

DOCTORATE THESIS

On the phase-space distribution of heavy particles in  
turbulence

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Turbulent fluids laden with small, heavy particles are common in nature. From-  
nent examples of such turbulent suspensions are water droplets in warm clouds,  
as well as particulate matter or living organisms in the turbulent upper layer of  
oceans. Because of their inertia, heavy particles tend to distribute inhomogeneously  
over phase-space, and over configuration space. This phenomenon is referred to  
as clustering, and it is believed to have a strong impact on the rate of collisions  
between particles. The collision dynamics, in turn, is crucial for the time evolution  
of turbulent suspensions, as collisions enable the particles to grow in size.

In this thesis, I study the phase-space distribution of heavy particles in turbu-  
lence in terms of a simplified, statistical model that qualitatively captures the particle  
dynamics on the smallest length scales of turbulence. I use methods from dynam-  
ical systems theory, and the theory of large deviations, to describe the long-time  
behaviour of the particle distribution. In most parts of the thesis, I investigate sus-  
pensions of identical particles, and study statistical observables that characterise  
clustering in phase-space, and in configuration space.

For these 'mono-disperse' suspensions I analyse phase-space clustering in a  
one-dimensional limit by computing the large-deviation statistics of phase-space  
finite-time Lyapunov exponents, and the phase-space Rnyi dimensions. Spatial  
clustering is studied by projecting the phase-space dynamics to configuration space.  
I show how the large-deviation statistics of spatial finite-time Lyapunov exponents is  
affected by this projection, and the effects it has on the spatial correlation dimension.  
Finally, I extend the analysis to particle suspensions of two different sizes. I  
show that this 'poly-dispersivity' has a strong effect on the phase-space distribution  
of particles, where it leads to a plateau in the distribution of separations and relative  
velocities.

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