DNA, making it impossible for these cells to continue to grow and divide. The tumour mass may spread and infiltrate healthy tissues. The goal of radiation therapy is to damage as many cancer cells as possible, while limiting harm to nearby healthy tissue. Radiation killing of cells is a stochastic process and has a probabilistic nature. Its evolution is determined by random events of energy deposition in a single interaction. However the effect of the radiation on a large collection of cells is deterministic and related to the amount of the mean energy imparted to the medium, i.e. the absorbed dose. Oncologists prescribe different doses depending on the type and stage of the cancer being treated in order to achieve a certain clinical effect.

The accuracy of the dose delivery is of great importance. Larger dose causes significant complications in the normal tissue, whereas reduced dose decreases the probability of tumour control. Therefore the treatment is carefully planned. Tumours are diagnosed and localized with 3D imaging techniques and the irradiation of the patient is simulated by advanced software referred to as a treatment planning system (TPS). The calculation includes (i) configuration of the source of the delivered radiation, i.e. the accelerator output and (ii) simulation of the photon and electron transport through the tissue to obtain dose distribution in the patient.

Different simplifications and assumptions are needed in TPS algorithms in order to keep balance between the requirements for fast calculations and for sufficient accuracy of the result. The treatment planning system does not model accelerator components. It rather replaces the machine by a set of virtual sources fitting beam output to certain measured data. Semi-empirical algorithms are implemented to carry out photon and electron transport through the patient. Basic idea is that tissue mainly consists of water and one can therefore calculate the absorbed dose in a water phantom. Libraries of pre-calculated energy deposition kernels in water are produced for different elementary geometries like pencil beam and point kernels. Dose values in tissues with deviating electron densities are derived applying correction factors to dose in water. Validation of the results from treatment planning systems is needed, particularly in situations of complex field shapes, inhomogeneous media and interfaces.

The Monte Carlo method is the most accurate method for dose calculations in a wide variety of radiation conditions. Characterisation of the particle beam

emitted by an accelerator can be addressed as a separate task preceding the simulation of the interactions in the irradiated tissue for external radiation treatment. Typical accelerator assembly includes electron gun injecting electrons into a waveguide where they are further accelerated and delivered into the treatment head in form of high-energy electron pulses. This primary electron beam hits the target producing bremsstrahlung photons. The bremsstrahlung photons penetrate a filtering system, beam monitor detectors and beam defining system and exit the accelerator head as a photon beam with desired characteristics. The Monte Carlo modelling of the accelerator head includes the generation of the bremsstrahlung photons and their further transport through the head components. The model is sensitive to the component descriptions, e.g. target thickness and density, primary collimator specifications, shape and density of the flattening filter, etc [Keall2003, Chetty2007, Sheikh-Bagheri2002]. Therefore the technical data embedded in the model are of importance in spite of the simplifications in the component description by combinatorial geometry.

The parameters of the primary electron beam, such as the dimension of the spot, the energy and the spatial distribution, are in general unknown. In the Monte Carlo model, they can be initially set according to the manufacturer recommendations. Their values are then adjusted in a trial and verify process, e.g. simulation of the accelerator output assuming certain parameters, calculation of dose profiles and depth dose distribution, comparisons with measured ones, refining the source parameters until the comparison shows acceptable deviations.

Different strategies for tuning the parameters of the primary electron beam are reported in the literature. It is investigated in which radiation geometry the effect of a certain parameter dominates and how to determine its value with higher precision. For example, the derivation of best estimates by [Sheikh-Bagheri2002] is based on comparison of calculated and measured values of in-air off-axis factors for large fields together with calculated and measured central axis relative depth-dose curves. The off-axis factors are found to be sensitive to the mean energy of the electron beam and to FWHM of the radial distribution of the beam assumed to be Gaussian and cylindrically symmetric. The depth-dose curves are shown to be sensitive to the electron beam energy, and to its energy distribution, but not sensitive to the FWHM of the electron beam intensity distribution. [Pena2004] concludes that the accelerator model can be commissioned by large field dose profiles only since these are sensitive both to the energy and width of the electron beam. Depth dose distributions are found to be less sensitive to changes in beam energy. Other authors [Sham2008, Scott2009] recommend implementation of output factors of small fields of order 0.5x0.5 cm or less for adjusting the FSW.

Published results from Monte Carlo modelling of 6 MV Varian accelerators show variations in the optimal parameter values found. For example, [Sheikh2002] report primary electron energy of 5.7 MeV with 3% energy spread and a FSW of 0.1 cm FWHM as optimum parameters for a high energy machine, [Keall2003] report electron energy of 6.2 MeV with a 3% energy spread and a FSW of 0.13 cm FWHM for a 2100 EX Varian, [Jutemark2005] presents 6.4 MeV energy of a monoenergetic primary electron beam and a FSW of 0.12 cm FWHM as optimal parameters for a Varian Clinac-23EX accelerator. Variations in the derived optimal parameter values are observed even for one and the same accelerator type (see for example the data for Varian 2100 in table III by [Keall2003]). Since free distribution and information exchange of technical data is not allowed by Varian Medical Systems, detailed comparative studies of Monte Carlo models is not possible. Consequently, optimal parameters reported in the literature can not be automatically adopted since they may not be valid outside the particular model used to derive them. In addition the measured data sets used as a reference in the optimisation procedure may differ even for identical accelerators. Thus developing and optimising a Monte Carlo accelerator model locally for each particular machine becomes a necessary basis for performing radiation treatment simulations.

This work presents the Monte Carlo model developed for the Varian Clinac iX accelerator at the radiation treatment department at Sahlgrenska University Hospital (treatment room 8).

2 Material and methods

The Monte Carlo code package BEAMnrc (Graphical User Interface 2.0) [Walters2009] is used to design a model of linear accelerator Varian Clinac iX. Accelerator components considered in a simplified way are the target, primary collimator, flattening filter, monitor chamber, and upper and lower jaws. The model is based on technical data provided by Varian Medical Systems. It should be noted that several densities are not explicitly specified in the documentation obtained and dimensions presented in different drawings and tables are not always consistent. Densities and dimensions of the accelerator components are fixed during the simulations. Optimisation parameters are the energy and the FSW of the primary electron beam. In-air off-axis factors are used as suggested by [Sheikh-Bagheri2002] and comparison is made between calculated and measured water dose profiles at different depths, depth dose curves and output factors for various field sizes. The calculations are performed partly on a local computer with an Intel Core-2 Duo processor (1066MHz FSB, 4MB L2) using Ubuntu operating system and

partly on a Linux cluster at the National Supercomputer Centre (NSC), Linköping, Sweden (operating system CentOS 5 x86_64 and Intel Xeon E5345 processors). The code is run in a parallel mode on the NSC cluster, using several processors for each job.

The optimisation procedure includes two main steps, namely accelerator head simulation with radiation field as result followed by calculation of the dose distribution in irradiated water phantom. The radiation field is stored in an intermediate phase-space file containing information about the particle speed, direction and charge/type. The iterative method of optimising the model is shown schematically in Figure 1. Simulations are made for several combinations of electron energy and FSW. Dose distributions of various field sizes are analysed for each parameter combination. The optimum parameter combination is then verified by simulating the field sizes presented in Table 2 section 2.7.

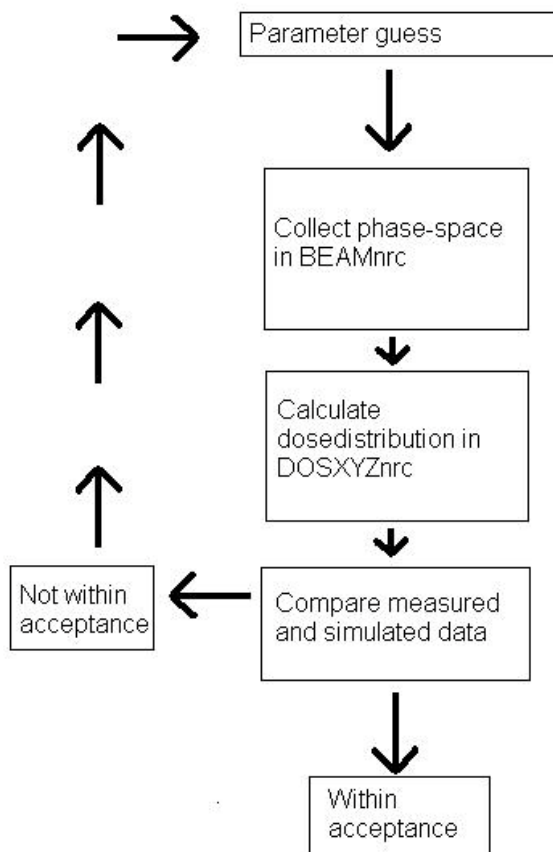


Figure 1: Sketch describing the iterative method of finding the optimum parameter set describing the radiation field.

2.1 Accelerator head simulation

A sketch over the accelerator head and schematic boxes symbolizing phase space and the region with dose distribution of interest are shown in Figure 2. The primary electron beam hitting the target is assumed to be monoenergetic, normally incident with a gaussian radial distribution (BEAMnrc: source number 19). The width of the gaussian radial distribution, the FSW, is characterized by FWHM.

The global photon and electron cut-off energy is 0.01 MeV and 0.7 MeV respectively. The variance reduction technique named directional bremsstrahlung splitting (DBS) is used. The splitting number is set to 1000 and the electron splitting is performed in the lower layers of the flattening filter as recommended in the BEAMnrc users manual [Walters2009]. Range rejection is turned on with varying ECUTRR (= the minimum energy a charged particle requires to be able to exit the accelerator still having more than 0.7 MeV). Range rejection is considered for electrons with energy less than 2 MeV (ESAVE_GLOBAL = 2) except for in the target where range rejection is considered for electrons with energies less than 1 MeV. The same range rejection parameters are used for example by [Hasenbalg2008].

2.2 Simulation of in-air profiles

A first estimate of the energy of the electrons incident on the target is found by using the in-air off axis factors as described by [Sheikh-Bagheri2002]. Water-kerma-profiles (collision) are obtained by processing the phase-space file in a modified version of BEAMDP code. The weight of each photon in the phase space is multiplied by its energy, mass-energy-absorption coefficient [Hubbel1995] and one over the cosine of the angle its direction makes with the z-axis. Only the photons from the phase-space file are taken into account. The contaminating electrons are estimated to influence the results with a magnitude comparable to the uncertainty of the method (for uncertainty reasoning see page 12). Collision kerma profiles are normalised to the value at the central axis to obtain off-axis factors. Collision kerma is assumed to be proportional to the signal from an ionisation chamber with a full build-up cap, an assumption based on the principles of small detector cavities in a region of charge particle equilibrium in which the photons are very unlikely to contribute directly to ionisation but more likely via secondary electrons.

The in-air off axis method is fast since the step of calculating dose distribution in the water phantom is avoided. The energy of the electrons incident on the target obtained by this method is regarded to be a first coarse estimate because only one distance from the target is considered, namely the distance at which

the phase-space is collected. Changes in FSW may influence the value of optimal electron energy found. However, the FSW sensitivity of the in-air factors is smaller compared to the electron energy sensitivity.

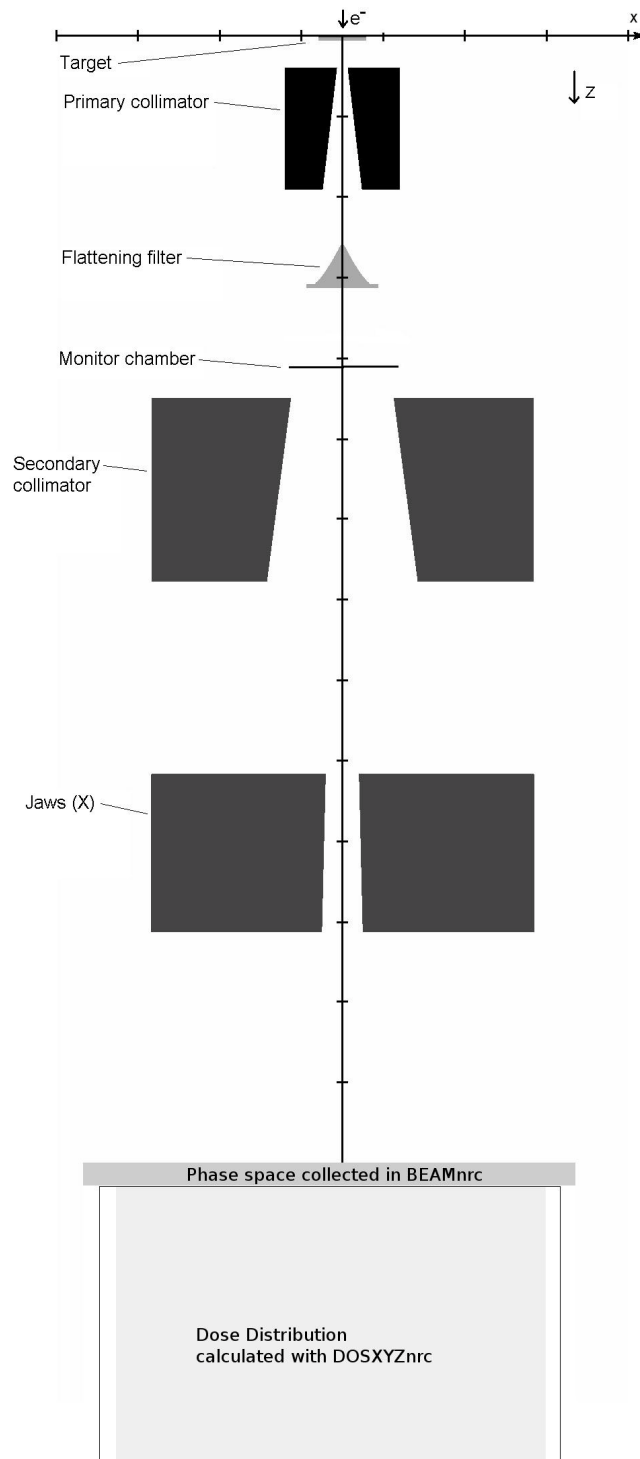


Figure 2: Sketch over the accelerator head, phase space collection and region with dose distribution of interest. x/z -plot at $y=0$ (central axis). Y direction Jaws not visible in this plane when separated.

2.3 Calculation of dose distributions in water

The dose profiles in water phantom are calculated using the Monte Carlo code DOSXYZnrc. The depth dose curves are calculated by the CHAMBER module in BEAMnrc code. No range rejection is used in both cases. The electrons are tracked until their energy falls below 0.512 MeV and the photons are tracked until their energy is below 0.010 MeV. The phantom size is large enough to include the irradiation field with 10 cm lateral margin and 10 cm deeper than the last data point.

In DOSXYZnrc the region of interest is divided into voxels with dimensions depending on the resolution needed. When simulating dose profiles for fields larger than $4 \times 4 \text{ cm}^2$ the central voxels are 1 cm wide (square top area) and the remaining voxels are 0.3 cm wide. In the cases of 4×4 and $2 \times 2 \text{ cm}^2$ fields the central voxels are 0.5 cm wide and the remaining ones are 0.5 cm and 0.2 cm wide, respectively. The voxel width in the case of $4 \times 4 \text{ cm}^2$ and $2 \times 2 \text{ cm}^2$ field sizes is chosen to correspond to the dimensions of the ionisation chambers to make the simulated penumbral region comparable to the measured (in the cases of 4×4 and $2 \times 2 \text{ cm}^2$ field sizes the penumbral region constitutes a large part of the field). Because of the measurement uncertainties associated with the size of the detector and its material the smallest field size considered in this work is $2 \times 2 \text{ cm}^2$.

When performing simulations for several different parameter combinations (see Section 2.6), dose profiles are extracted at 1.5, 5 and 10 cm depth from 0.5 cm high voxels. When verifying the optimum parameter set, dose profiles are calculated at 1.5, 5, 10 and 20 cm depth using 0.5, 0.5, 0.5 and 1 cm high voxels, respectively. The measured dose profiles for $40 \times 40 \text{ cm}^2$ field size are half-profiles. Therefore the simulated profiles are in this case averaged over positive and negative x-axis to obtain better statistics.

The depth dose (BEAMnrc) values are determined in 0.2 cm high standing cylinders with a radius of 0.75 cm at the central axis, except for the case of $2 \times 2 \text{ cm}^2$ field. In the latter case the cylinders are 0.3 cm high with a radius of 0.15 cm.

2.4 Ionisation chamber measurements

The in-air measurements are performed at a source-detector-distance of 100 cm using a cylindrical ionisation chamber (Exradin T2 Spokas Thimble chamber, 0.53 cm^3 , 4.6 mm diameter of the collecting volume) with a 3 mm thick brass build-up cap to ensure charged particle equilibrium over the measuring cavity. The chamber signal is assumed to be proportional to dose to water at the centre of the chamber. Air crossline profiles (the x-axis direction

defined by the lower jaws) are measured with 1.5 cm steps. The measurement at the central axis position is repeated to achieve better precision. No chamber correction is made for changes in temperature and pressure during the process taking between 30 minutes and one hour.

The water measurements are performed using cylindrical ionisation chambers as follows. For field sizes larger than 2x2 cm² the compact chamber CC13, manufactured by Iba Dosimetry is used (0.13 cm³, inner air cavity diameter 0.6 cm). For the field size 2x2 cm² the PTW Pin-Point (0.015 cm³, inner cavity diameter 0.2 cm, central electrode of steel) chamber is utilized. Source-surface-distance (SSD) is equal to 100 cm in all water measurements except for the case of the asymmetric 10x10 cm² field. Dose profile for this asymmetric field is measured using the compact chamber CC04 (0.04 cm³, inner cavity diameter 0.4 cm) at SSD=90 cm.

The uncertainties in the above described measurements are estimated to be about 0.5%. Regarding the dose profile measurements the uncertainty, expressed in mm, in the penumbra region for small field sizes is estimated to be less than 1 mm. For the field sizes 10x10 cm and 20x20 cm at a depth of 10 cm this uncertainty is estimated to be around 0.5 mm. The uncertainties concerning the depth dose measurements in the build-up region are more difficult to estimate due to, among other things, the lack of charge particle equilibrium in this region as well as the air cavity size of the cylindrical ionization chamber used for the measurements.

2.5 Comparison, measurement-simulation

The measured and simulated dose profiles and depth dose curves are compared visually and in some cases also by two different methods, namely by χ^2/NDF (Number of Degrees of Freedom) cost function and by the number of simulated data points deviating more than a given percentage from the corresponding measured data. The value of χ^2/NDF is calculated according to the equation:

$$\chi^2 / NDF = \sum_{i=1}^N \frac{(s_i - m_i)^2}{\sigma_i^2} / (N - 1)$$

where m_i and s_i are measured and simulated normalised dose values, respectively. σ_i is the standard error of the i-th simulated value and N is the number of data points compared. NDF is in this case $N-1$ since σ is estimated using s_i (for more details regarding the statistics, see the BEAMnrc users manual [Walters2009] or [Walters2002]). Data beyond dose maximum are included in the χ^2/NDF evaluation because of the measurement uncertainties in the build-up region.

A comparison between simulations in the build-up region is presented in the appendix along with a discussion regarding differences in simulation methods and versions of BEAMnrc code.

2.6 Finding the optimum parameter combination

2.6.1 In-air simulations

The field sizes and parameter combinations used for in-air simulations are presented in Table 1.

Table 1: Field sizes and parameter combinations used for in-air simulations. The symbol *x* indicates that simulation is made.

		Energy (MeV)						
field size (cm ²)	FSW (cm)	5.2	5.4	5.5	5.6	5.7	5.8	6.0
40x40	0.05						x	
40x40	0.1						x	
30x30	0.05			x	x		x	x
20x20	0.05	x	x		x	x	x	

2.6.2 Dose profiles in water

Simulations are initially performed for 10x10 cm² field with fixed electron energy at 6 MeV and varying the FSW from 1 cm to 0.06 cm. Field size 40x40 cm² is simulated for the following energy/FSW parameter combinations: 5.8 MeV with 0.05 and 0.1 as well as 5.7 MeV with 0.08, 0.1 and 0.15 cm FSW. Field size 20x20 cm² is simulated for the same parameter combinations except for the combination 5.7 MeV with 0.08 cm FSW. The start values of the parameter combination are based partly on published results for similar accelerators and partly on the analysis of the in-air simulations and measurements. At the stage of parameter optimisation, only crossline dose profiles (x-direction defined by the lower pair of collimators) are analysed.

2.6.3 Depth dose distributions in water

Simulations are made for a 10x10 cm² field when keeping the FSW at a value of 0.06 cm and varying the energy in steps of 0.2 MeV from 5.2 MeV to 6.4 MeV in order to investigate the response of the depth dose curve to energy changes.

2.7 Verifying the optimum parameter combination

The optimum parameter combination is verified by comparing simulated and measured crossline profiles for the fields listed in Table 2. Inline dose profiles (y-direction defined by the upper pair of collimators) for 10x10 and 20x20 cm fields are included in the analysis.

Table 2: Simulations in BEAMnrc when verifying the optimum parameter combination. In the second column the associated DBS-radius defined at a distance 100 cm from the top of the target is given. In the last column the calculated dose distributions are given.

Field size (cm ²)	DBS-radius (cm)	
2x2	10	depth distribution, profile
4x4	20	depth distribution, profile
10x10	20	depth distribution, profile
20x20	30	depth distribution, profile
40x40	30	depth distribution, profile
10x10*	20,30	profile
x=4,y=20**		profile
*Asymmetric, see the explanation below		
**Rectangular field		

When verifying the optimum parameter set a 10x10 cm² asymmetric field is simulated with 5 cm offset in x-direction. Results for -5 cm offset are considered to be a mirrored image of these for 5 cm offset. In general, asymmetric fields are essential for treatment plans containing joint fields. A symmetric (around the central axis) but rectangular field with dimensions x=4 cm and y=20 cm is also simulated to further test the performance of the model.

Output factors are calculated for the symmetrical fields in Table 2. The output factors are defined as the ratio between the dose at the central axis at 10 cm depth, for a given field size, and the dose at central axis at 10 cm depth for the 10x10 cm² square reference field. The dose at 10 cm depth is assessed in two different ways, namely, (i) from a fifth grade polynomial fitted to dose values between depth 5 cm and 20 cm and (ii) from the voxel containing the point of interest.

3 Results

The phase-space files obtained typically contain about $3.5E8$ particles for $20 \times 20 \text{ cm}^2$ field size and between $2E8$ and $8E8$ particles for $30 \times 30 \text{ cm}^2$ field size. The relative uncertainty (1 standard deviation) of the in-air simulated values is 0.1% or smaller. Verification profiles in water are obtained by simulation of more than $1E7$ histories per cm^2 at $\text{SSD}=100 \text{ cm}$. Phase space particles are recycled 10 to 15 times. Statistical uncertainties of the simulated dose in water vary. Better statistics is provided when verifying the optimum parameter set compared to that during the optimisation procedure.

3.1 Finding the optimum parameter combination

3.1.1 In-air simulations

It is found that changing the value of FSW from 0.1 to 0.05 cm does not significantly influence the in-air profiles. The simulated off-axis factors for different energies, fixing FSW at 0.05 cm, are presented in Fig. 3 together with the measured off-axis factors. The off-axis distance is 12 cm and 7.5 cm for 30×30 and $20 \times 20 \text{ cm}^2$ field size, respectively. This off-axis distance is chosen to avoid dose gradients. The optimum energy for 0.05 cm FSW is found to be 5.71 and 5.78 MeV for 20×20 and $30 \times 30 \text{ cm}^2$ field size, respectively. The error in the determined energy because of uncertainty in the simulated off-axis factors is difficult to determine from the residuals of the linear fit (the few degrees of freedom yield $\pm 0.5 \text{ MeV}$, 95% confidence interval of the energy from LINEST (Excel 2003) and the t-distribution). In order to take into account the uncertainty of the simulated off-axis factors a linear fit is made for maximum simulated off-axis factors (profile value +95% confidence interval) and for the minimum simulated off-axis factor (profile value -95% confidence interval) respectively. The energy difference is 0.06 MeV. An error of measured off-axis factors of $\pm 0.25\%$ leads to uncertainty in the determined energy of $\pm 0.07 \text{ MeV}$. Thus the method gives at least $\pm(0.07+0.06/2)=\pm 0.1 \text{ MeV}$ uncertainty in the energy estimate. The energy intervals should not be considered as statistical confidence intervals but rather as precision limits of the method.

3.1.2 Dose profiles in water

No change in the lateral profiles is found for 10x10 cm² field when decreasing FSW below 0.1 cm. Moreover, the profiles obtained for the optimum energy of 5.7 MeV from the in-air simulations in combination with FSW 0.1 cm are found to be in compliance with the measured data, see section 3.2.1.

3.1.3 Depth dose

Regarding depth dose curves, energies between 5.6 and 6.2 MeV could be considered equally good when compromising between good fit at dose-max and good fit at deeper depths (assuming that the change in depth dose curve due to FSW is negligible). However as shown in Fig. 4 (125 degrees of freedom, depth 3 to 30 cm), the chi² analysis is clearly pointing out an optimum energy of 6 MeV when 0.06 cm FSW is used.

3.2 Verifying the optimum parameter combination

The optimum parameter set chosen is 5.7 MeV energy of the electrons incident on the target and FSW 0.1 cm FWHM.

3.2.1 Crossline dose profiles

Crossline dose profiles (x-direction) are shown in Figs. 5 to 9. All profiles are at the central axis plane. The dose is normalised to the dose at the central axis for each depth.

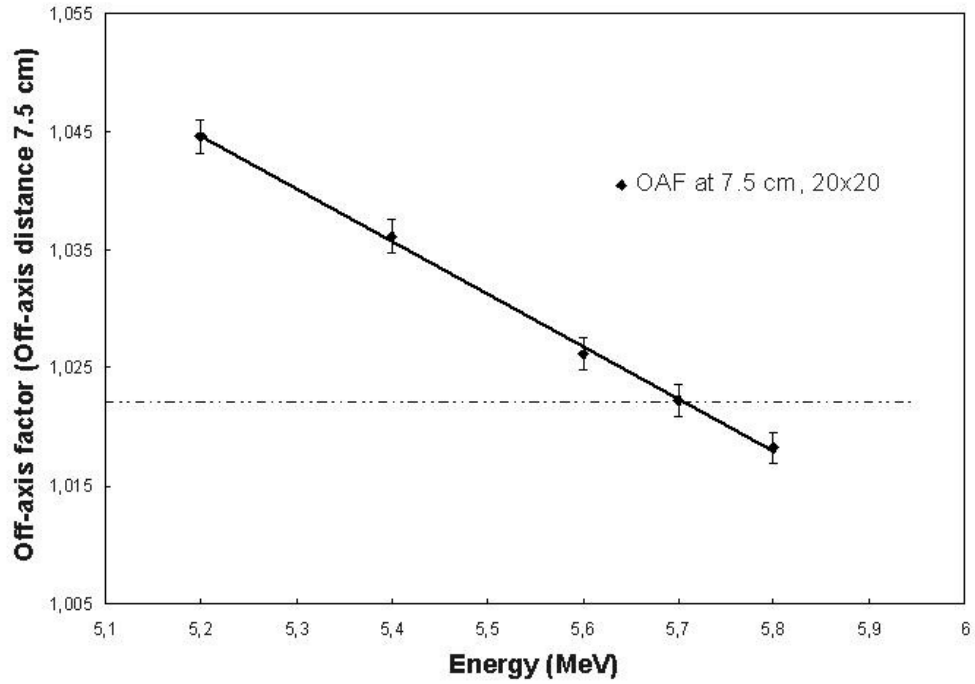
The simulated and measured profiles for 40x40 cm² field size for the optimum parameter set [5.7 MeV 0.1 cm] are shown in Fig. 5. None of the simulated data points, between x=0 and x=19.75 cm, in Fig. 5a, 5b, 5c and 5d deviate from the measured data more than 1.5%, 1%, 1% and 1.8% of the central axis dose at the given depth, respectively. The deviation should be considered in conjunction with the relative standard errors of the normalised simulated values which, within the actual interval, are between 0.3% and 0.4%.

The simulated and measured profiles for 20x20 cm² field size for the optimum parameter set [5.7 MeV 0.1cm] are presented in Fig. 6. None of the simulated data points between, x=-8.95 and x=8.95 cm in Figure 6a, 6b, 6c and 6d deviate from measured data more than 1.4%, 1%, 1.3% and 1.2% of the central axis dose at the given depth, respectively. The deviation should be considered together with the relative standard errors of the normalised

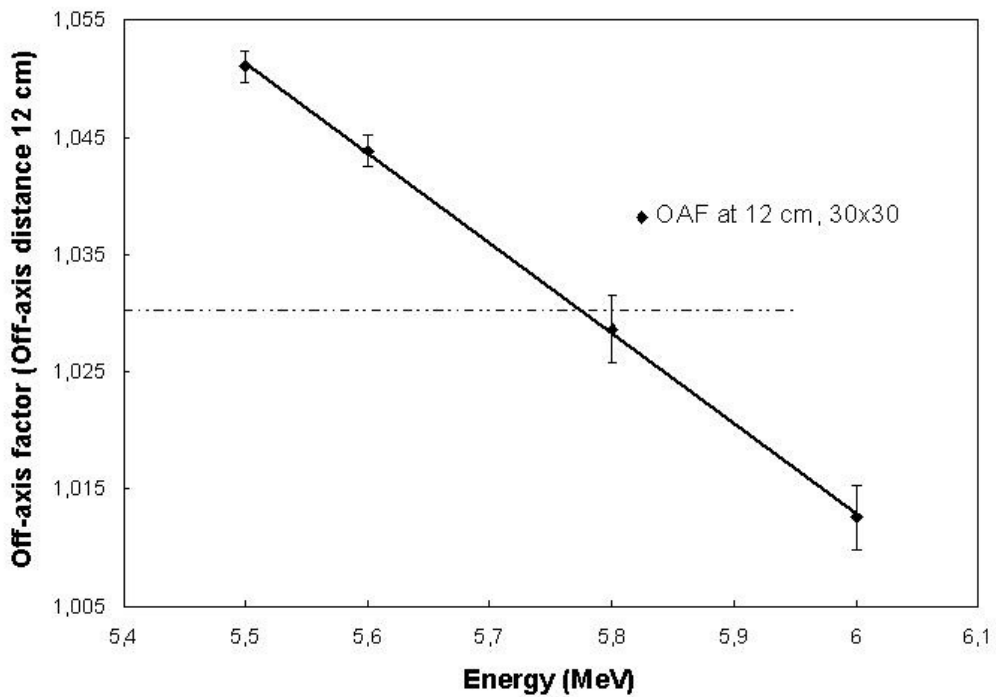
simulated values which, within the actual interval, are between 0.45% and 0.55%.

The chosen parameter set [5.7 MeV 0.1 cm] is further verified for field sizes 10x10, 4x4 and 2x2 cm². These profiles are shown in Figs. 7 to 9. In the case of 10x10 cm² field size none of the simulated data points between x=-4.25 and x=4.25 cm in Figs. 7a, 7b, 7c and 7d deviate from measured data more than 1.7%, 1%, 1.5% and 1.2% of the central axis dose at the given depth, respectively. The deviation should be considered in conjunction with the relative standard errors of the normalised simulated values. Within the actual interval these are around 0.4%.

The profiles for field sizes 4x4 and 2x2cm² are analysed visually and the simulated penumbra is seen to agree with measured data to within 1 mm except for at 1.5 cm depth for the 2x2 cm² field and at 1.5 cm and 5 cm depth for the 4x4 cm² field, where the difference is between 1 and 1.5 mm. This larger difference is observed only in one of the penumbra regions of the field. It should be noted that non centred measured profiles are used in this case.



(a)



(b)

Figure 3: Off-axis factors (OAF) plotted against the energy of electrons incident on the target for the field sizes (a) 20x20 cm² and (b) 30x30 cm². The dashed line represents the measured value of off-axis factor at 7.5 cm and 12 cm off-axis distance, respectively. The error bars represent the 95% confidence interval of the simulated data points.

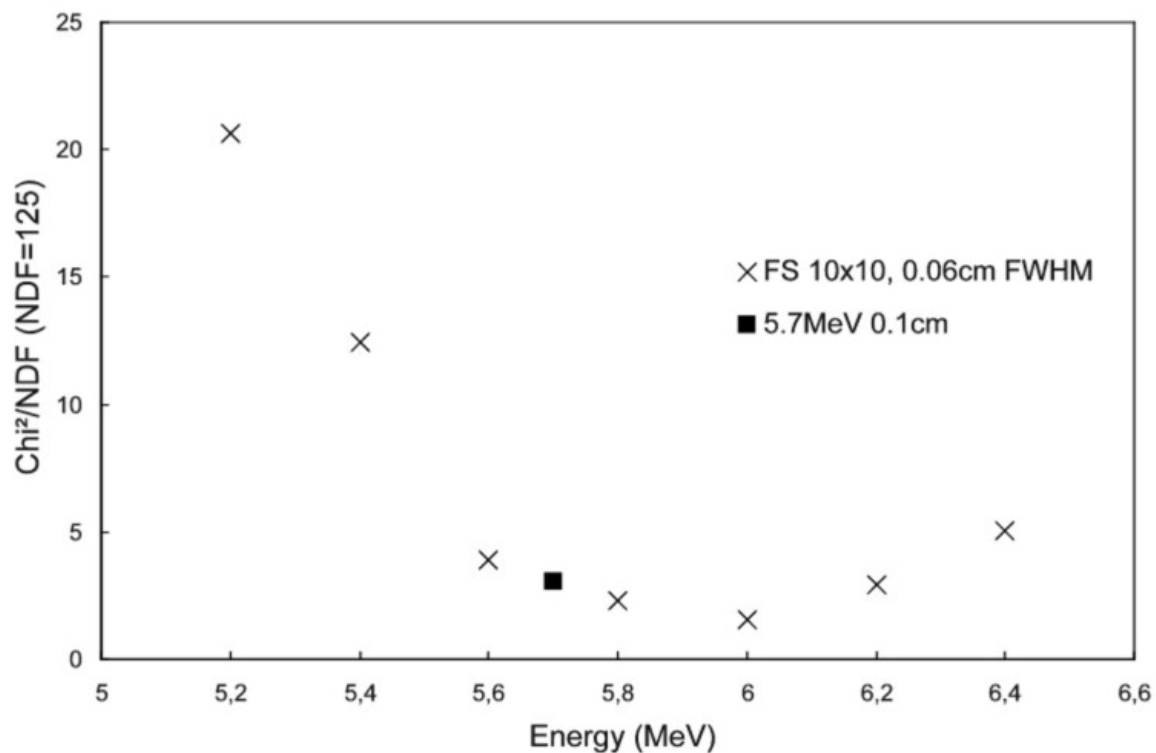
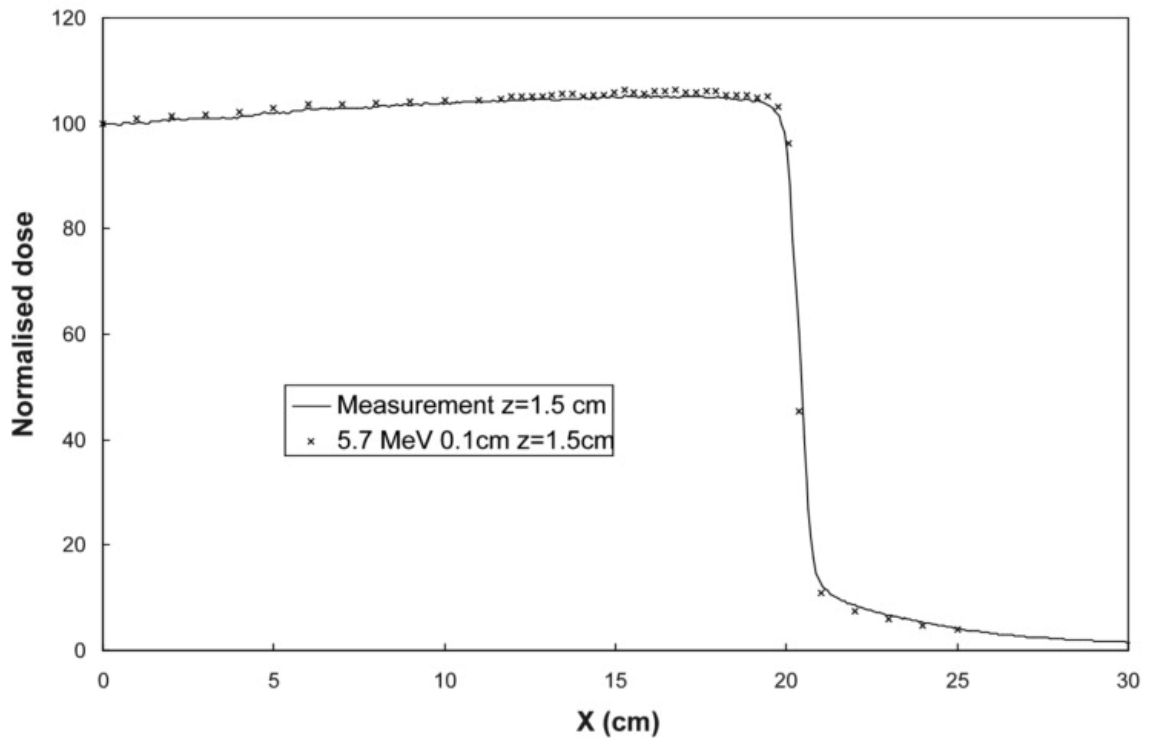
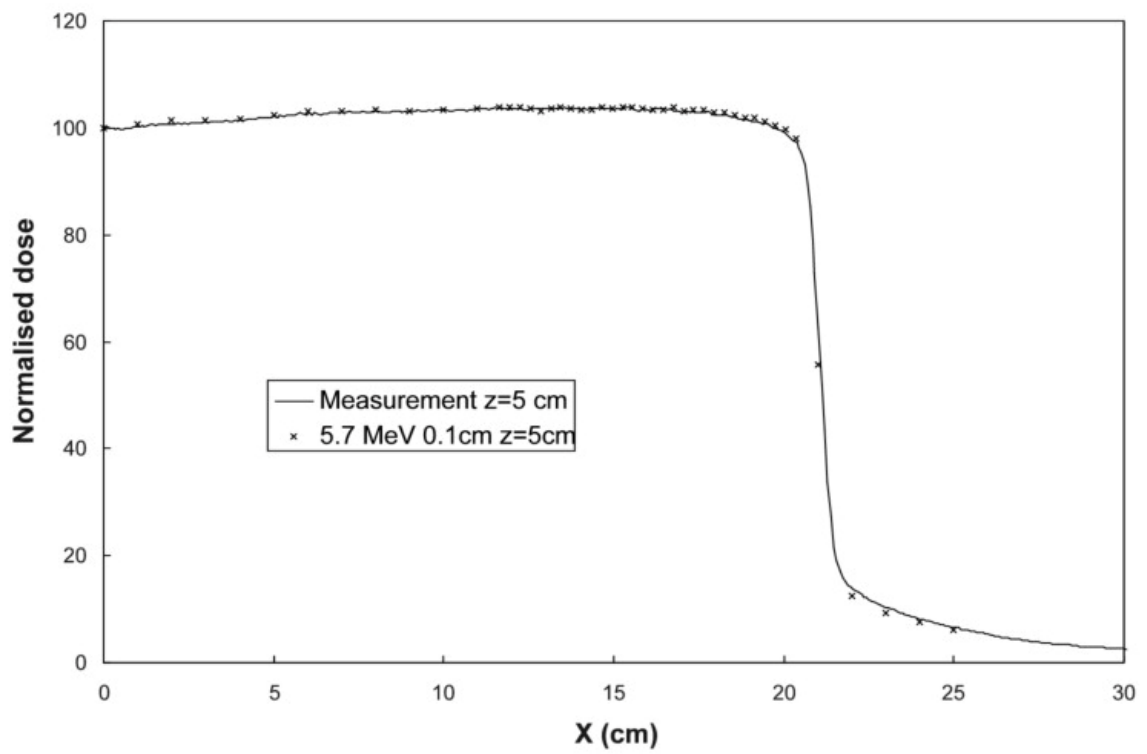


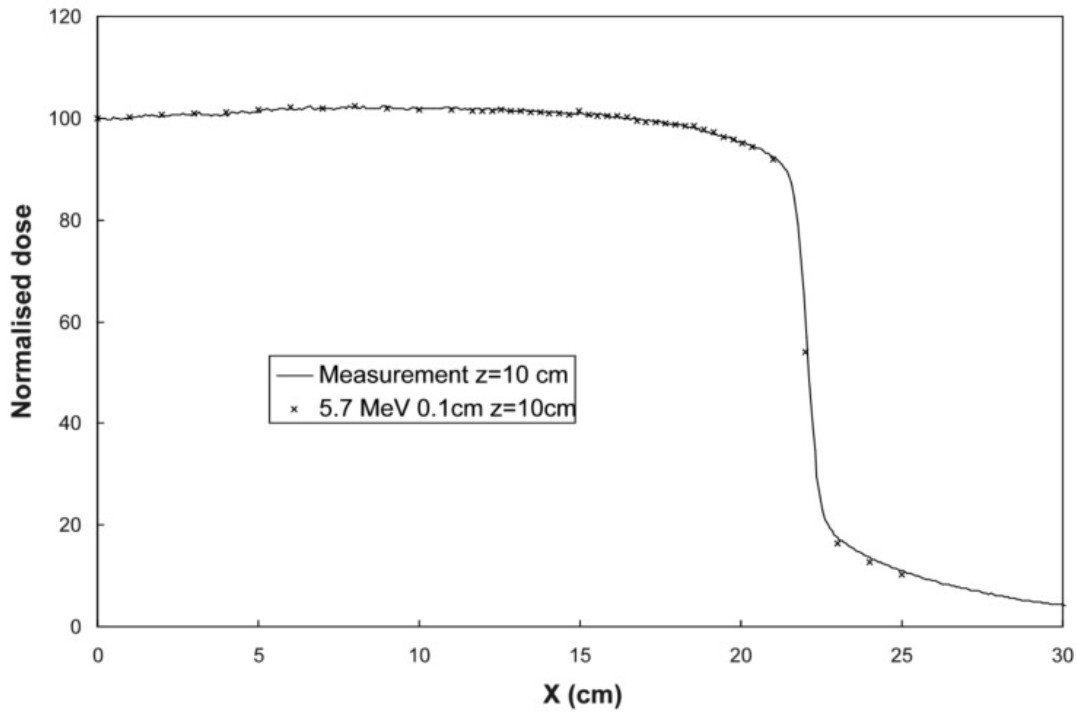
Figure 4: χ^2/NDF for depth dose curves for $10 \times 10 \text{ cm}^2$ field plotted against energy of the electrons incident on the target. Focal spot width fixed at 0.05 cm, energy varied between 5.2 and 6.4 MeV. Error bars ($2 * \sqrt{2/NDF}$) represented by the size of the data points. $NDF=125$, depths between 3 and 30 cm.



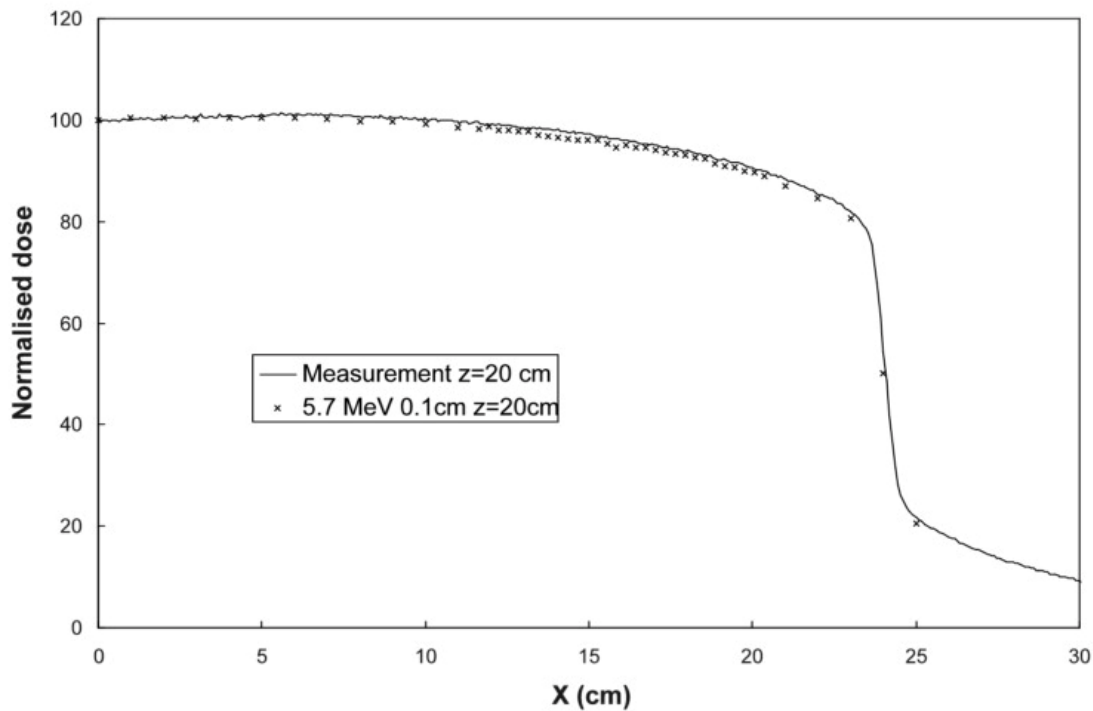
(a)



(b)

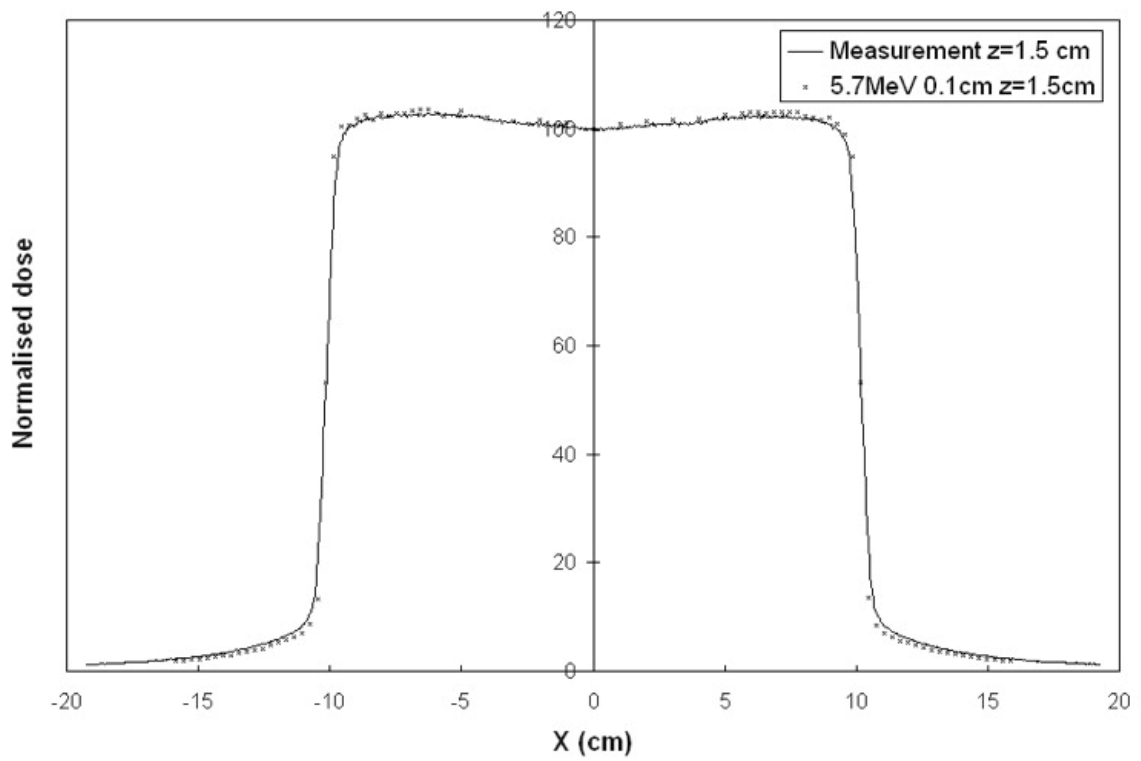


(c)

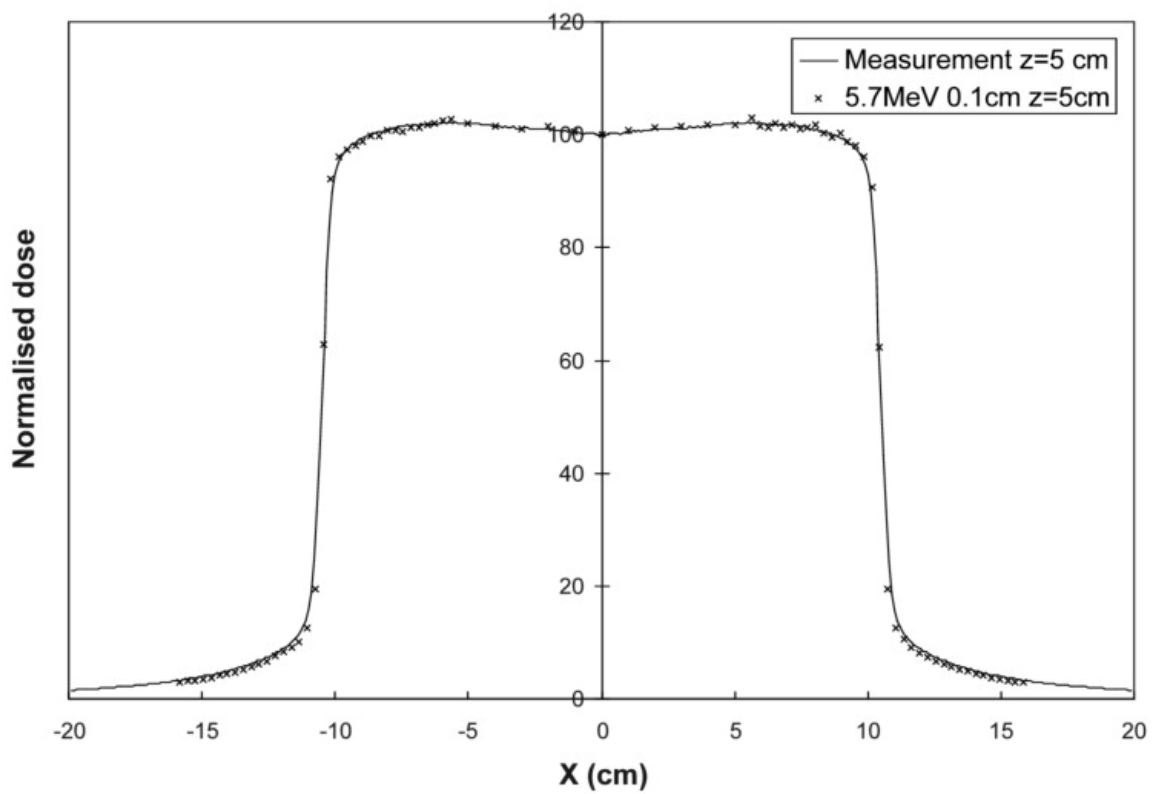


(d)

Figure 5: Dose profiles for 40x40 cm² field size in water phantom at a) 1.5 cm, b) 5 cm, c) 10 cm, d) 20 cm depth. Solid line measured (CC13) and discrete points simulated. The uncertainties of the simulated values ($\pm 1SE$) are represented by the size of the data points. Deviation between measured and simulated data is less than a) 1.5%, b) 1%, c) 1%, d) 1.8% of the dose at central axis in the range $x=0$ to 19.75 cm.



(a)



(b)

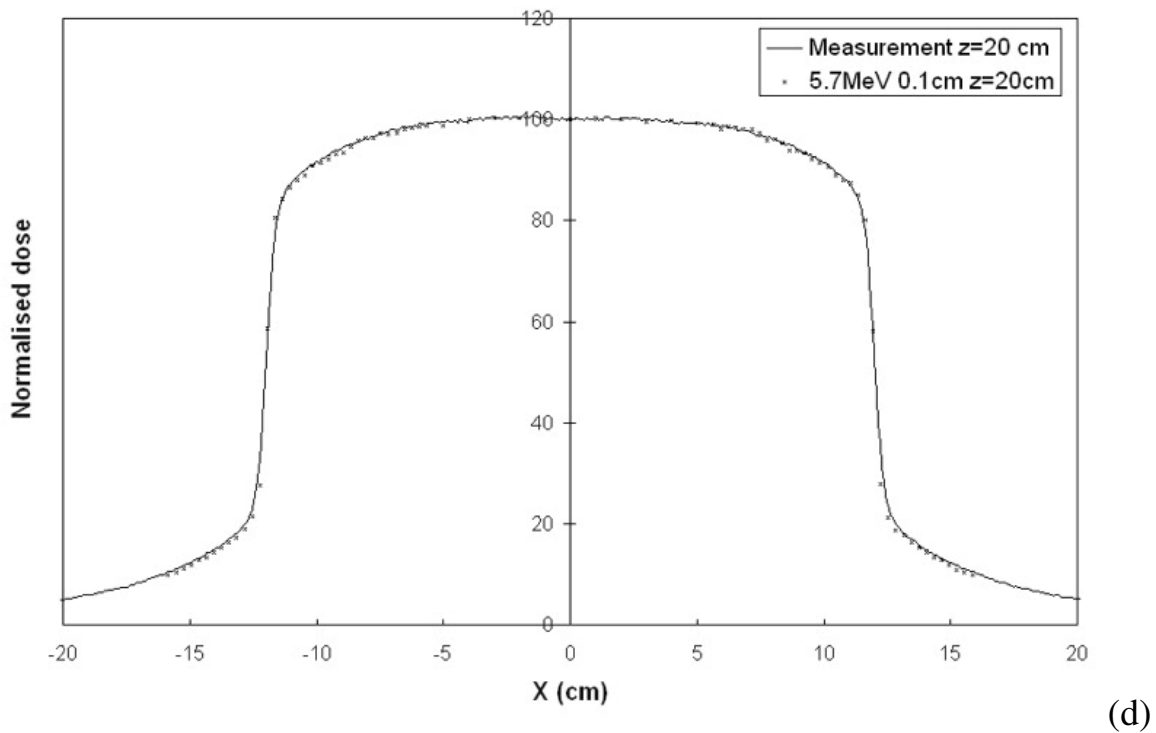
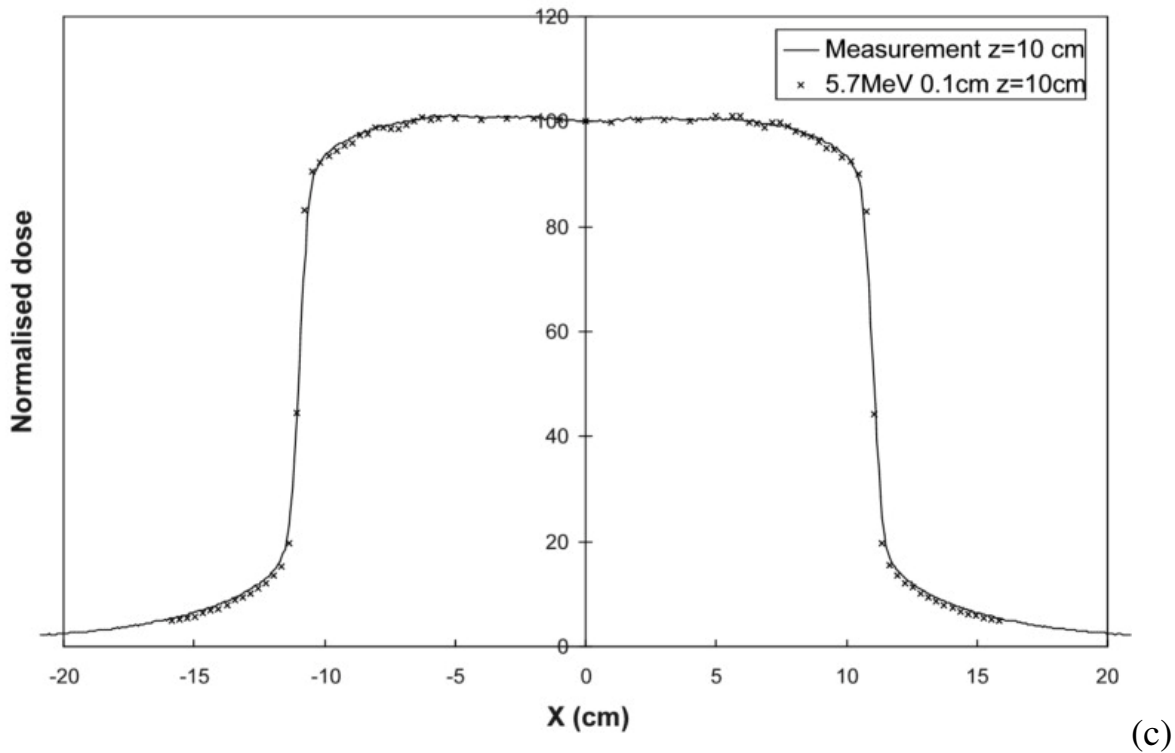
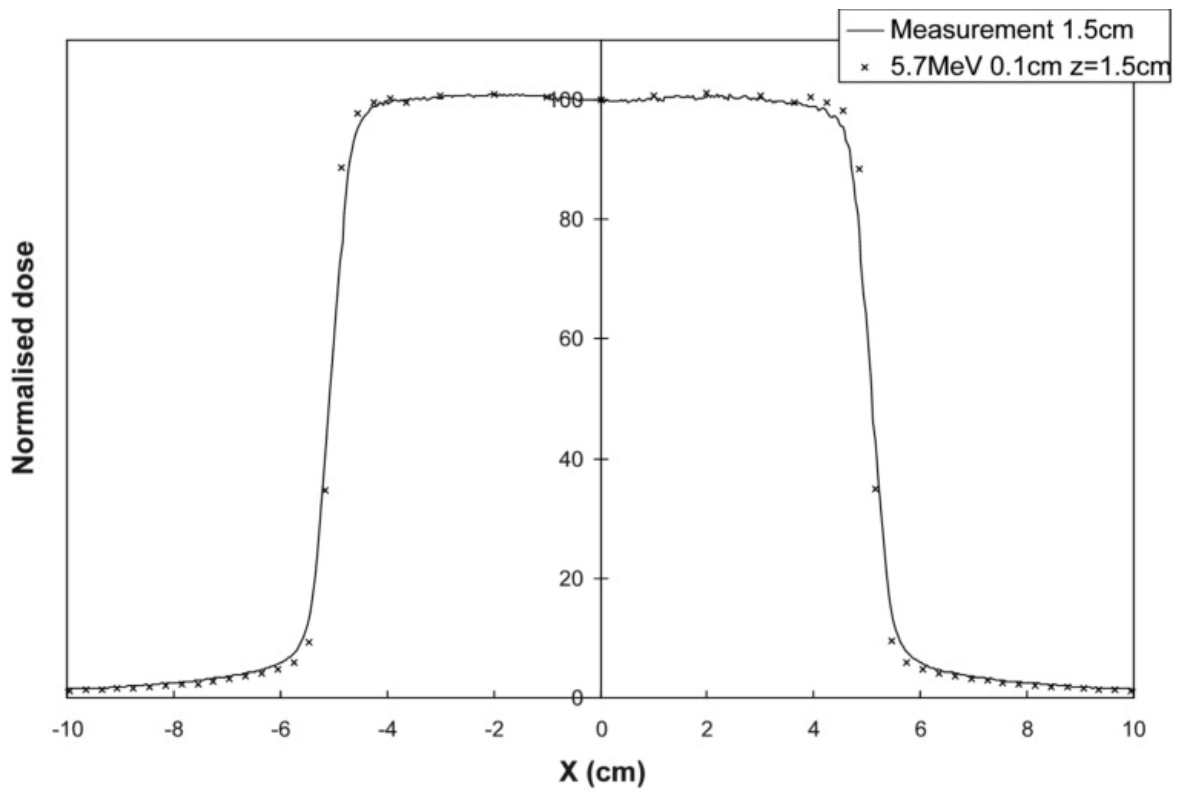
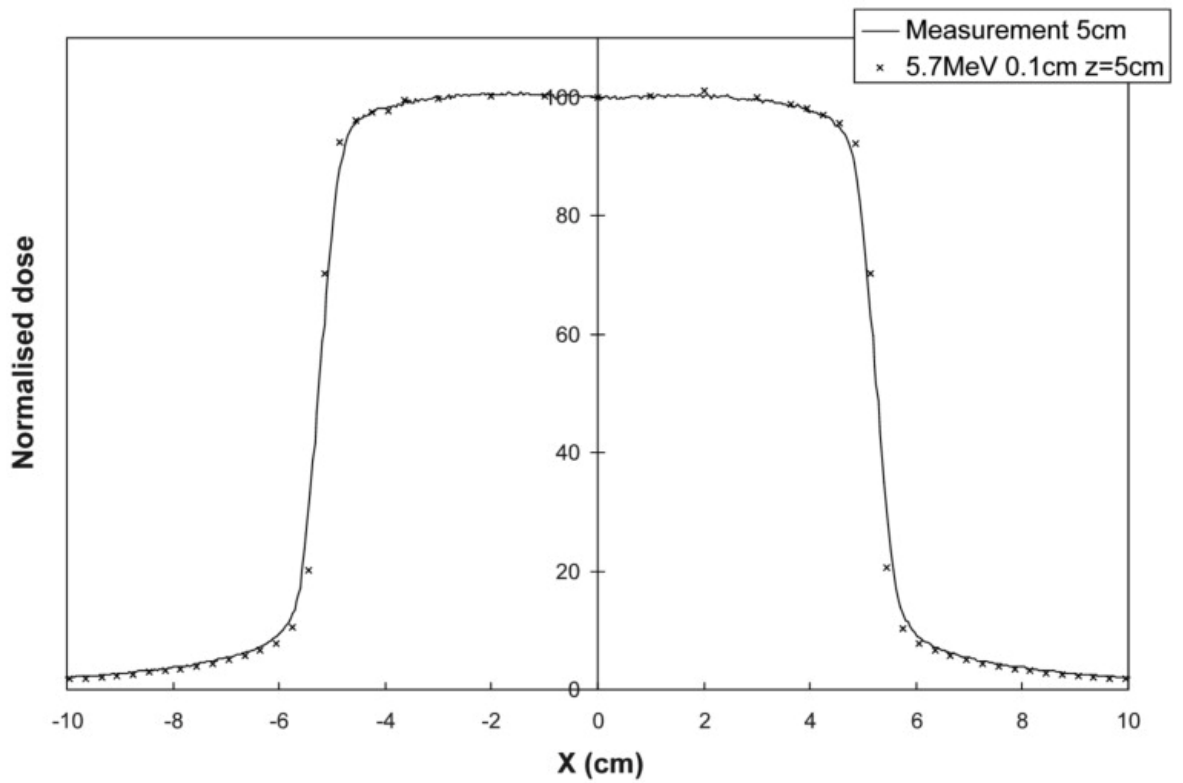


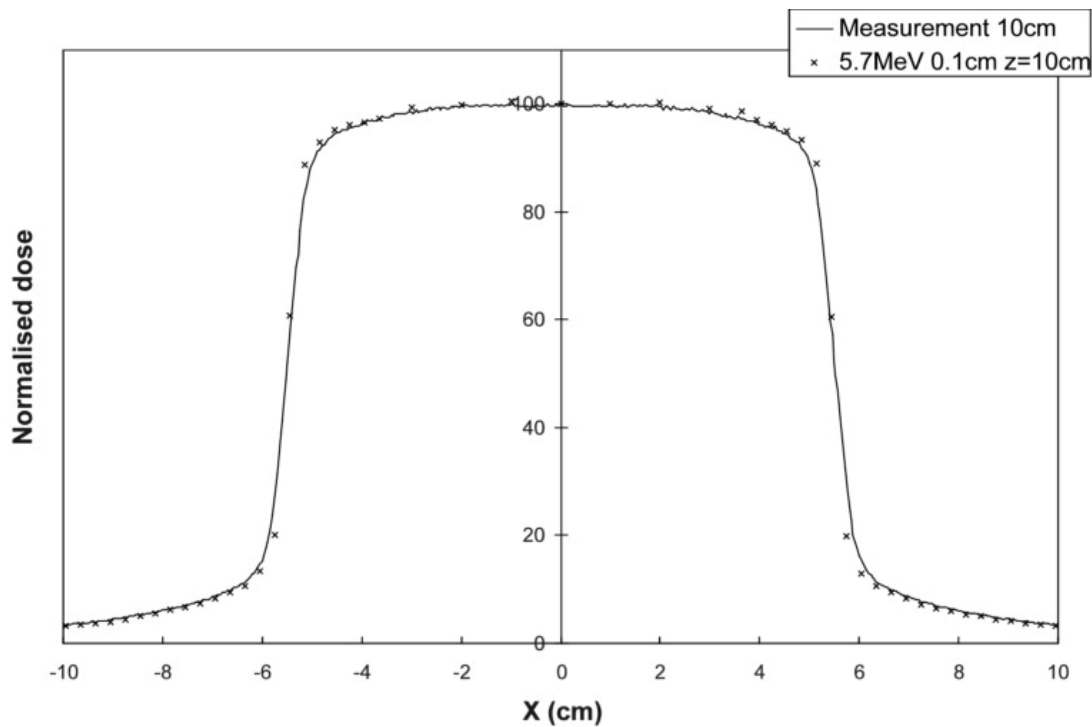
Figure 6: Dose profile for $20 \times 20 \text{ cm}^2$ field size in water phantom at a) 1.5 cm, b) 5 cm, c) 10 cm, d) 20 cm depth. Solid line measured (CC13) and discrete points simulated. The uncertainties of the simulated values ($\pm 1\text{SE}$) are represented by the size of the data points. Deviation between measured and simulated data is less than a) 1.4%, b) 1%, c) 1.3%, d) 1.2% of the dose at central axis in the range $x = -8.95$ to $x = 8.95$ cm.



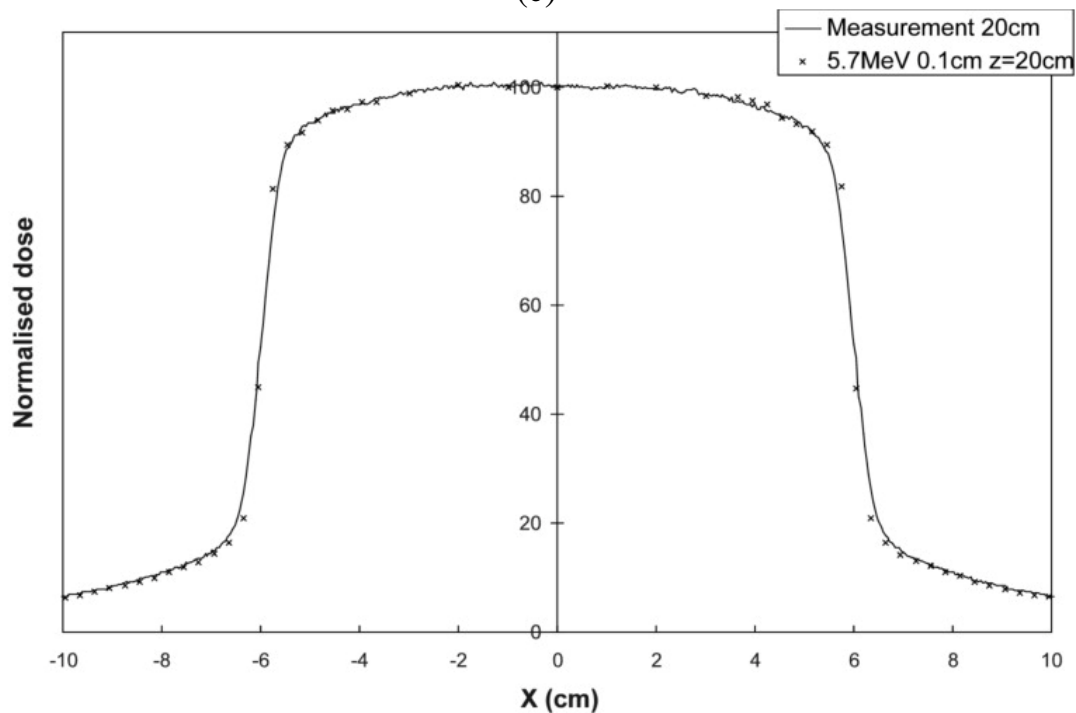
(a)



(b)

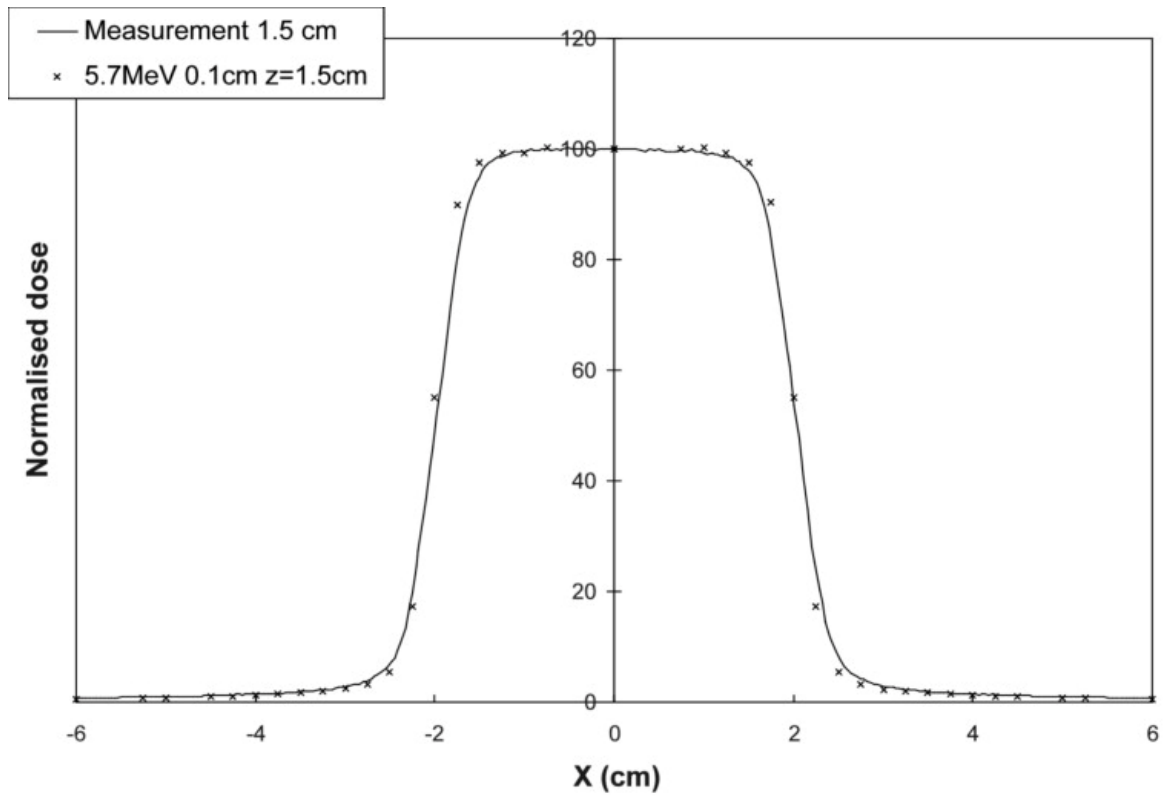


(c)

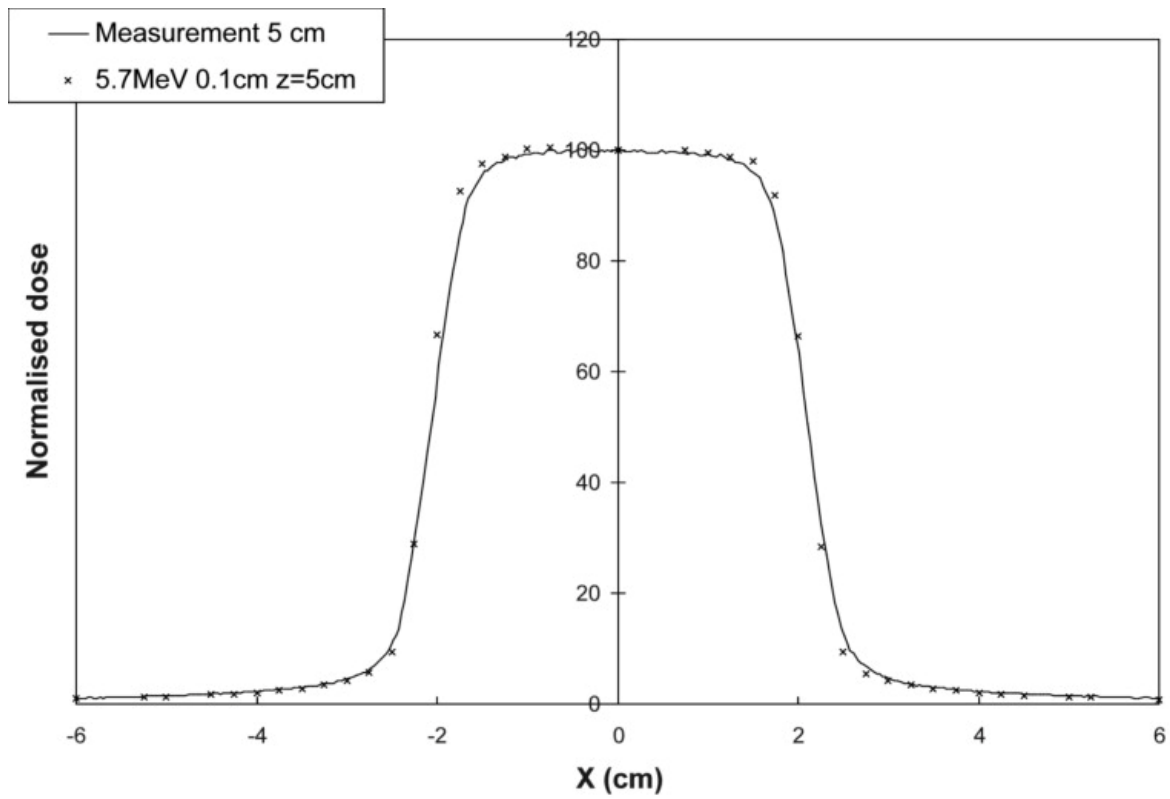


(d)

Figure 7: Dose profile for $10 \times 10 \text{ cm}^2$ field size in water phantom at a) 1.5 cm, b) 5 cm, c) 10 cm, d) 20 cm depth. Solid line measured (CC13) and discrete points simulated. The uncertainties of the simulated values ($\pm 1\text{SE}$) are represented by the size of the data points. Deviation between measured and simulated data is less than a) 1.7%, b) 1%, c) 1.5%, d) 1.2% of the dose at central axis in the range $x = -4.25$ to $x = 4.25$ cm.



(a)



(b)

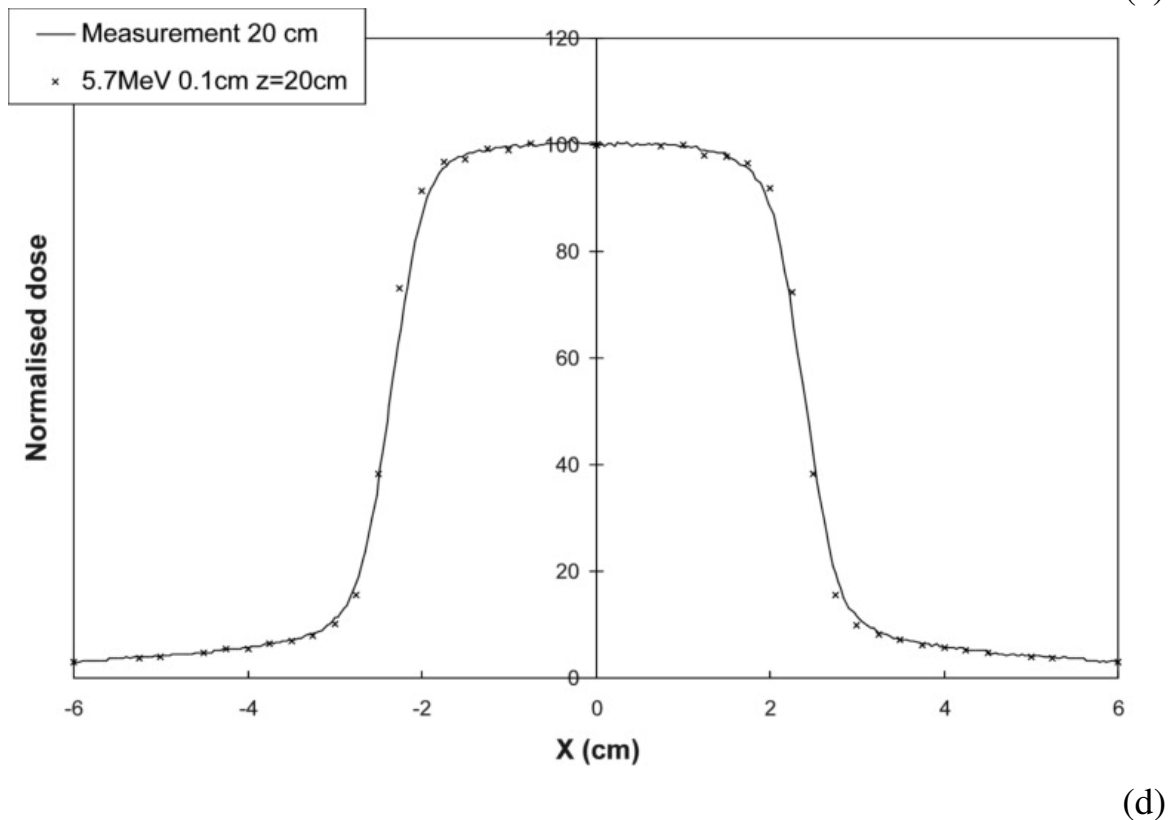
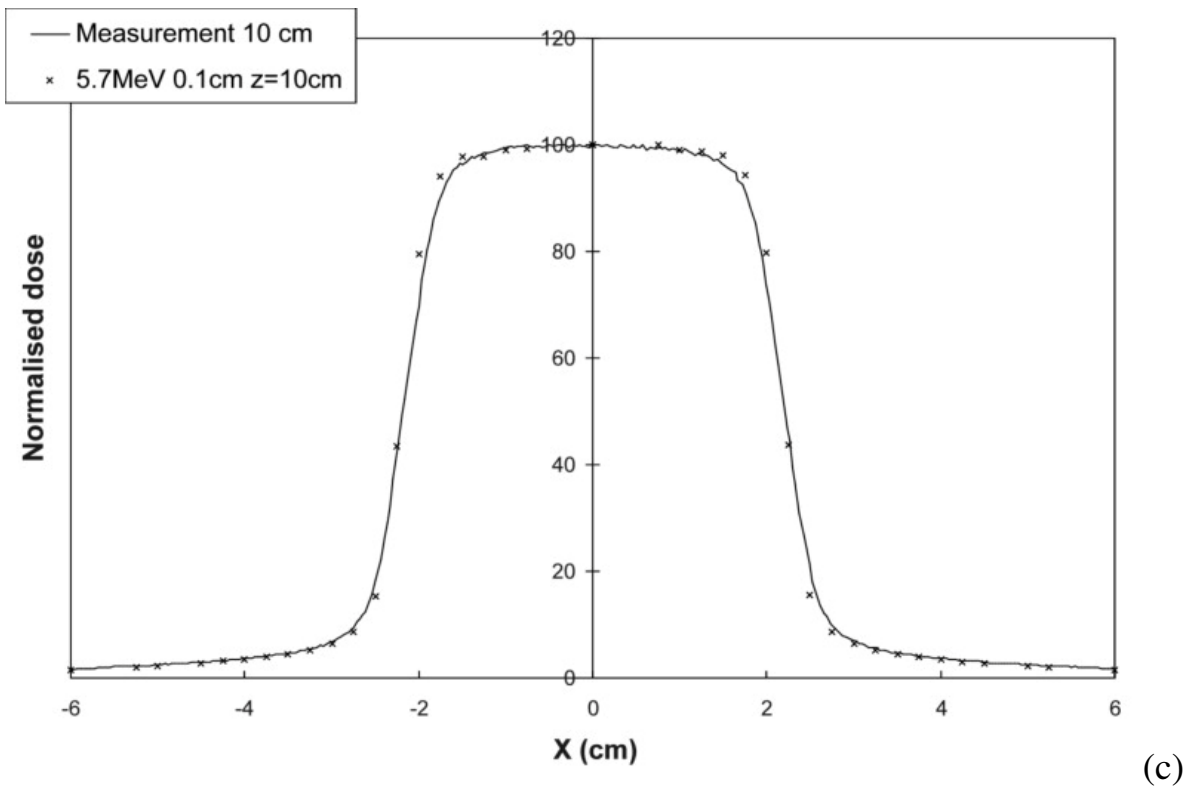
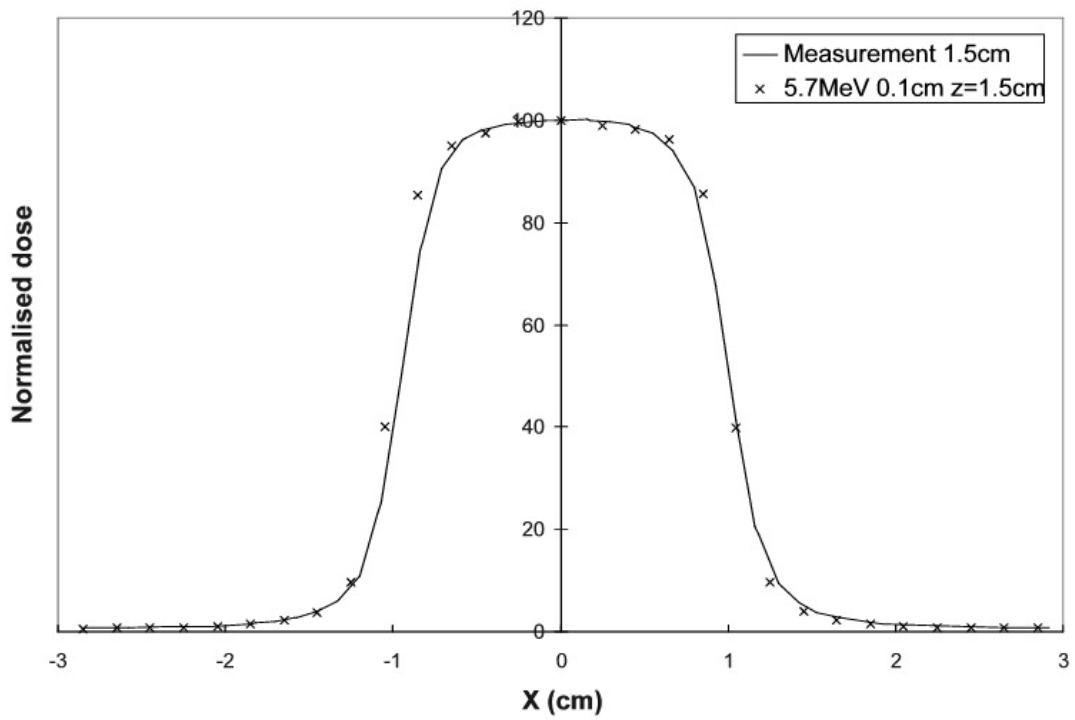
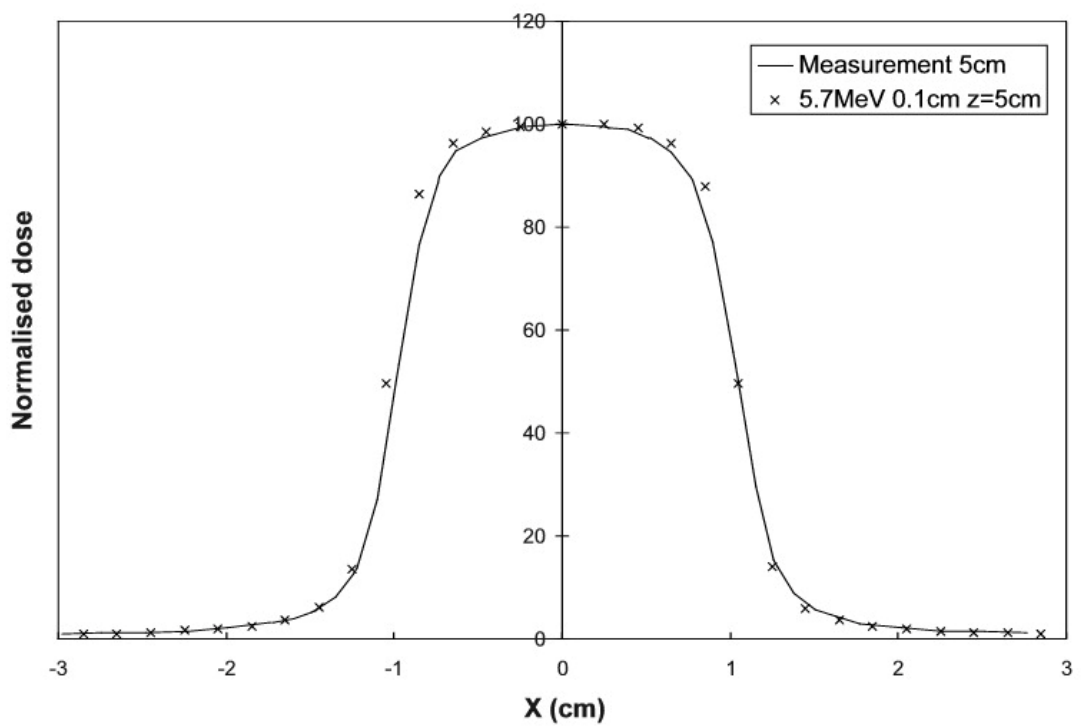


Figure 8: Dose profile for 4x4 cm² field size in water phantom at a) 1.5 cm, b) 5 cm, c) 10 cm, d) 20 cm depth. Solid line measured (CC13) and discrete points simulated. The uncertainties of the simulated values ($\pm 1SE$) are represented by the size of the data points.



(a)



(b)

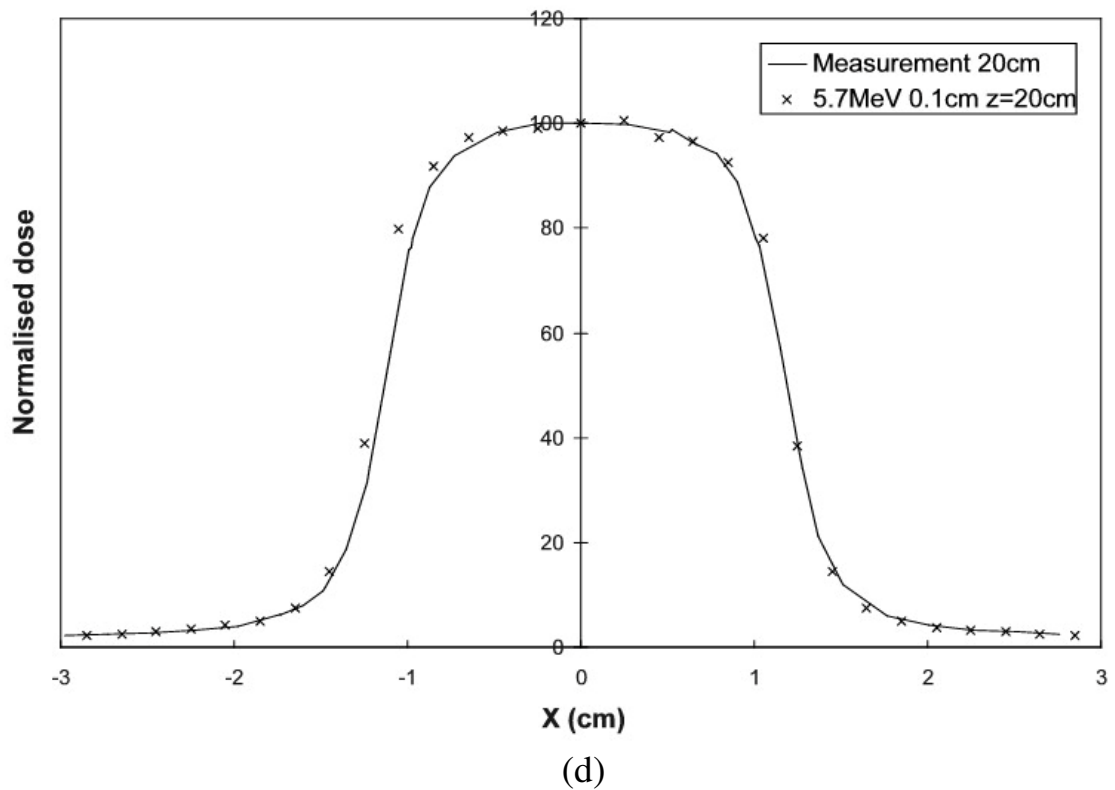
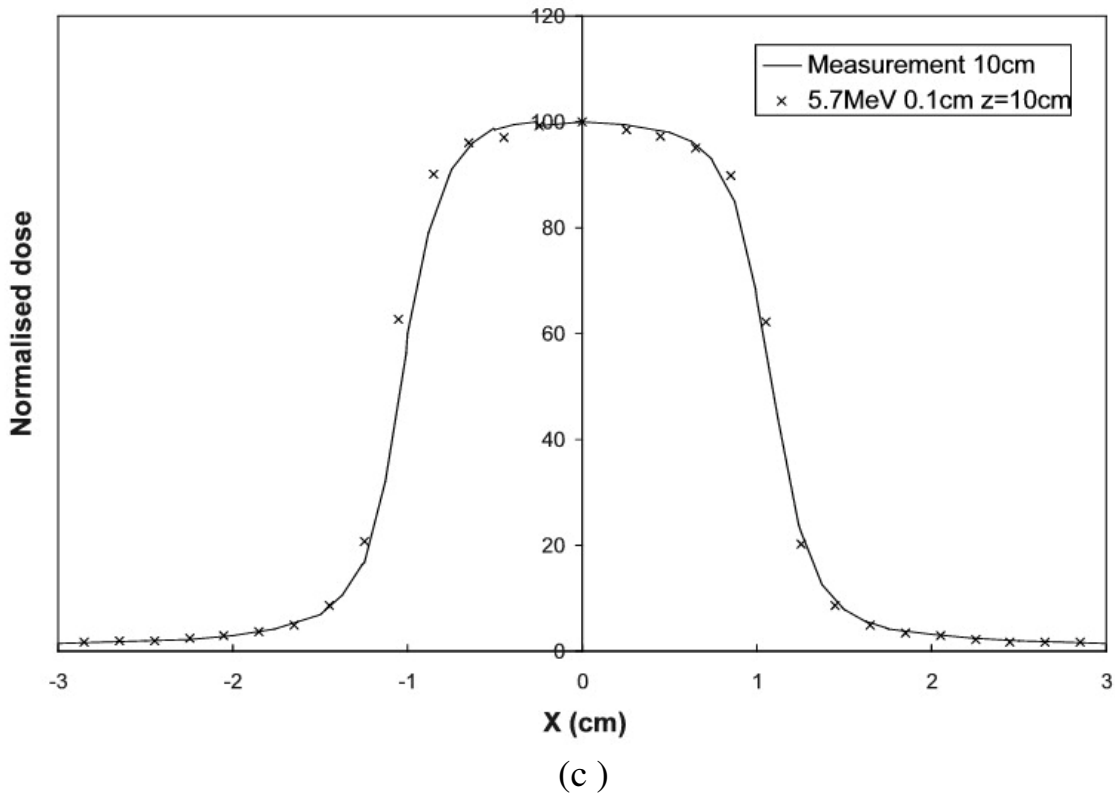
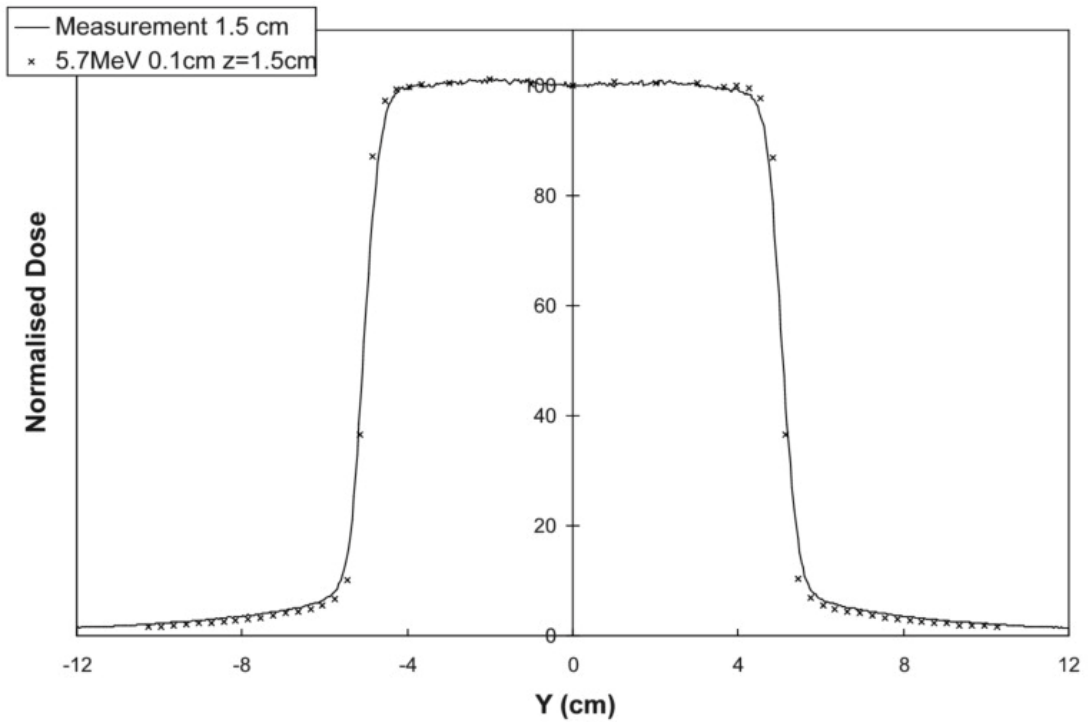


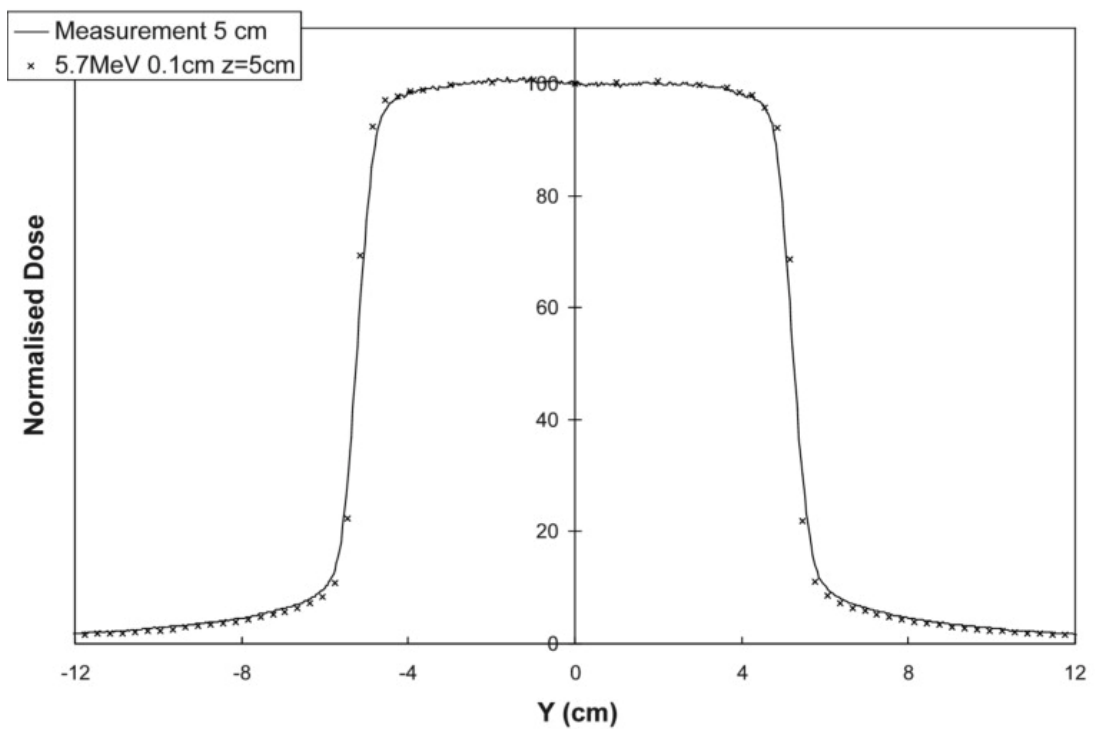
Figure 9: Dose profiles for $2 \times 2 \text{ cm}^2$ field size in water phantom at a) 1.5 cm, b) 5 cm, c) 10 cm, d) 20 cm depth. Solid line measured (pin-point, steel electrode) and discrete points simulated. The uncertainties of the simulated values ($\pm 1\text{SE}$) are represented by the size of the data points.

3.2.2 Inline dose profiles

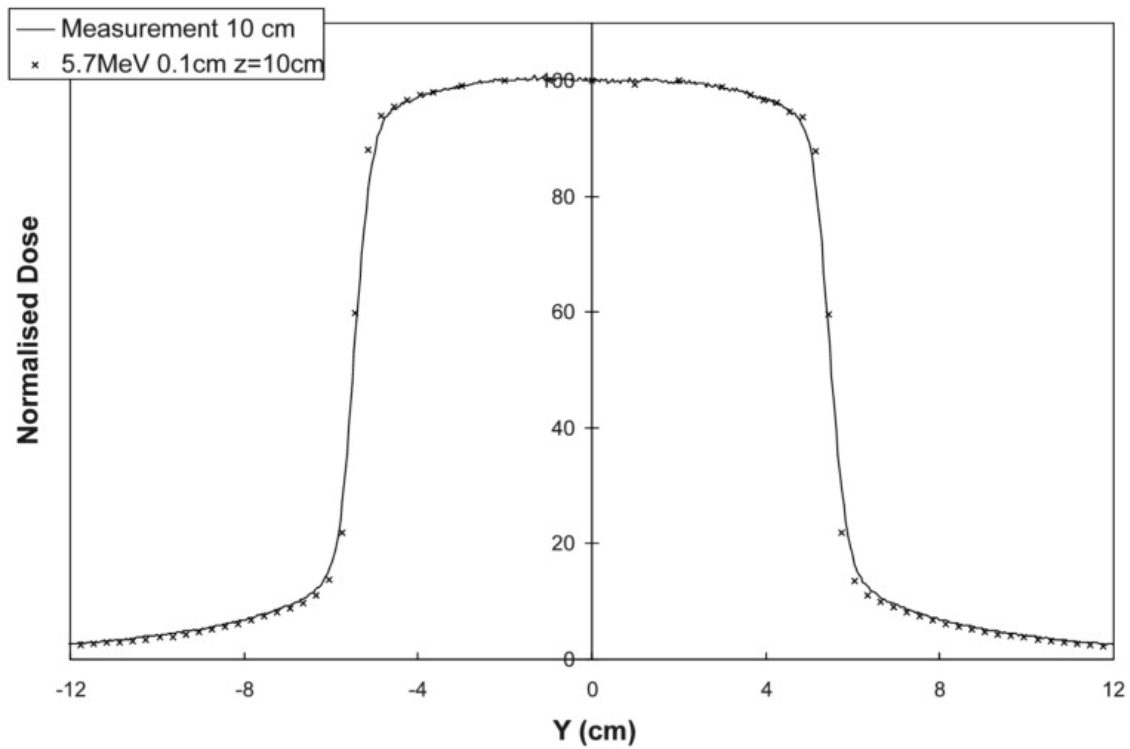
Inline dose profiles (y-direction) are analysed visually for a 10x10 cm² and 20x20 cm² field. The comparison between measured and simulated data is shown in Figs. 10 and 11. All profiles go through the central axis. The dose is normalized to the dose at the central axis for each depth.



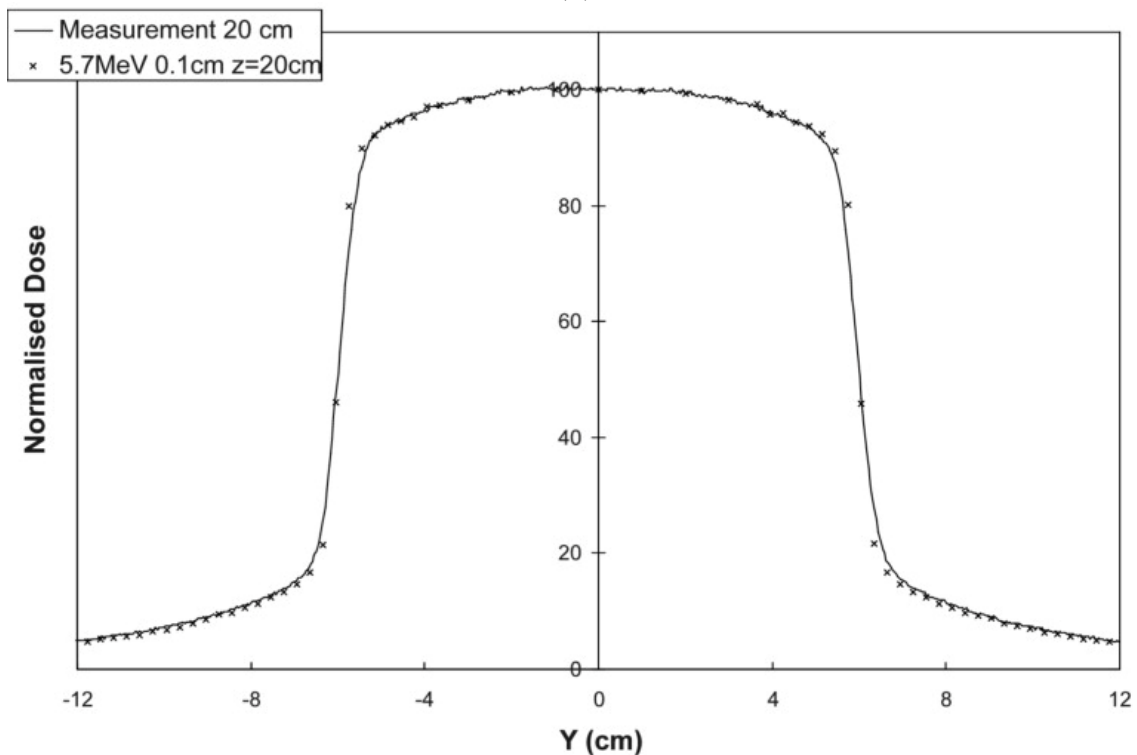
(a)



(b)

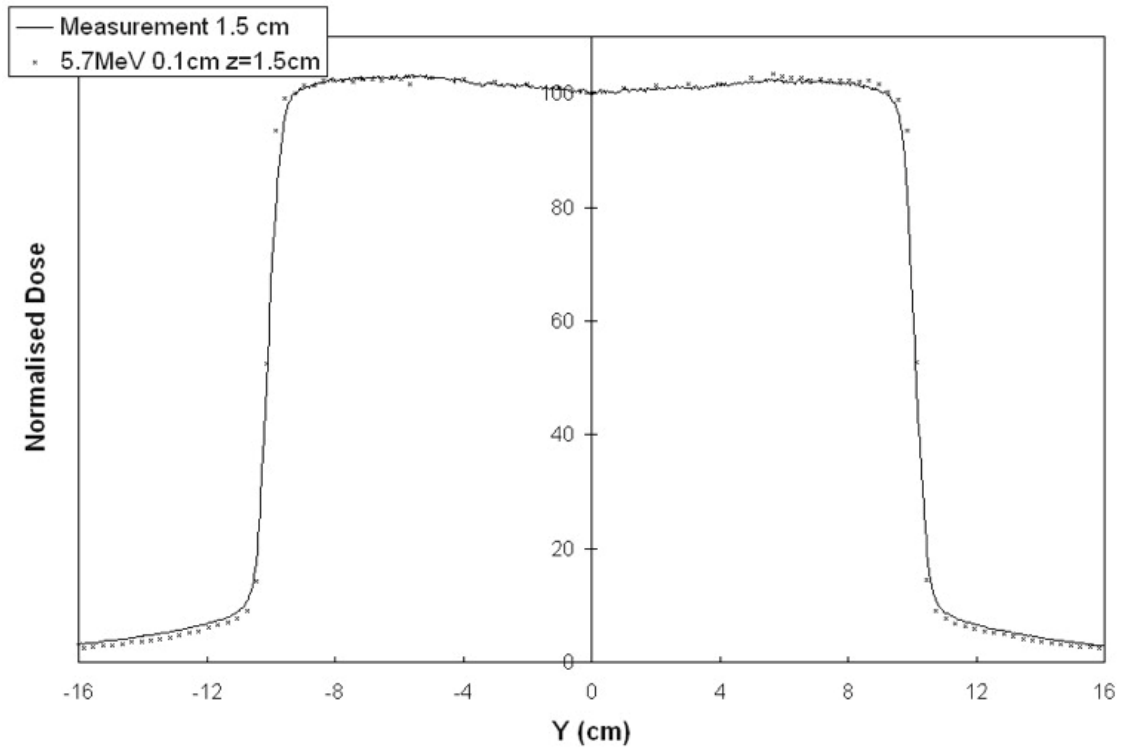


(c)

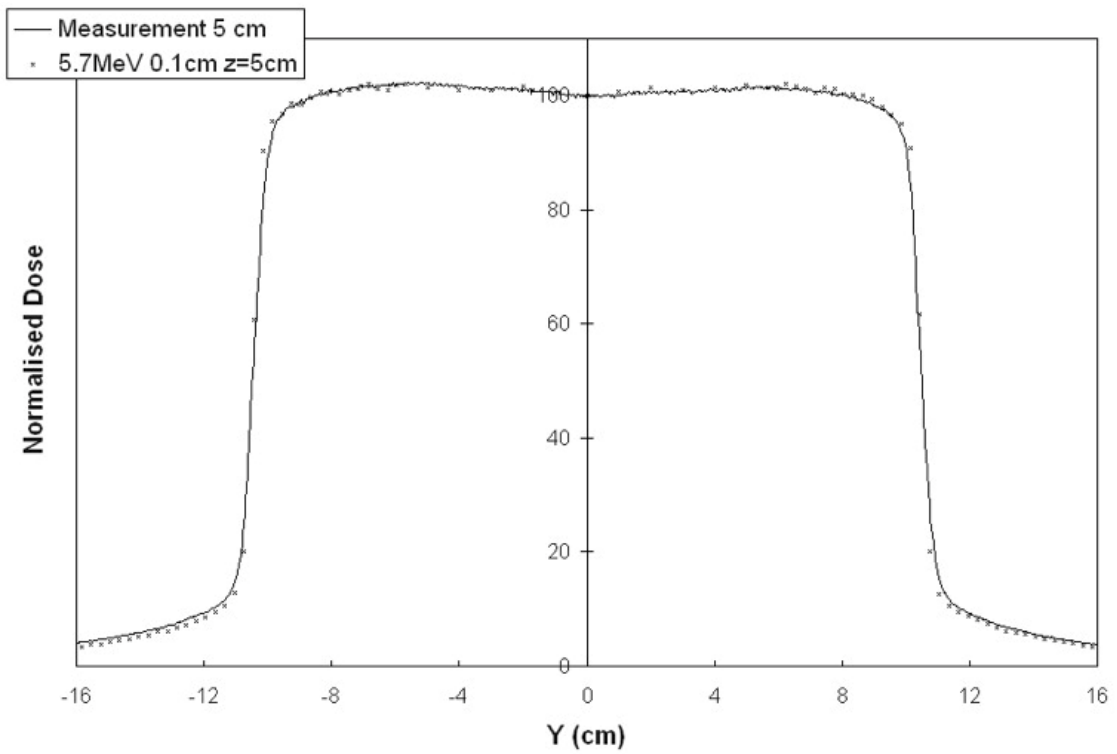


(d)

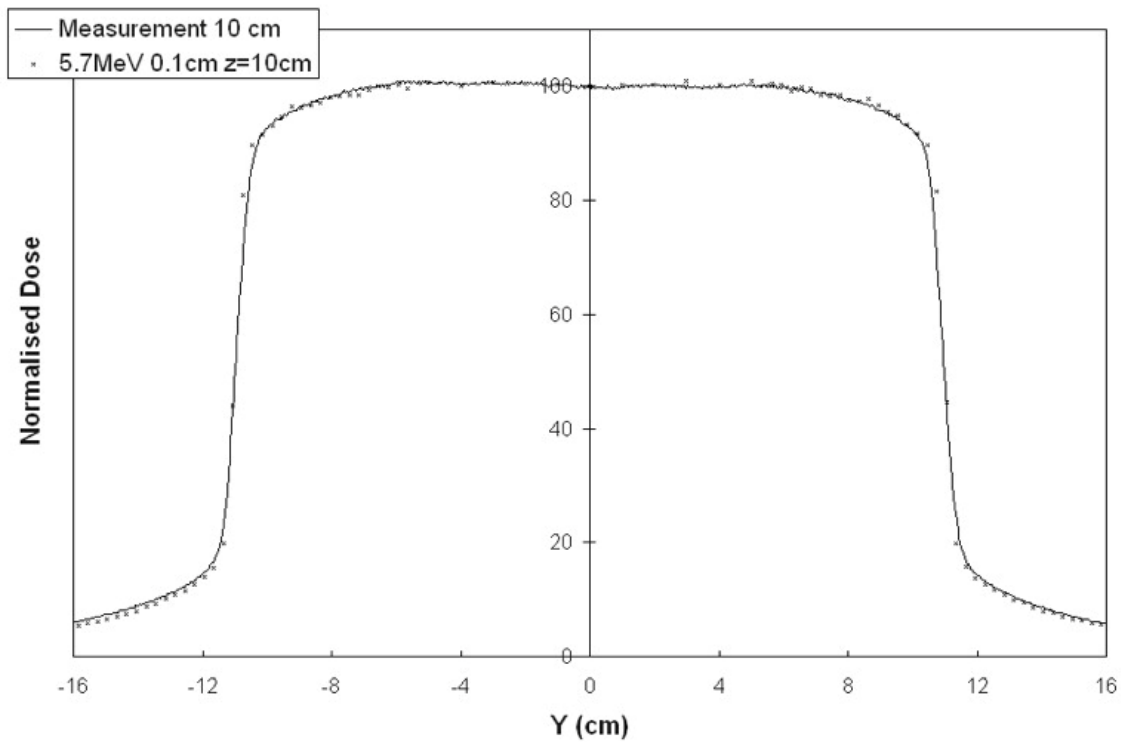
Figure 10: Y-direction dose profiles for $10 \times 10 \text{ cm}^2$ field size in water phantom at a) 1.5 cm, b) 5 cm, c) 10 cm, d) 20 cm depth. Solid line measured (CC13) and discrete points simulated. The uncertainties of the simulated values ($\pm 1\text{SE}$) are represented by the size of the data points.



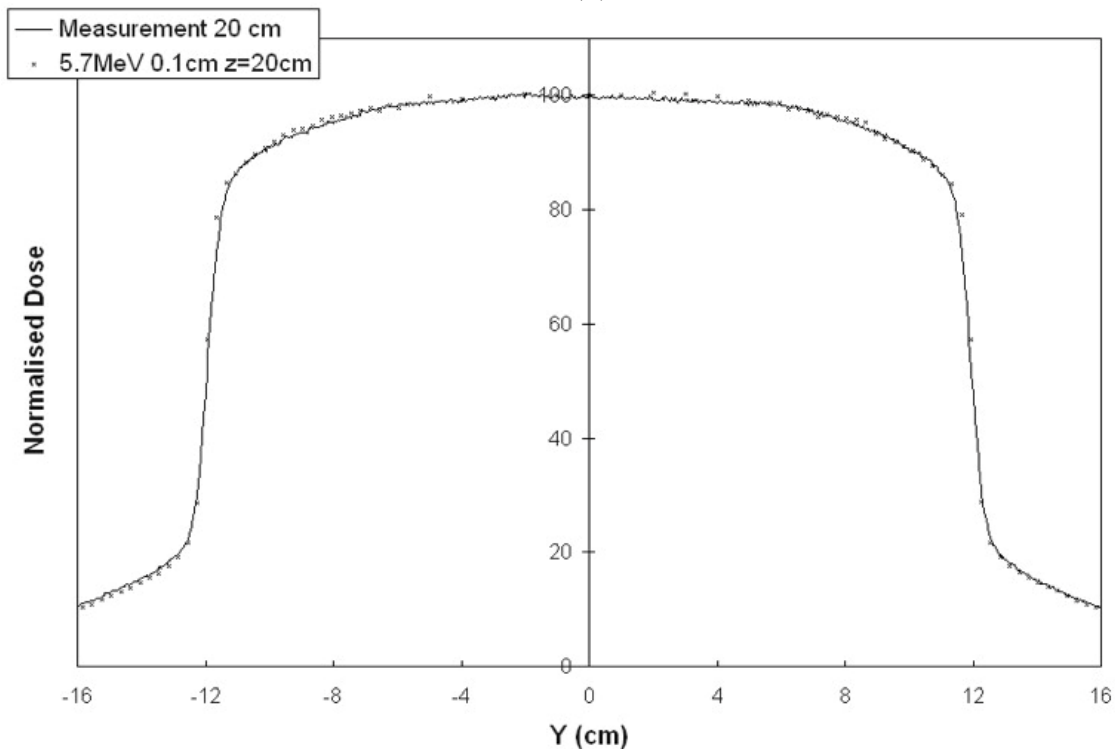
(a)



(b)



(c)



(d)

Figure 11: Y-direction dose profiles for 20x20 cm² field size in water phantom at a) 1.5 cm, b) 5 cm, c) 10 cm, d) 20 cm depth. Solid line measured (CC13) and discrete points simulated. The uncertainty of the simulated values ($\pm 1SE$) is represented by the size of the data points.

3.2.3 Depth Dose Curves

The depth dose verification curves for the optimum parameter set [5.7 MeV 0.1 cm] are shown in Figs. 12 to 16. The dose is normalised (100%) to dose value at 10 cm depth, taken from a fifth grade polynomial fitted to the simulated data points between the depths 5 and 20 cm. In all cases the simulated data points do not deviate more than 1% (of the maximum dose) from the measured data between the depth of dose max and 25 cm, except for in the case of the 2x2 cm² field (the extreme regarding small field size), in which the deviation at dose maximum is 2.5% of the dose at dose maximum.

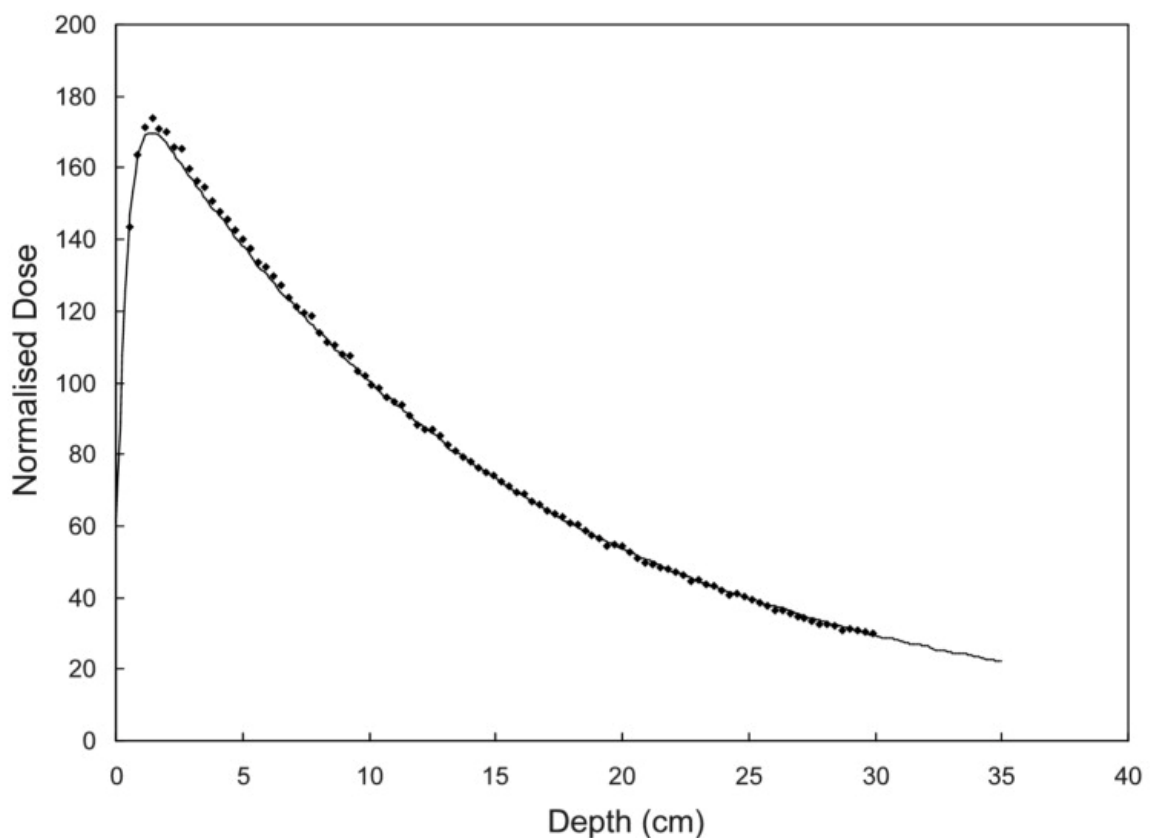


Figure 12: Depth dose curve for 2x2 cm² field size in water phantom. Solid line - measured data (pin-point ionization chamber, steel electrode) and discrete points - simulated data. The uncertainties of the simulated values ($\pm 1SE$) are represented by the size of the data points.

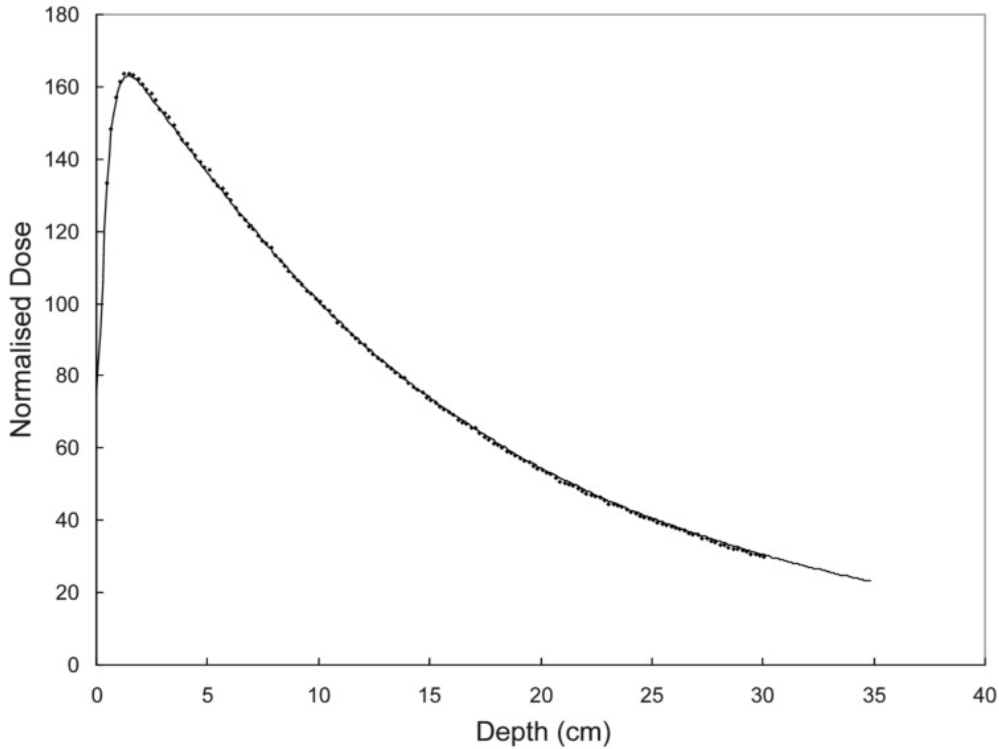


Figure 13: Depth dose curve for 4x4 cm² field size in water phantom. Solid line measured (CC13) and discrete points simulated. The uncertainties of the simulated values ($\pm 1SE$) are represented by the size of the data points.

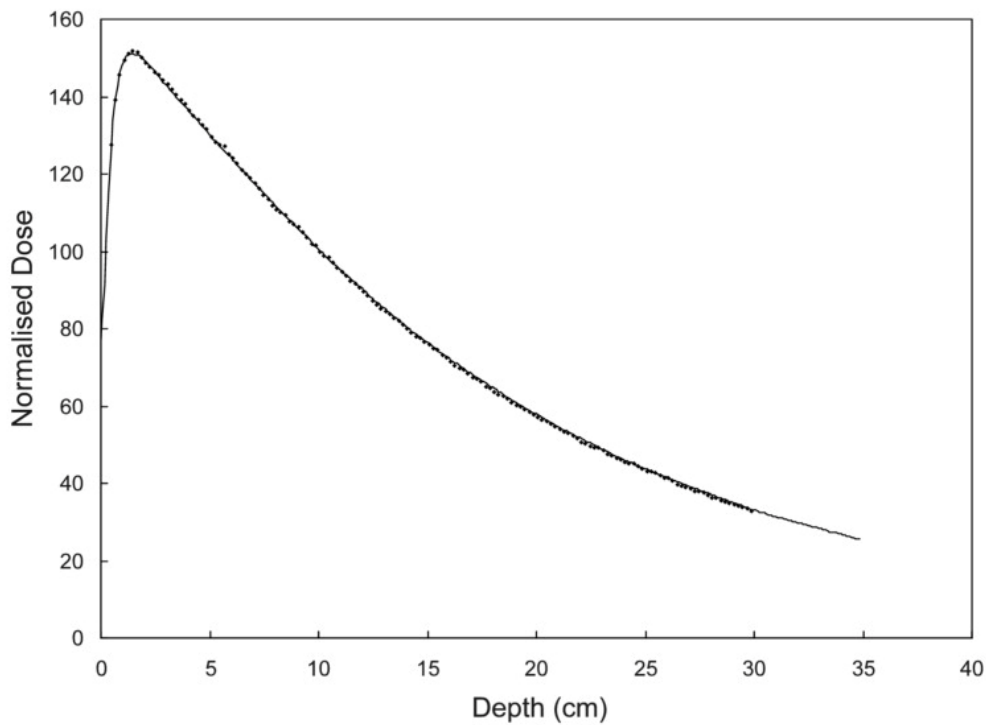


Figure 14: Depth dose curve for 10x10 cm² field size in water phantom. Solid line measured (CC13) and discrete points simulated. The uncertainties of the simulated values ($\pm 1SE$) are represented by the size of the data points.

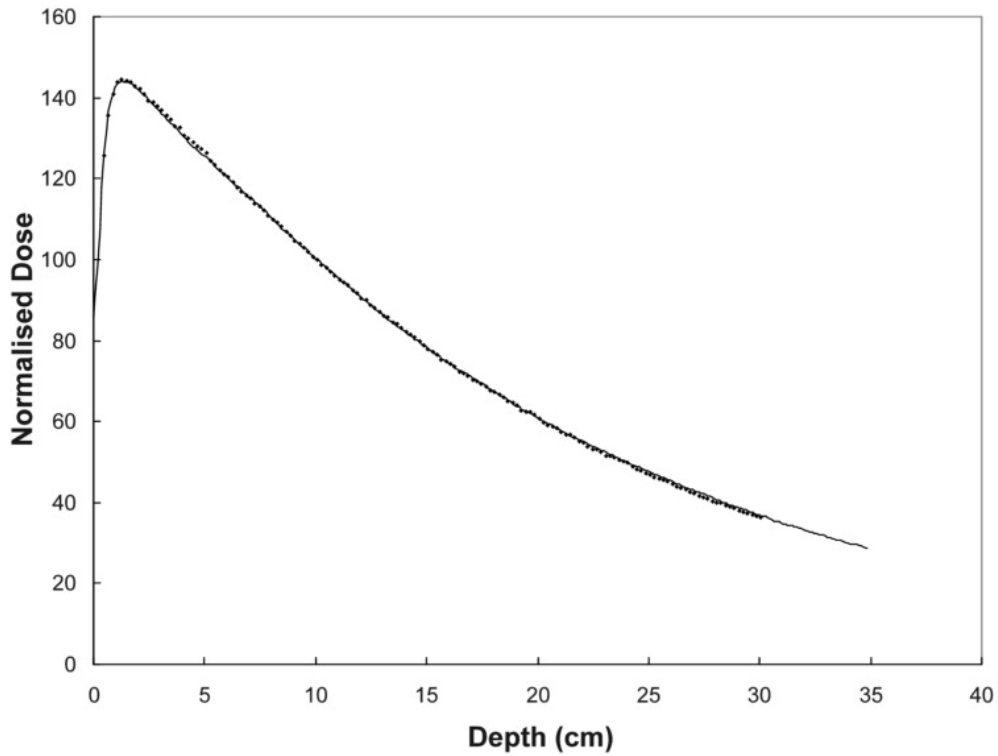


Figure 15: Depth dose curve for 20x20 cm² field size in water phantom. Solid line measured (CC13) and discrete points simulated. The uncertainties of the simulated values ($\pm 1SE$) are represented by the size of the data points.

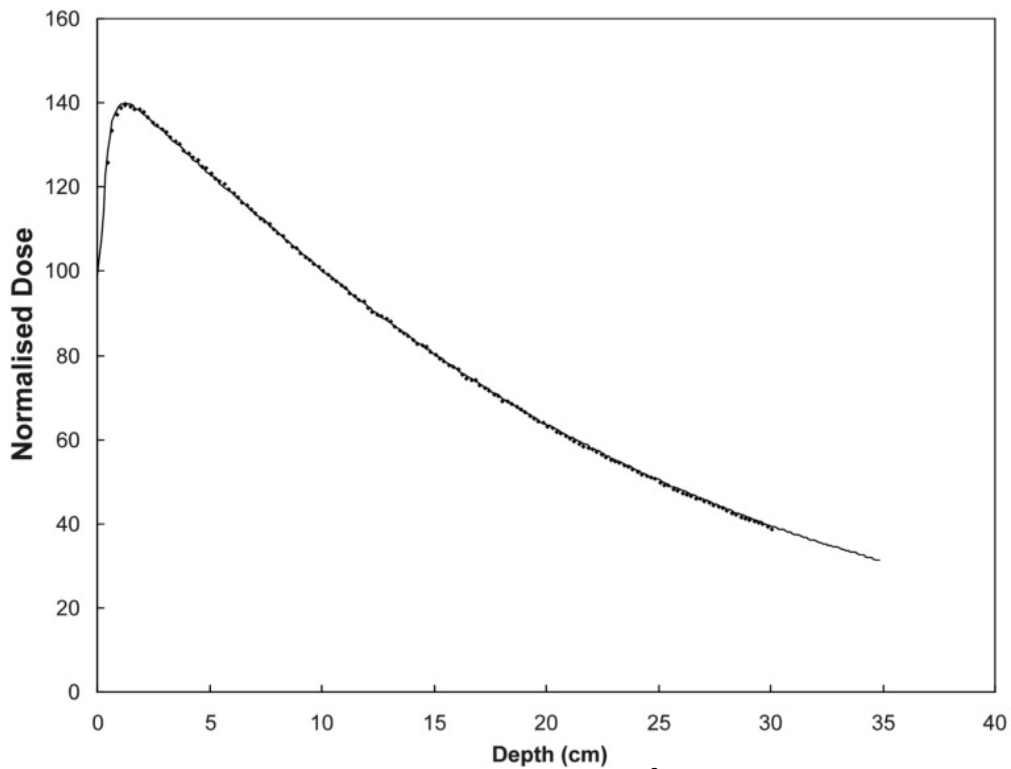


Figure 16: Depth dose curve for 40x40 cm² field size in water phantom. Solid line measured (CC13) and discrete points simulated. The uncertainties of the simulated values ($\pm 1SE$) are represented by the size of the data points.

3.2.4 Output Factors

The output factors obtained are presented in Table 3 and 4. Factors based on dose values taken from polynomial fit of the simulated depth dose curve are presented in Table 3. The factors based on voxel doses are presented in Table 4. The measured output factors are presented as well for comparison. The differences between measured and calculated values normalised to the measured value are shown in column 3. In Table 4 the uncertainty of the normalised difference between measured and simulated output factors is presented. It is seen from Table 3 that the simulated output factors do not deviate more than 2.3% from the measured output factors. For field sizes smaller than 20x20 cm² the deviation is less than 1.65%.

Table 3: Results from output-factor calculations based on doses from polynomial fits of depth dose curves. First column specifies field size ratio (symmetrical fields). Column 1: measured output factors. Column 2: simulated output factors. Column 3: Difference between simulated and measured ratios in percent of the measured ratio.

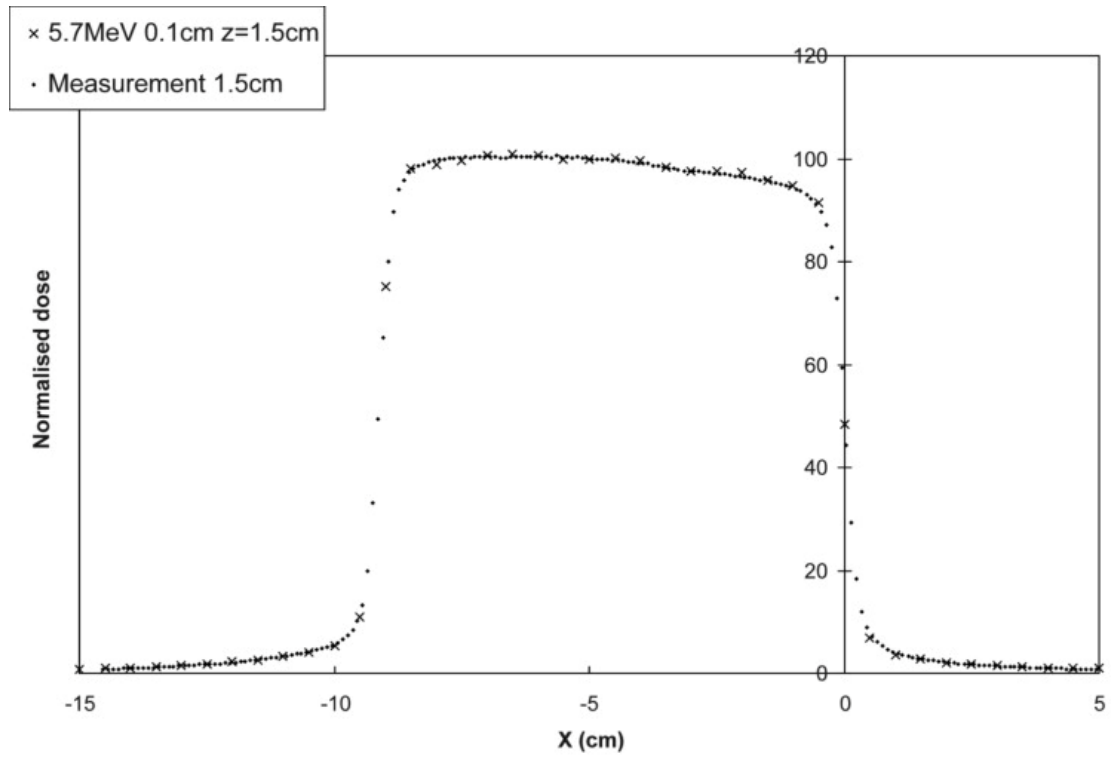
	1	2	3
(cm ² /cm ²)	Meas OF	Sim OF	[sim-meas]/meas*100
2x2/10x10	0.79	0.80	0.16
4x4/10x10	0.86	0.87	0.93
10x10/10x10	1	1	0
20x20/10x10	1.10	1.08	-1.65
40x40/10x10	1.19	1.16	-2.30
x4y20/10x10	0.94	0.94	-0.02
x20y4/10x10	0.92	0.93	0.59

Table 4: Table of results from output-factor calculations based on doses taken from single voxels. First column specifies field size ratio (symmetrical fields). Column 1: measured output factors. Column 2: simulated output factors. Column 3: Difference between simulated and measured ratios in percent of the measured ratio. Column 4: Uncertainty (expressed as the standard error) in the quantity given in column 3.

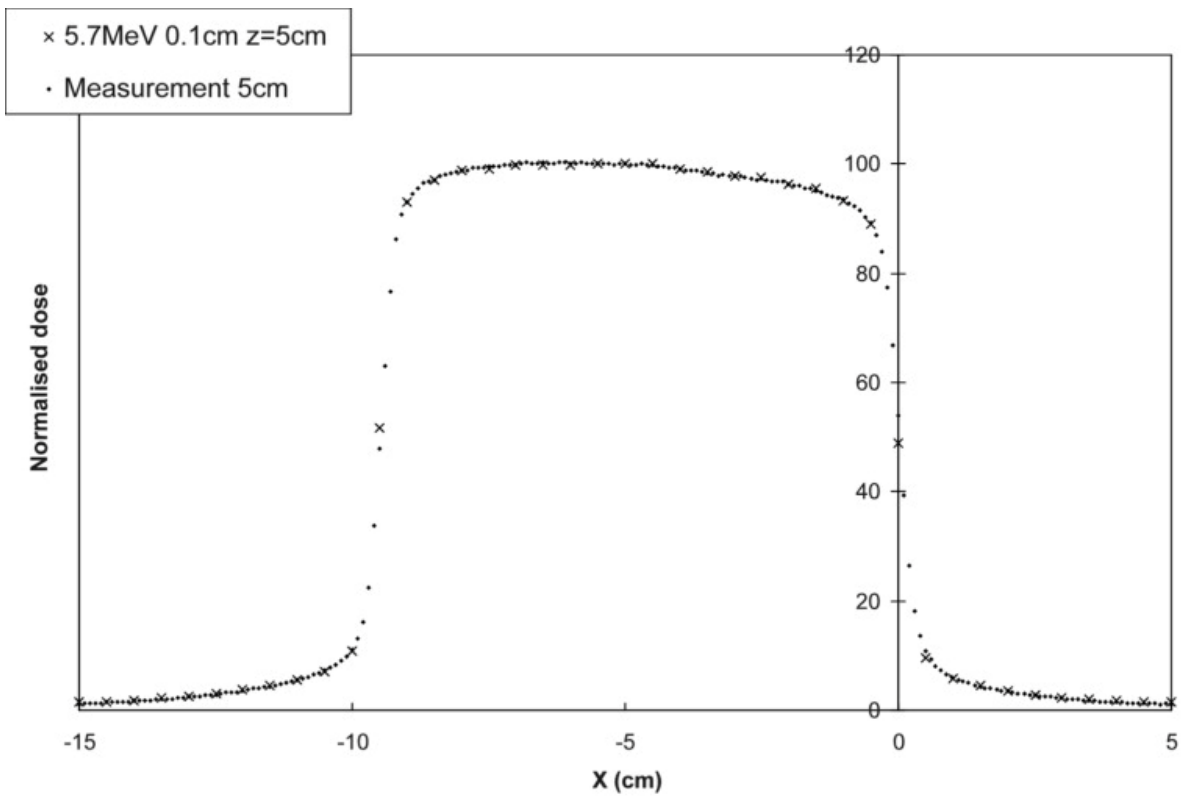
	1	2	3	4
(cm ² /cm ²)	Meas OF	Sim OF (voxel)	[sim-meas]/meas*100	SE of column 3
2x2/10x10	0.79	0.79	-0.32	1.42
4x4/10x10	0.86	0.87	1.37	0.59
10x10/10x10	1	1	0	-
20x20/10x10	1.10	1.10	-0.60	0.56
40x40/10x10	1.19	1.16	-2.17	0.54
x4y20/10x10	0.94	0.94	-0.02	0.53
x20y4/10x10	0.92	0.93	0.41	0.54

3.2.5 Crossline dose Profiles - asymmetric and rectangular fields

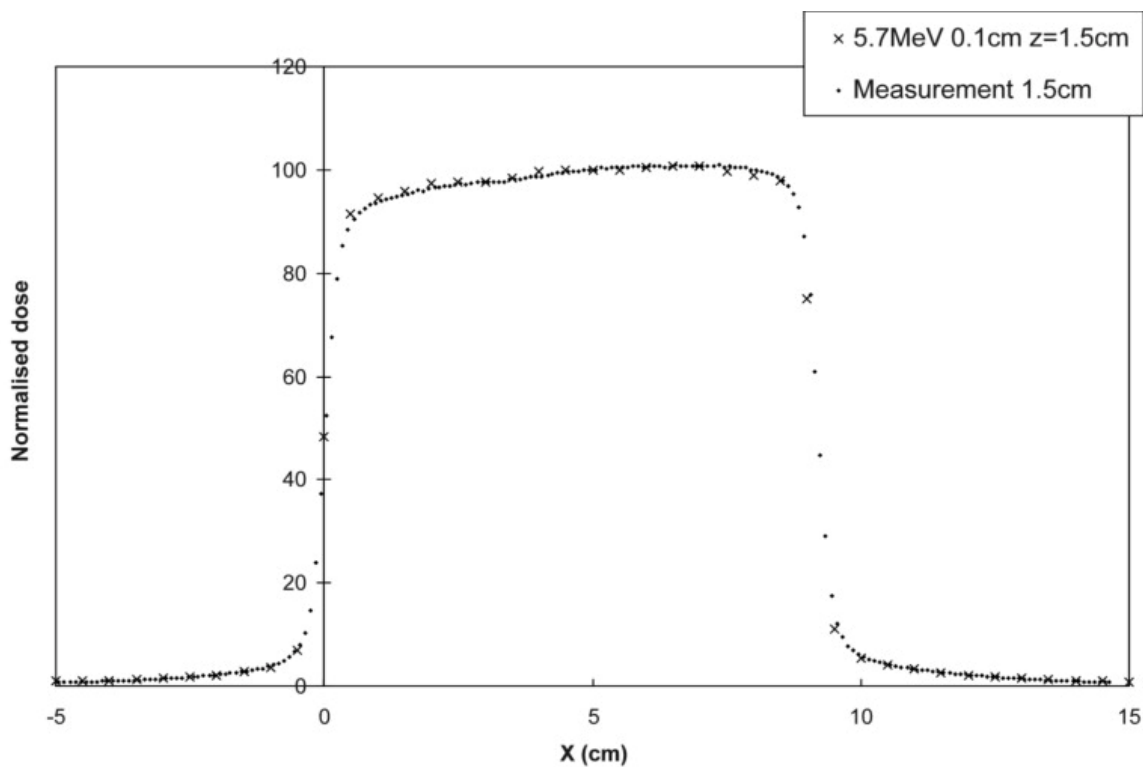
The two special cases of lateral profiles are: one asymmetric 10x10 cm² field and one rectangular 4x20 cm² field. The diagrams in which measured and simulated data are compared are shown in Figures 17 and 18. The asymmetric field is analysed at two depths, namely 1.5 cm and 5 cm and the rectangular field at 1.5, 5, 10 and 20 cm depths. Measurements are performed for the different asymmetric fields whereas the symmetry of the Monte Carlo model allows for the simulated data to be mirrored and reused.



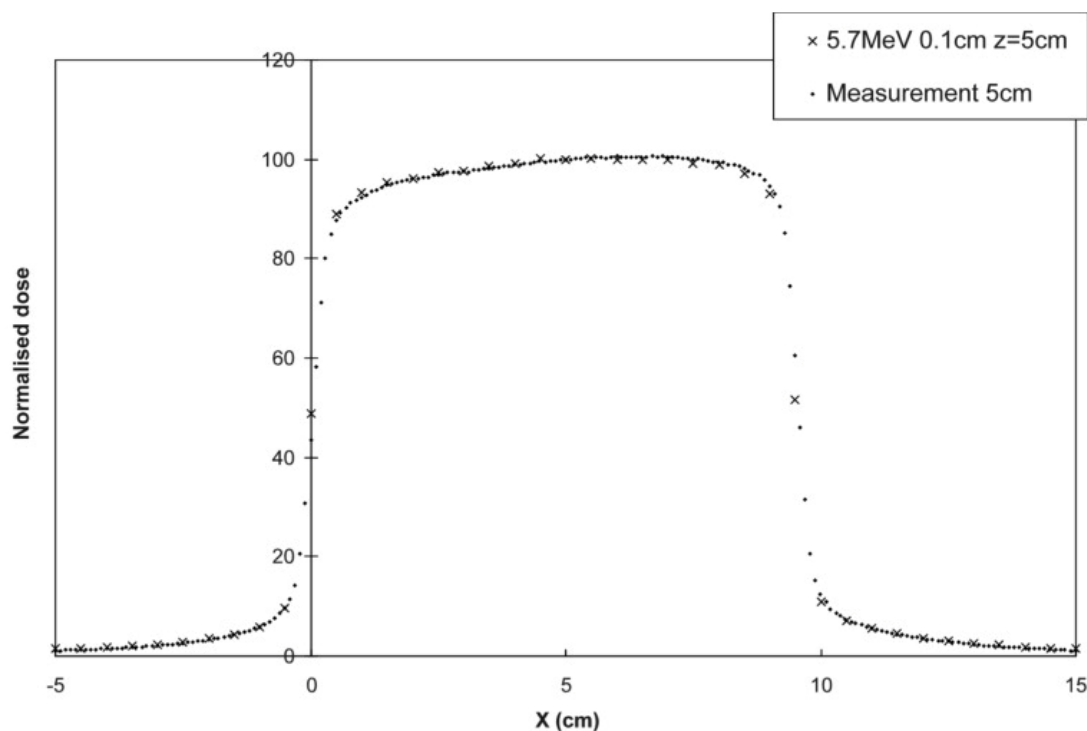
(a)



(b)

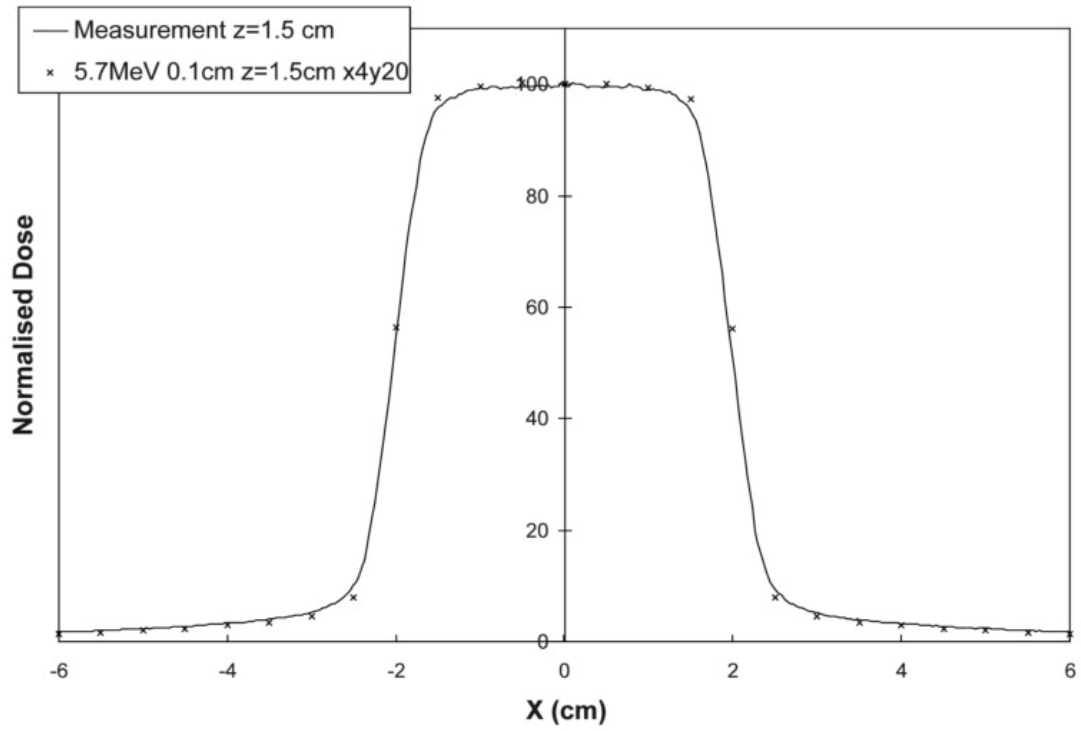


(c)

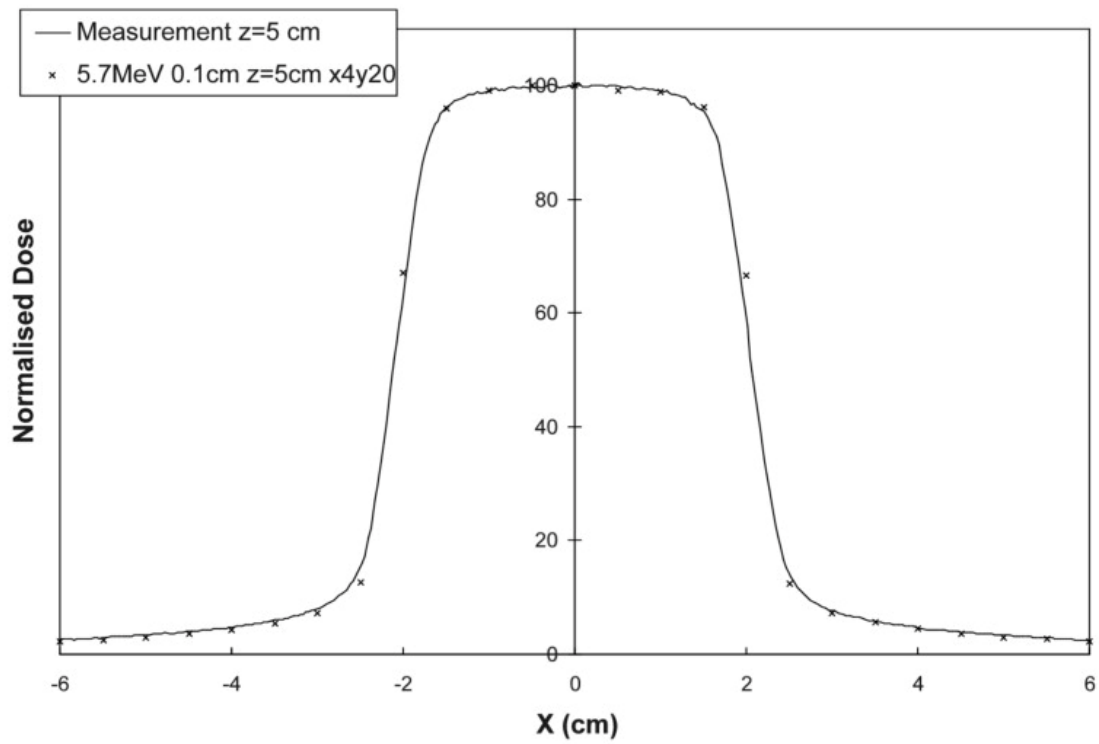


(d)

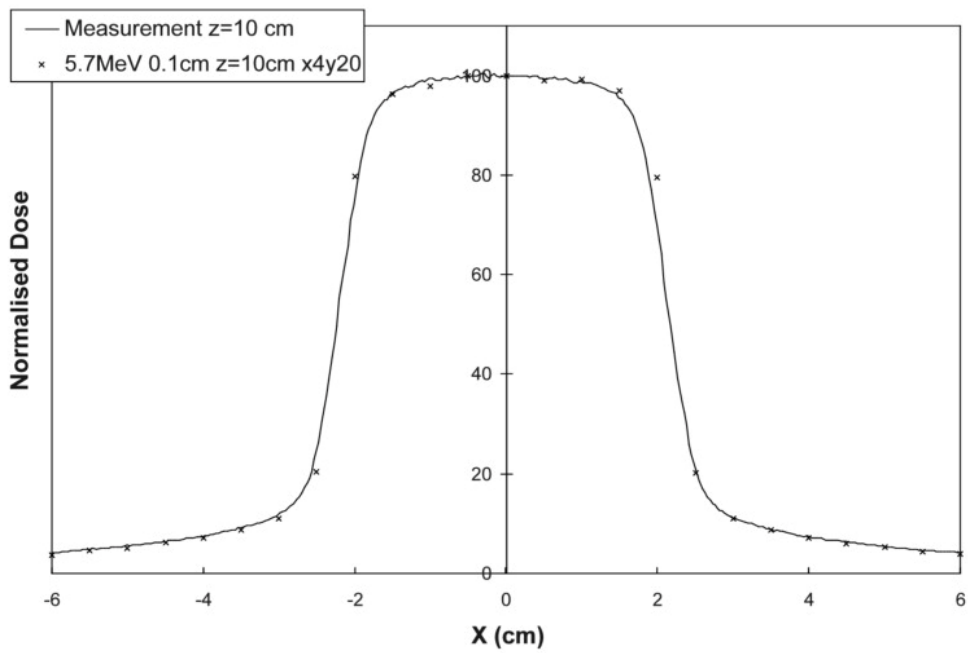
Figure 17: Dose profiles for 10x10 cm² asymmetric field in water phantom at a) 1.5 cm, b) 5 cm, c) 1.5 cm, d) 5 cm depth. Dots measured (CC04) and x simulated data. Simulated data from a) and b) mirrored in the dose-axis and used in the comparison in c) and d).



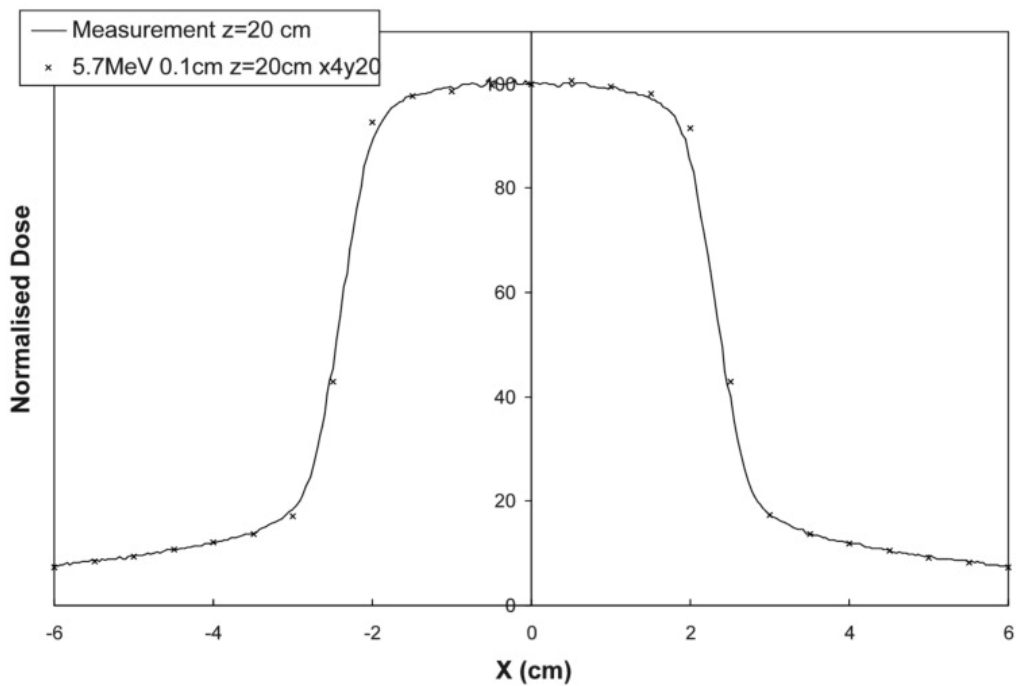
(a)



(b)



(c)



(d)

Figure 18: Dose profile for symmetric but rectangular field 4 cm in the x-direction (crossline) and 20 cm in the y-direction (inline) in water phantom at a) 1.5 cm, b) 5 cm, c) 10 cm, d) 20 cm depth. Solid line measured and discrete points (x) simulated data.

4 Remarks and discussion

The parameter optimisation is made with the future utilisation of the model in mind, in particular, to simulate radiation treatment of breast and lung cancer. The model is fitted to produce accurate dose distributions for various field sizes and depths but not perfectly to reproduce a certain single profile or depth dose distribution. For example, the fit of a depth-dose curve is never perfect but a compromise between dose-maximum at correct depth and good fit deeper along the curve. The accuracy of the model should be additionally tested when applied to other radiation treatment situations, e.g. verification of small field characteristics when simulating IMRT treatments.

The parameter set finally chosen for modelling of Varian Clinac iX accelerator (treatment room 8 at the radiation treatment department at Sahlgrenska University Hospital) is found to be 5.7 MeV monoenergetic electrons normally incident on the target with a Gaussian spatial distribution with FWHM 0.1 cm. Those parameter values are within the variations of the results obtained by other authors cited in the Introduction.

The off-axis distance in the in-air experiment is chosen with intention to avoid large errors from detector positioning in steep gradient regions. In general, the choice of off-axis distance may affect the resulting optimum energy from the in-air simulations. However, in this study the results from the in-air experiment analysis are regarded only as first approximation and we believe that the choice of the off-axis distance does not influence the final parameter set obtained.

All simulated data points in the depth dose curves deviate less than 1% of the dose at dose maximum from the measured data, except for the data points around dose max in a $2 \times 2 \text{ cm}^2$ field. A maximum deviation of 1% (of the dose in dose maximum) deviation is further fulfilled in all profiles, except for those at 1.5 cm depth, where the maximum deviation is 1.7%, 1.4% and 1.5% for 10×10 , 20×20 and $40 \times 40 \text{ cm}^2$ field sizes respectively. The simulated output factors for fields smaller than 20 cm could be assessed to within 1.65% of the measured output factors.

The output factors could be more correctly assessed by doing a complete simulation of the monitor chamber in the accelerator head. In this way eventual effects due to backscatter to the monitor chamber from the JAWS could be accounted for. [Ding2003] report such approach for a Varian CL2100EX linear accelerator model. The changes in dose to the monitor chamber per incident electron hitting the target for a 6 MV beam when

varying field size are in the order of the deviation between measured and simulated data in this work.

Future work includes modelling of 15 MV beams and MLC-component to be able to simulate clinical fields with more complicate shapes. The developed model can also be the base for analytical modelling of the accelerator head which would enable simulation of dynamic wedges and IMRT fields with dynamic delivery.

Acknowledgements

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6 Appendix

Depth dose simulations - build-up region

Depth dose distributions are simulated in two different ways denoted A and B:
A) by the module CHAMBER in BEAMnrc using version released 2005
B) by DOSXYZ code using version released 2009 and file format .IAEAphsp

Simulations by the CHAMBER module are initially made with poor resolution in the build-up region and then a simulation with 1mm resolution between 0.1 and 2 cm depth is performed. The results from method A and B are compared in Figure 19 and 20. The DOSXYZ-simulations are made in 1 cm² square pixels and the CHAMBER simulations are made in standing cylinders with 0.75 cm radius and 0.5 cm height.

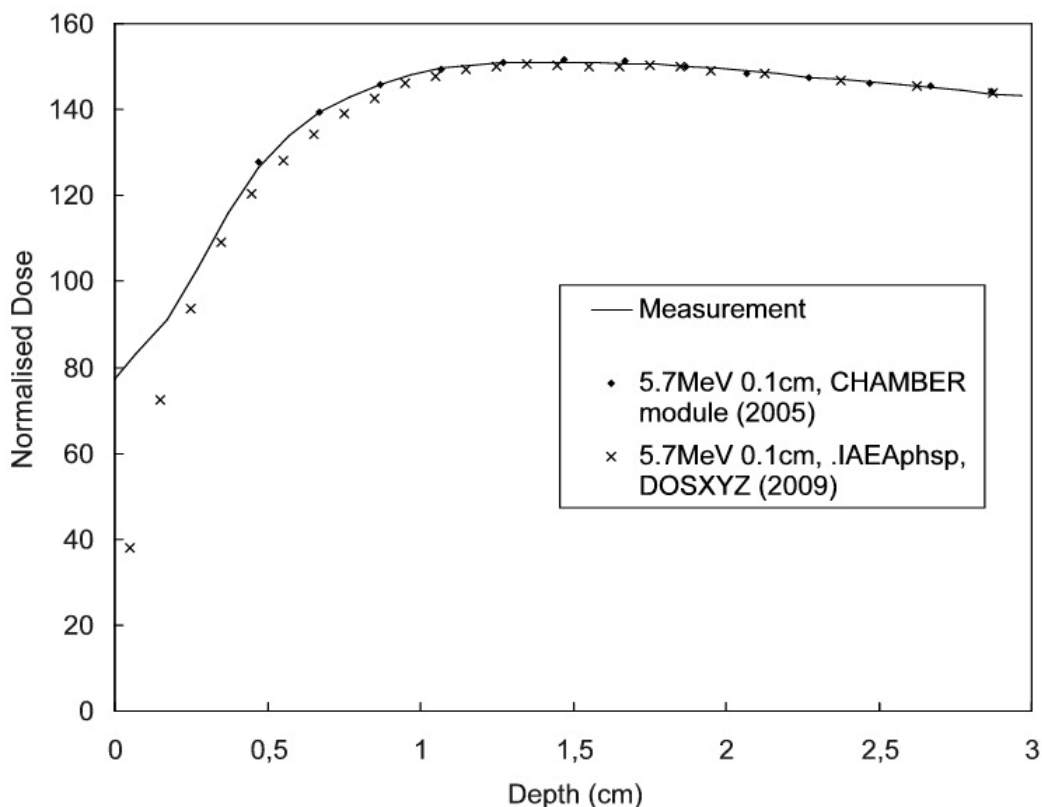


Figure 19: Simulation by the module CHAMBER with poor resolution in the build-up region compared to simulation made with DOSXYZ (x). Difference is seen at shallow depths. Solid line shows measured depth dose (CC13). Beyond dose maximum the two methods/versions overlap. Additional investigation and a literature study is needed to understand the differences in versions and methods and to understand which one is most correct.

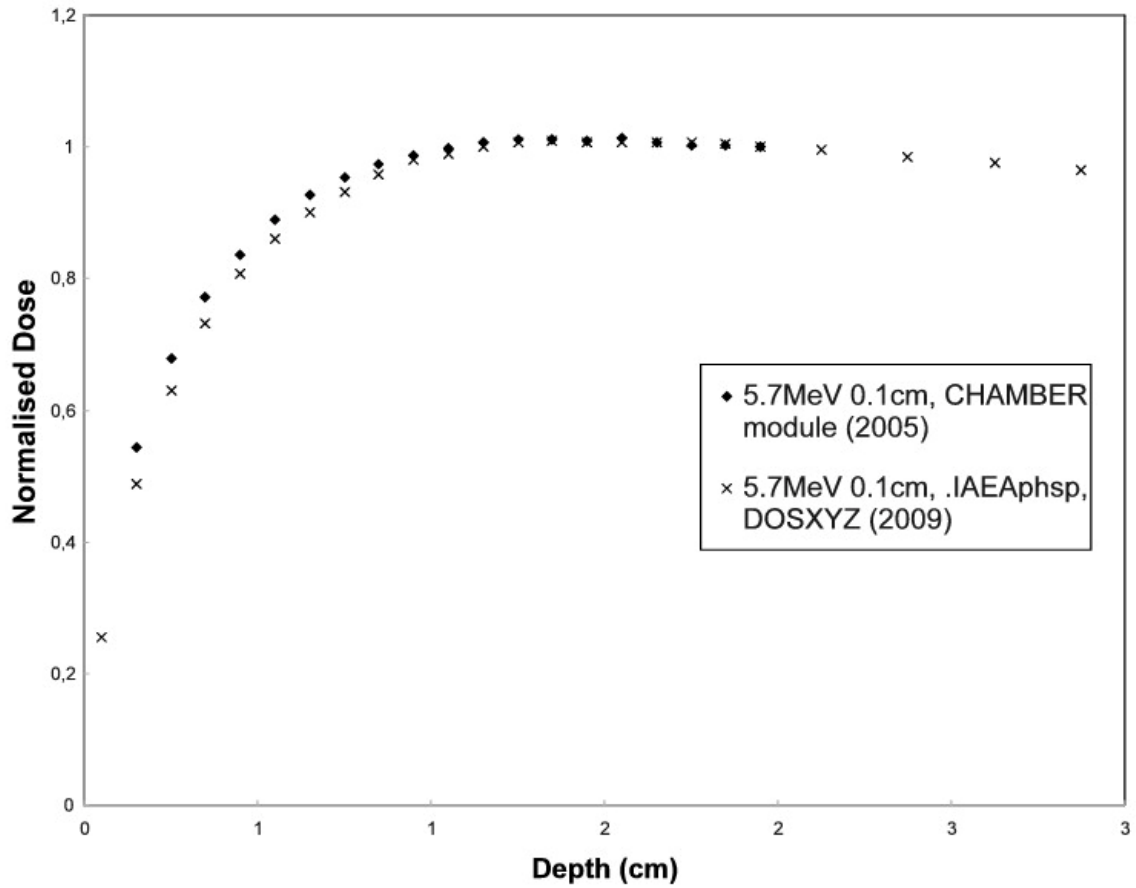


Figure 20: Simulation by the CHAMBER module with 1 mm resolution in the region 0.1-2cm depth compared to simulation with DOSXYZ (x – the same curve as in Figure 19). Differences seen at shallow depths.

Excerpt of BEAMnrc list file

```

NRCC CALN: BEAMnrc(EGSnrc) Vnrc(Rev 1.78 of 2004-01-12 11:44:06-05),
(USER_MACROS Rev 1.5)
ON i686-pc-1-gnu 15:09:20 Sep 25 2009
*****
**
** BEAMnrc
**
** Code developed at National Research Council of Canada as part of
** OMEGA collaboration with the University of Wisconsin.
**
** This is version V1 of BEAMnrc (Rev 1.78 last edited 2004-01-12 11:44:06-05**
**
*****

Max # of histories: to run 10000000 To analyze 10000000
Incident charge -1
Incident kinetic energy 5.700 MeV

Bremsstrahlung splitting DIRECTIONAL
splitting field radius 20.000 cm
splitting field SSD 100.000 cm
splitting no. in field 1000
e+/e- will be split at plane 20 in CM 3:
Z of splitting plane 12.500 cm
Z of Russian Roulette plane 12.300 cm
Radial redistribution of split e+/e- ON
Photon force interaction switch OFF
SCORING PLANES: # CM #
-----
1 7
Phase space files will be output at EVERY scoring plane
Range rejection switch ON
Range rejection in 61 regions
Automatic ECUTRR used starting from 0.700 MeV
Range rejection based on medium of region particle is traversing
Maximum electron ranges for restricted stopping powers:
kinetic Range for media 1 through 5
energy (g/cm**2)
(MeV) AIR700IC W700ICRU CU700ICR W700ICRU KAPTON70
0.200 6.072 0.002 0.002 0.002 0.005
0.400 84.941 0.010 0.016 0.011 0.070
0.600 178.342 0.020 0.033 0.021 0.146
1.000 383.457 0.041 0.069 0.043 0.317
1.500 651.119 0.069 0.118 0.072 0.543
2.000 921.052 0.097 0.167 0.101 0.775
4.000 1984.479 0.208 0.362 0.217 1.714
5.700 2862.394 0.301 0.527 0.314 2.511
Discard all electrons below K.E.: 2.000 MeV
if too far from closest boundary
Maximum cputime allowed 900.00 (hrs)
Initial random number seeds 25 30
LATCH_OPTION = 2: Latch values inherited, origin of
secondary particles recorded.

=====

Electron/Photon transport parameter

=====

Photon cross sections PEGS4
Photon transport cutoff (MeV) AP (medium)
Pair angular sampling KM
Pair cross sections BH

```



```

Triplet production           Off
Bound Compton scattering     ON
Radiative Compton corrections Off
Rayleigh scattering          OFF
Atomic relaxations           OFF
Photoelectron angular sampling ON

Electron transport cutoff(MeV) AE (medium)
Bremsstrahlung cross sections NIST
Bremsstrahlung angular sampling KM
Spin effects                  On
Electron Impact Ionization   OFF
Maximum electron step in cm (SMAX) 0.1000E+11
Maximum fractional energy loss/step (ESTEPE) 0.2500
Maximum 1st elastic moment/step (XIMAX) 0.5000
Boundary crossing algorithm    EXACT
Skin-depth for boundary crossing (MFP) 3.000
Electron-step algorithm        PRESTA-II

```

=====

Material summary 5 Materials used

```

*****
# Material          density(g/cm**3)  AE (MeV)  AP (MeV)  UE (MeV)  UP (MeV)
-----
1 AIR700ICRU        1.205E-03  0.700    0.010    55.511    55.000
2 W700ICRU          1.930E+01  0.700    0.010    55.511    55.000
3 CU700ICRU         8.933E+00  0.700    0.010    55.511    55.000
4 W700ICRU18        1.800E+01  0.700    0.010    55.511    55.000
5 KAPTON700ICRU     1.420E+00  0.700    0.010    55.511    55.000
*****

```

SOURCE PARAMETERS

```

INITIAL PARTICLES are Electrons
PARALLEL BEAM WITH 2-D GAUSSIAN X-Y DISTRIBUTION
ON FRONT FACE at Z= 0.0000 cm
BEAM SIGMA= 0.0425 cm (FWHM= 0.1000 cm)
X,Y,Z DIRECTION COSINES = ( 0.00000  0.00000  1.00000)

KINETIC ENERGY OF SOURCE = 5.700 MeV

```